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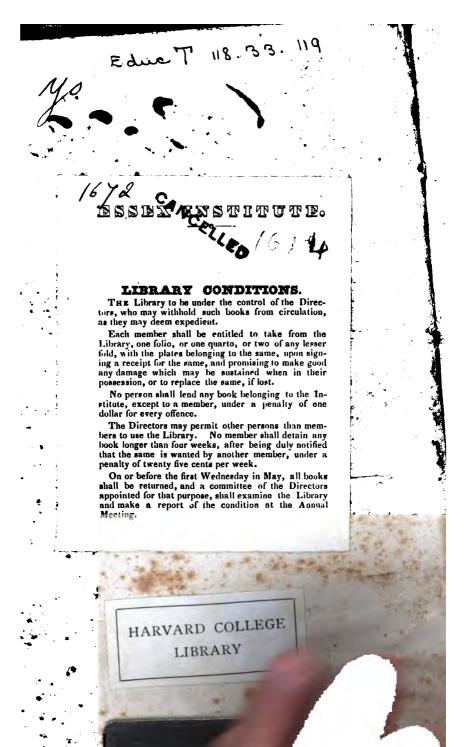
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SCHOLAR'S ARITHMETIC:

OR,

FEDERAL ACCOUNTANT:

CONTAINING.

- I. COMMON ARITHMETIC, the Rules and Illustrations.
- II. EXAMPLES and ANSWERS with BLANK SPACES, sufficient for their operation by the Scholar.
- III. To each RULE a SUPPLEMENT, comprehending, 1. QUESTIONS on the Nature of the Rule, its Use and the manner of its OPERATIONS.
 2. EXERCISES.
- IV. FEDERAL MONEY, with rules for all the various operations in it, to reduce Federal to Old Lawful, and Old Lawful to FEDERAL MONEY.
 - V. INTEREST cast in FEDERAL MONEY, with Compound Multiplication,
 Compound Division, and Practice, wrought in Old Lawrel and in Federal
 Money; the same questions being put in separate columns on the
 same page in each kind of money, these two modes of
 account become contrasted, and the great advantage gained by reckoning in Federal
 Money easily discerned.
- VI. DEMONSTRATIONS by Engravings of the reason and nature of the various steps in the extraction of the Square and Come Roots, not to be found in any other treatise on Arithmetic.

VH. FURNS OF NOTES, DREDS, BONDS and other INSTRUMENTS of WARTING.

THE WHOLE IN A FORM AND METHOD ALTOGETHER NEW, FOR THE EASE OF THE MASTER AND THE GREATER PROGRESS OF THE SCHOLAR.

BY DANIEL ADAMS, M. B.

STEREOTYPE EDITION, REVISED AND CORRECTED, WITH ADDITIONS.

KEENE, N. H.—PRINTED BY JOHN PRENTISS,

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Sold at his Bookstore, and by the principal Booksellers in the New-England States
and New-York.—1833

Price io Dollars per dosen, 1 Dollar single.

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MELHUE ARTHUR PLIMPTON

JANUARY 25, 1924

Newhampshire District, ss.

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BE IT REMEMBERED, that on the seventeenth day of July, in the thirty ninth year of the Independence of the United States of America, Dakiel ADAMS, of Mont Vernon, in said District, bath deposited in this office the Title of Apans, of Mont Vernon, in said District, hath deposited in this office the Title of a Book, the right whereof he claims as Антнов, in the following words, to wit:—" The Scholar's Arithmetic: or Federal Accountant. Containing t. Common Arithmetic, the Rules and Illustrations.—II. Examples and Answers, with blank spaces sufficient for their operation by the Scholar.—III. To each Rule, a Supplement, comprehending, I. Questions on the nature of the tule, its. usa, and the manner of its operations.—2, Exercises.—IV. Federal Money, with rules for all the various operations in it, to reduce Federal to Old Lawful, and Old Lawful to Federal Money.—V. Interest cast in Federal Money with Compound Multiplication, Compound Division and Practice wrought in Old Lawful and in Federal Money, the same pare in in Federal Money, the same questions being put in separate columns on the same page in each kind of money, by which these two modes of account become contrasted, and the great advantage gained by reckoning in Federal Money easily discerned.—VI. Demonstrations by engravings of the reason and nature of the various steps in the extraction of the Square and Cube Roots, not to be found in any other treatise on Arithmetic.—VII. Forms of Notes, Deeds, Boads; and other instruments of writing.—The whole has form and method altogether new, for the case of the Master and the greater progress of the Scholar.—By DANIEL ADAMS, M. B."

In conformity to the act of Congress of the United States, entitled "an act for the encouragement of Learning, by securing the copies of Mays, Charts and Books, to the authors and proprietors therein mentioned, and extending the benefit thereof to the arts of Designing, Engineering, Etching, Historical and other prints.

G. W. PRESCOTT, Clerk of the U.S. Court, N. H. District.

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PREFACE.

IT is fourteen years since the first Edition of the Scholar's Arithmetic was offered to the Public. It has now gone through nine editions, and more than Forty Themand copies have been circulated. In those places where it has been introduced, it never has, to the best of our knowledge, been supersaded by any other work which has come in competition with it. A knowledge of these facts is, perhaps, one of the best recommendations which can be desired of the work.

It has now madergone a careful revisal. Some of the rules have been thought to be deficient in examples; in this revised edition, more than sixty new examples have been added maden the different rules. Some have expressed andesine that answers might be given to the "Miscellancous Questions," at the end of the book; these have been added accordingly, and the number of these questions increased. But what more particularly claims attention in this revised edition, is the introduction of the rule of Exchange, where the pupil is made acquainted with the different currencies of the several states, (that of S. Carolina and Georgia, only excepted,) and how to change these currencies from one to another; also, to Federal Money, and Federal Money to these several currencies. This has been done more particularly with a view to the accommodation of the State of New-York, and other more southern states, where this work has already acquired a very considerable circulation. Answers are given to many of the questions in different currencies, so that the pupil in N. England, N. York, &c. will find an answer to the question, each in the currency of his own particular state. 2114 B &

These comprehend the only additions in the present new edition.

We have now the testimony of many respectable Teachers to believe, that this work, where it has been introduced into Schools, has proved a very kind assistant towards a more speedy and thorough improvement of

Scholars in Numbers, and at the same time, has relieved masters of a heavy burden of writing out Rules and Questions, under which they have so long labored, to the manifest neglect of other parts of their Schools.

To answer the several intentions of this work, it will be necessary that it should be put into the hands of every Arithmetician: the blank after each example is designed for the operation by the scholar, which being first wrought upon a slate, or waste paper, he may afterwards transcribe into his book.

The Supplements to the Rules in this work are something nest; experience has shown them to be very useful, particularly those. "Questions," unanswered, at the beginning of each Supplement. These questions the pupil should be made to study and reflect upon, till be can of himself devise the proper answer. They should be put to him not only once, but again, and again, till the answers shall become as familiar with him as the numbers in his multiplication Table. The Exercises in each supplement may be omitted the first time going through the book, if thought proper, and taken up afterwards as a kind of review.

Through the whole it has been my greatest care to make myself intelligible to the scholar; such rules and remarks as have been compiled from other authors are included in quotations; the Examples, many of them are extracted; this I have not hesitated to do, when I found them suited to my purpose.

Demonstrations of the reason and nature of the operations in the extraction of the Square and Cube Roots have never been attempted in any work of the kind before to my knowledge; it is a pleasure to find these have proved so highly satisfactory.

Grateful for the patronage this work has already received, it remains only to be observed that no pains nor exertions shall be spared to merit its continuance.

provide at the key placement of the second of DANIEL ADAMS.

Mont-Vernon. (N. H.) December 26th, 1815.

RECOMMENDATIONS.

New-Salem, Sept. 14th, 1801. HAVING attentively examined " The Scholar's Arithmetic," I cheerfully give it as my epinion that it is well calculated for the instruction of youth, and that it will abridge much of the time row necessary to be spent in the communication and attainment of such Arithmetical knowledge as is proper for the discharge of business.

WARREN PIERCE. Preceptor of New-Salem Academy.

Groton Academy, Sept. 2, 1801.

Sim....I have perused with attention "The Scholar's Arithmetic," which you transmitted to me some time since. It is in my opinion, better calculated to lead students in our Schools and Academies into a complete knowledge of all that is useful in that branch of literature, then any other work of the kind I have seen. With great sincerity I wish you success in your exertions for the promotion of useful learning; and I am confident that to be generally approved your work needs only to be generally known.
WILLIAM M. RICHARDSON

Preceptor of the Academy.

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Extract of a Letter from the Hon. John WHEELOCK, IL. D. President of Dartmouth College, to the Author.

"The Scholar's Arithmetic is an improvement on former productions of the same nature. Its distinctive order and supplement will help the learner in his progress; the part on Fe deral Money makes it more useful; and I have no doubt but the whole will be a new fund. derai Money makes it more contry."

September 7th, 1907.

The Scholar's Arithmetic contains most of the important Pales of the Art, and something, also, of the curious and entertaining kind.

The subjects are handled in a simple and concise manner.

Sec. 16

While the questions are few, they exhibit a considerable variety. While they are gene-

raily easy, some of them afford scope for the exercise of the Scholar's judgment.
It is a good quality of the Book, that it has so much to do with Federal Money.

The plan of showing the reasons of the operations in the extraction of the Square and Cube Roots is good. DANIEL HARDY, Jun. Preceptor of Chesterfield Academy.

er er er er er**spigtig sik** systeme Extract of a Letter from the Rev. Language Agreeworth of Jaffrey, to the publisher of the fourth Edition, dated August 3, 1807.

"The superiority of the Scholar's Arithmetic to any book of the kind in my knowledge, clearly appears from its good effect in the schools I annually visit. - Previous to its introduction, Arithmetic was learned and performed mechanically; since, scholars are tible to give a rational account of the several operations in Arithmetic, which is the best proof of their having learned to good purpose."

CONTENTS.

Introduction	Numeration
SECT	ION I.
Fundamental Rui	ce of Arithmetic.
Simple Addition	Simple Division
SECTI Rules essentially necessary for every person to but	
Fractions 68. Decimal Fractions 69. Federal Money 80 Exchange 84 Table to reduce shillings and pence to cents and mills 7 Tables of Exchange 92 Interest 95	Method of casting Interest on Notes and Bonds when par- tial payments at different times have been made Compound Interest
SECTI	ON III.
Rules occasionally useful to men	in particular employments of life.
Evolution 157 Evolution 157 Extraction of the Square Root 158 Demonstration of the reason and nature of the various steps in the operation of extracting the Square Root 167 Extraction of the Cube Root 167 Demonstration of the reason and nature of the various steps in the operation of extracting the Cube Root 168 Single Fellowship 177 Double Fellowship 179 Bartar 182	Examples for measuring wood 189 Boards 190 1
Loss and Gain	The Axle
Duodecimals	•
RECT	TON IP. The State of the State
Form of Notes - 211 Bonds - 212	Notes, &c. Deeds 214 Indenture - 216 Will - 216

ARITHMETIC is the art or science which treats of numbers.

It is of two kinds, theoretical and practical.

The THEORY of Arithmetic explains the nature and quality of numbers, and demonstrates the reason of practical operations. Considered in this sense. Arithmetic is a Science.

PRACTICAL ARITHMETIC shews the method of working by numbers, so as to be most useful and expeditious for business. In this sense Arithmetic and the control of the second control of

DIRECTIONS TO THE SCHOLAR.

DEPPLY impress your mind with a sense of the importance of arithmetical knowledge. The great concerns of life can in no way be conducted without it. Do not, therefore, think any pains too great to be bestowed for so noble an end. Drive far from you idleness and sloth; they are great enemies to improvement. Remember that youth, like the morning, will soon be past, and that opportunities once neglected, can never be regained. First of all things, there must be implanted in your mind a fixed delight in study; make it your inclination; "A desire accomplished is sweet to the soul." Be not in a hurry to get through your book too soon. Much instruction may be given in these few words, understand EVERY THING AS YOU GO ALONG .--Each rule is first to be committed to memory; afterwards, the examples in illustration, and every memerk is to be perused with care. There is not a word inserted in this Treatise, but with a design that it should be studied by the Scholar. As much as possible, endeavour to do every thing of yourself; one thing found out by your own thought and reflection, will be of more real use to you, than twenty things told you by an Instructor. Be not overcome by little seeming difficulties, but rather strive to overcome such by patience and application; so shall your progress be easy and the object of your endeavours sure the property of the first of the property of the property of the first of the first

the control of the continues in the property of the property of the property of the control of t On entering upon this most useful study, the first thing which the Scholar

The first section is a first of NOTATION. The grade ways the product of the section of the secti Novations is the art of expressing numbers, by certain characters or figures : of which there are two methods. -1. The Roman method, by Letters. 2: The Anglie method, by Figures The latter is that of general present In the Arabic method all numbers are expressed by these ten characters or figures.

Unit; or two; three; four; five; six; seven; eight; nine; cypher one [or nothing.

The nine first are called significant figures, or digits, each of which standing by itself or alone, invariably expresses a particular or certain number; thus, 1 signifies one, 2 signifies two, 3 signifies three, and so, of the rest, until you come to nine, but for any number more than nine, it will always require two or more of those figures set together in order to express that number. This will be more particularly taught by

NUMERATION.

Numeration teaches how to read or write any sum or number by figures. In setting down numbers for arithmetical operations, especially with beginners, it is usual to begin at the right hand, and proceed towards the left.

EXAMPLE. If you wish to write the sum or number 537, begin by setting down the seven, or right hand figure, thus 7, next set down the three, at the left hand of the seven, thus 37, and lastly the five, at the left hand of the

three, thus 587, which is the number proposed to be written.

In this sum thus written you are next to observe that there are three places, meaning the situations of the three different figures, and that each of these places has an appropriated name. The first place, or that of the right hand figure, or the place of the 7, is called unit's place; the second place, or that of the figure standing next to the right hand figure, in this the place of the 3, is called ten's place; the third place, or next towards the left hand, or place of the 5, is talled hundred's place; the next or fourth place; for we may suppose more figures to be connected, is thousand's place; the next to this tens of thousand's place, and so on to what length we please, there being particular names for each place. Now every figure signifies differently, accordingly as it may happen to occupy one or the other of these places.

The value of the first or right hand figure, or of the figure standing in the place of units, in any sum or number, is just what the figure expresses standing alone or by itself; but every other figure in the sum or number, or those to the left hand of the first figure, have a different signification from their true or natural meaning, for the next figure from the right hand towards the left, or that figure in the place of tens, expresses so many times ten, as the same figure signifies units or ones when standing alone, that is, it is ten times its simple primitive value; and so on, every removal from the right hand figure, making the figure thus removed ten times the value of the same

figure when standing in the place immediately preceding it.

Hund. Tens. Units.

EXAMPLE. Take the sum 3 3 3, made by the same figure three times repeated. The first or right hand figure, or the figure in the place of units, has its natural meaning or the same meaning as if standing alone, and signifies three units or ones; but the same figure again towards the left hand in the second place, or place of tens, signifies not three units, but three tens, that is thirty, its value being increased in a tenfold proportion; proceeding on still further towards the left hand, the next figure or that in the third place, or place of handreds signifies neither three nor thirty, but three hundred, which is ten times the value of that figure, in the place immediately preceding it, or that in the place of tens. So you might proceed and add the figure 3, lifty or

an hundred times, and every time the figure was added, it would signify ten times more than it did the last time.

A Cyphen standing alone is no signification, yet placed at the right hand of another figure it increases the value of that figure in the same tenfold proportion, as if it had been preceded by any other figure. Thus 3, standing slone, signifies three; place a cypher before (30) and it no longer signifies three, but thirty; and another cypher (300) and it signifies three hundred.

The value of figures in conjunction, and how to read any sum or number agreeably to the foregoing observations, may be fully understood by the following

THE words at the head of the Table shew

read all the remaining numbers in the Table.

*TABLE.

the signification of the figures against which they stand; and the figures shew how many of that signification are meant. Thus Units in the first place signify ones, and 6 standing against it, shews that six ones or individuals are here meant; tens in the second place shew that every figure iff this place means see many tens, and 3 standing against it, shews that three tens are here meant, equal to thire 2 1 8 3 6 ty, what the figure really signifies. Hundreds against it, shews that six ones or individuals sthat three tens are here meant, equal to thir-6 2 1 4 6 3 1 2 in the third place shew the meaning of fig-1 3 0 2 5 0 3 7 6 1 5 ures in this place to be Hundreds, and 8 9.821064 shews that eight hundreds are meant. 0 2 1 3 6 7 5 the same manner the value of each of the re-6 3 2 7 2 9 1 maining figures in the table is known. Hav-1 2 3 4 6 3 2 ing proceeded through in this way, the sum 2 3 4 5 6 7 of the first line of figures or those immedi-8 9 0 9 8 ately against the words, will be found to be 7 6 5 4 Two Billions, one hundred sixty seven thou-1 2 3 sands, two hundred and thirty-five Millions; 4.5 four hundred twenty-one thousands; eight hun-7 dred and thirty-six. In the like manner may be

Those words at the head of the Table are applicable to any sum or number, and must be committed perfectly to memory so as to be readily applied on any occasion.

For the greater ease of reckoning, it is convenient and often practised in public offices, and by men of business, to divide any number into periods and half periods, as in the following manner:

Hundreds thouse, of bill. & Tenthrons.
The thousand billions of Hundred billions & Hundred billions of Billions.
Hundred thous. of mill. & Thousand pinillions.
Thousand millions.
Thousand millions.
Hundred millions.
Millions.
Ten millions.
Ten thousands & Hundred thousands & Hundred thousands & Hundreds.
Thousands & Hundreds.
Thousands & Hundreds.
Thousands & Hundreds.

The first six figures from the right hand are called the unit period, the next six the million period, after which the trillion, quadrillion, quintillion periods, &c. follow in their order.

Thus by the use of ten figures may be reckoned every thing which can be numbered; things, the multitude of which far exceeds the comprehen-

sion of man.

+

"It may not be amiss to illustrate by a few examples the extent of numbers, which are frequently named without being attended to. If a per son employed in telling money, reckon an hundred pieces in a minute and continue at work ten hours each day, he will take seventeen days to reckon a milion; a thousand men would take 45 years to reckon a hiling. If we suppose the whole earth to be as well peopled as Britain, and to have been so from the creation, and that the whole race of mankind had constantly spent their time in telling from a heap consisting of a quadrillion of pieces, they would hardly have yet reckoned a thousandth part of that quantity."

After having been able to read correctly to his instructor, all the numbers in the foregoing Table, the learner may proceed to write the follow-

ing numbers out in figures.

Two hundred and sixty-three.

Five thousand one hundred and sixty.

One hundred thousand, six hundred and four

Five million, eighteen thousand, seven hundred & six.

Two million, six hundred and fifty thousand, one hundred and thirty-seven.

Seven hundred and ninety-four million, one hundred and forty-nine thousand, five hundred and twenty.

Three thousand, nine hundred and forty million four hundred and two thousand, eight hundred and four.

Five hundred thirty six thousand, two hundred and seventy two million, one hundred and three thousand and six.

Four billion, six hundred thousand million, seven hundred thousand, two hundred and ninety-two.

Explanation of the Characters made use of in this Work.

The sign of equality; as 100 cts=1 Dol. signifies that 100 cents are equal to 1 dollar.

Saint George's Cross, the sign of addition; as 2+4=6, that is, 2 added to 4 are equal to 6.

The sign of subtraction; as 6—2=4; that is, 2 taken from 6 leaves 4.

Saint Andrew's Cross, the sign of multiplication; as $4 \times 6 = 24$; that is, 4 times 6 are equal to 24.

Reversed Parentheses, the sign of division; as 3)6(2, that is, 6 divided by 3 the quotient is 2, or 6; 3-2.

The sign of proportion; as 2:4::8:16, that is, as 2 is

to 4 so is 8 to 16.

SECTION I.

FUNDAMENTAL RULES OF ARITHMETIC.

THESE are four, Addition, Subtraction, Multiplication, and Division; they may be either simple or compound; simple, when the numbers are all of one sort or denomination; compound, when the numbers are of different denominations.

They are called, Principal or Fundamental Rules, because all other rules and operations in arithmetic are nothing more than various uses and repetitions of these four rules.

The object of every arithmetical operation, is, by certain given quantities which are known, to find out others which are unknown. This cannot be done but by changes effected on the given numbers; and as the only way in which numbers can be changed is either by increasing or diminishing their quantities, and as there can be no increase or diminution of numbers but by one or the other of the above operations, it consequently follows, that these four rules embrace the whole art of Arithmetic.

1. SIMPLE ADDITION.

SIMPLE ADDITION is the putting together of two or more numbers, of the same denomination, so as to make them one whole or total number, called the sum, or amount.

RULE.

1. Place the numbers to be added one under another, with units under units, tens under tens, &c. and draw a line under the lowest number.

2. Add the right hand column, and if the sum be under ten, write it under the column; but if it be ten, or any exact number of tens, write a sypher; and if it be not an exact number of tens, write the excess above tens at the foot of the column, and for every ten the sum contains, carry one to the next column, and add it in the same manner as the former.

3. Proceed in like manner to add the other columns, carrying for the tens of each to the next, and set down the full sum of the last or left hand

column,

PROOF.

Reckon the figures from the top downwards, and if the work be right this amount will be equal to the first;—or, what is often practised, "cuist off the upper line of figures and find the amount of the rest; then if the mount and upper line when added, be equal to the sum total, the work is supposed to be right."

EXAMPLES.

1. What will be the amount of . . . 3 6 1 2 dolls. dollars when added together?

Here are four sums given for addition; two of them contain units, tens, hundreds, thousands; another of them contains units, tens, hundreds; and a fourth contains units only. The first step to prepare these sums for the operation of addition, is to write them down, units under units, tens under tens, &c. thus ;---

	T. of Thos	to Thousand	9. Hundrede.	Ten.	to Units.	dollars
1		8	0	4 5	3 1 3	dollars dollars dollars
	1	2	3	0	9	dollar s

Answer, or Amount,

Amount of the three lower lines.

1 2 3

To find the answer or amount of the sums given to be added, begin with the right hand column, and say, 3 and 1 make 4, and 3 are 7, and 2 are 9, which sum (9) being less than ten, set down directly under the column you added. Then proceeding to the next column, say again; 5 and 4 are 9, and 1 is 10; being even ten, set down 0, and carry one to the next column, saying 1, which I carry to 6 is 7, and 0 is nothing, but 6 make 13; which sum (13) is an excess of 3 over even ten; therefore set down 3 and carry 1 for the ten to 8 in the next column, saying 1 to 8 is 9, and 3 are 12; this being the last column, set down the whole number (12) placing the 2, or unit figure directly under the column, and carrying the other figure, or the 1, forward to the next place on the left hand, or to that of Tens of thousands, and the work is done.

Proof.

It may now be required to know if the work be right. To exhibit the method of proof let the upper line of figures be cut off as seen in the example. Then adding the three lower lines which remain, place the amount (8697) under the amount first obtained by the addition of all the sums, observing carefully that each figure fall directly under the column which produced it; then add this last amount to the upper line which you cut off; thus 7 to 2 are 9; 9 to 1 are 10; carry one to 6 is 7 and 6 are 13; 1 which I carry again to 8 is 9 and 3 are 12, all which being set down in their proper places, and as seen in the example, compare the amount (12309) last obtained, with the first amount (12309) and if they agree, as it is seen in this case they do, then the work is judged to be right.

Note.—The reason of carrying for ten in all simple numbers is evident from what has been taught in Notation. It is because 10 in an inferior column is just equal in value to 1 in a superior column. As if a man should be holding in his right hand half pistareens, and in his left, dollars. If you should take 10 half pistareens from his right hand, and put one dellar into his left hand, you would not rob the man of any of his money, because 1 of these pieces in his left hand is just equal in value to 10 of these in his Mestical of the artic

right hand.

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SUPPLEMENT TO ADDITION.

THE attentive acholar who has understood, and still carries in his mind what has already been taught him of Addition, will be able to answer his instructor to the following QUESTIONS.

- 1. What is simple Addition ?
- 2. How do you place numbers to be added?
- 3. Where do you begin the addition?
- 4. What is the answer called?
- 5. How is the sum or amount of each celumn to be set down?
- 6. What do you observe in regard to setting down the sum of the last column ?
- 7. Why do you carry for ten rather than any other number ?
- 8. How is addition proved?

Norz. Should the learner find any difficulty in giving an answer to the above questions, he is advised to turn back and consult his Rule, with its illustrations. EXERCISES.

- 1. What is the amount of 2801 dollars; 765 dollars; and of 397 £210 at one time, £76 at another, collars, when added together?
- 2. Suppose you lend a neighbour £17 at another, and £9 at another. Ans. 3963 dollars. What is the sum lent? Ans. £312.

Nors. The scholar who looks at greatness in his class, will not be discouraged by a little difficulty which may at first occur in stating his question, but will apply himself the more closely to his Rule, and to thinking, that if possible he may be able himself to answer what another may be obliged to have taught him by his instructor.

3. A tree was broken off by the wind, 27 feet from the ground; the part broken off was 71 feet long; what was the height of that tree before it was broken?

4. A man being asked his age, said he was 27 years old when he married, and he had been married 15 years. What was the man's 'ge?

5. Washington was born in the year of our Lord 1732; he was 67 years old when he died; in what year of our Lord did he die?

Ans. 1799.

6. There are two numbers; the less number is 8761, the difference between the numbers is 597; what is the greatest number?

8. At the late Census, taken

A. D. 1810, the number of inhabit-

ants in the several New-England

States was as follows; viz. Mains, 228705; N. Humpshire, 214460;

Vermont, 217895; Ma. achusetts,

472040; Rhode-Island, 76931, Con-

necticut, 261942; what was the num-

ber of inhabitants at that time in

New-England ?

Au. 9358.

Ans. 1471973.

7. From the Creation to the departure of the Israelites from Egypt was 2513 years; to the siege of Troy, 307 years more; to the building of Solomon's temple, 180 years; to the building of Rome, 251 years; to the expulsion of the kings from Rome, 244 years; to the destruction of Carthage, 363 years; to the death of Julius Casar, 102 years; to the Christian ara, 44 years; required the time from the Creation to the Christian ara?

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Ans. 4004.

10. A gentleman left his son, 2475 dollars more than his daughters, whose fortune was 25 thousand, 25 hundred, and 25 dollars; what was

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amount of the whole estate?

Ans. Son's portion, 30000.

Whole estate, 57525.

the son's portion, and what was the

9. There are five numbers, the first is 2617; the second 893; the third 1702; the fourth as much as the three first; and the fifth twice as much as the third and fourth; what is the whole sum?

Ans. 24252.

2. SIMPLE SUBTRACTION.

SIMPLE SUBTRACTION is taking a less number from a greater of the same denomination, so as to shew the difference or remainder; as 5 taken from 8, there remains 3.

The greater number (8) is called the Minuend, the less number (5) the Subtrakend, and the difference (3) or what is lest after Subtraction, the Remainder.

RULE.

" Place the less number under the greater, units under units, tens under tens, and so on. Draw a line below; then begin at the right hand, and subtrace each figure of the less number from the figure above it, and place the remainder directly below. When the figure in the lower line exceeds the figure above it, suppose 10 to be added to the upper figure; but in this case you must add I to the under figure in the next column before you subtract it. This is called, borrowing ten."

PROOF.

Add the remainder and subtrahend together, and if the sum of them correspond with the minuend, the work is supposed to be right.

Minuend The numbers being placed with the larger uppermost, as the rule directs, I begin with the Subtrahend 5 unit or right hand figure in the subtrahend, and say, 1 from 3 there remain 2, which I set Remainder 8 down, and proceeding to tens, or the next figure. 3 3 7 from 5 I cannot, I therefore borrow, or sup-Proof pose ten to be added to the upper figure (5) which make 15, then I say 7 from 15 and there remain 8, which I set down: then proceeding to the next place, I say, I which I borrowed to 2 is 3, and 3 from 6 and there remain 3; this I set down, and in the next place I say 5 from 8 and there remain 3, which I set down and the work is done. Proof. I add the remainder to the subtrahend, and finding the sum just

equal to the minuend, suppose the work to be right.

Note. The reason of borrowing ten, will appear if we consider, that, when two numbers are equally increased by adding the same to both, their difference will be equal. Thus the difference between 3 and 5 is 2; add the number 10 to each of these figures (3 and 5) they become 13 and 15, still the difference is 2. When we proceed as above directed, we add or suppose to be added, 10 to the minuend, and we likewise add one to the next higher place of the subtrahend, which is just equal in value to 10 of the lower place.

2.							the minuend, the subtrahend.

Remainder.

Note.—In case of borrowing ten, it is a matter of indifference, as it respects the operation, whether we suppose ten to be added to the upper figure, and from the sum subtract the lower figure and set down the difference; or, as Mr. Pike directs, first subtract the lower figure from 10, and adding the difference to the figure above, set down the sum of this difference and the upper figure. The latter method may perhaps be thought more easy, but it is conceived, that it does not lead the understanding of youth so directly into the nature of the operation as the former.

1.	Take	1	_	_	_	_	-	-	 _	_	-	_	_	 _	8	_
	Rem.		· ·		<u> </u>				 					 		
2.	From Take	1													6 8	
	Rem.	_							 _	: .	_			 		

3. From 21468317012101, take 568497067382. Rem. 20899819944719

- 4. From 364710825193, take 279403865746. Rem. 85306959447
- Rem. 78337564775. 5. From 168012372458, take 89674807683.
- 6. From 100610828734; take 99874197867. Rem. 736330867. 7. From 628103670126, take 248976539782. Rem. 379127030344.
 - 8. From 10000, take 9999. Rem. 1. 9. From 10000, take 1. Rem. 9999.

The distance of time since any remarkable event, may be found by subtracting the date thereof from the present year.

EXERCISES. 1. How long since the Ameri-

Williams Committee to the second of the second

8 1 7 present time.

7 6 date of Ind.

Ans. 4 1 years since.

2. King Charles, the martyr, was beheaded 1648: how many years is it since ?

So, likewise, the distance of time from the occurrence of one thing to that of can Independence, which was another, may be found by subtracting the declared in 1776? date of the thing first happening, from that of the last.

EXAMPLE.

1. How long from the discovery of America by Columbus, 1492, to the commencement of the war, 1775, which gained our Independence?

2 8 3 years.

2. How long from the termination of the war in 1783, which gained our Independence, to the commencement of the last war between the United States and Great Britain in 1812? Ans. 29 years.

SUPPLEMENT TO SUBTRACTION.

QUESTIONS.

- 1. What is Simple Subtraction?
- 2. How many numbers must there be given to perform that operation ?
- 3. How must the given numbers be placed?
- 4. What are they called?
- 5. When the figure in the lower number is greater than that of the upper number from which it is to be taken, what is to be done?
- 6. How does it appear that in subtracting a less number from a greater. the occasional borrowing of ten does not affect the difference between these two numbers?
- 7 How is subtraction proved?

EXERCISES.

1. What is the difference between 78360 and 5421?

Ans. 72939.

- 2. From a piece of cloth that measured 691 yards, there were sold 273 yards; how many yards should there remain?
- 3. There are two numbers, whose difference is 375; the greater num-taken from 175 leaves 96? ber is 862; I demand the less? Ans. 487.

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- 5. Suppose a man to have been born in the year 1745, how old was he Ans. 54 years. -in 1799?
 - 6. What number is that to which if you add 789 it will become 6350? Ans. 5561:
- 7. Supposing a man to have been 63 years old in the year :1801; in Ans. in the year 1738. what year was he born?
- ment year wat is 8. At the census in 1900, the number of inhabitants in the New-England States was 1233011; at the late census in 1810, the number was 1471937; What was the increase of the population in the New-England States in the Ans. 238926. ten years between 1800 and 1810 ?

§ 3. SIMPLE MULTIPLICATION.

SIMPLE MULTIPLICATION teaches, having two numbers given of the same denomination, to find a third which shall contain either of the two given numbers as many times as the other contains a unit. Thus, 8 multiplied by 5, or 5 times 8 is 40—The given numbers (8 and 5) spoken of together, are called Factors. Spoken of separately, the first or largest number (8) or number to be multiplied, is called the Multiplicand; the less number (5) or number to multiply by, is called the multiplier, and the amount (40) the Product.

Before any progress can be made in this rule, the following Table must be committed perfectly to memory.

			MIC	Jai L'I	PLIC	JAI.	ION	TABI	JEJ.		
ī	2	3	4	5	6	7	8	9	10	11	12
2	1 4	6	8	10	12	14	16	18	20	22	24
3	6	9	12	15	18	21	24	27	30	33	36
4	8	12	16	20	24	28	32	36	40	44	48
-5	10	15	20	25	30	35	40	45	50	55	60
6	12	18	24	30	36	42	48	54	60	66	72
7	14	21	28	35	42	49	56	63	70	77	84
8	16	24	32	40	48	56	64	72	.80	88	96
9	18	27	36	45	54	63	72	81	90	99	108
i0	20	30	40	50	60	70	80	90	100	110	120
11	22	33	44	55	66	77	88	99	110	121	132
12	24	36	48	60	72	84	96	108	120	132	144

MULTIPLICATION TABLE.

By this table the product of any two figures will be found in that square which is on a line with the one and directly under the other. Thus, 56 the product of 7 and 8, will be found on a line with 7 and under 8: so 2 times 2 is 4; 3 times 3 is 9, &c.—In this way the table must be learned and remembered.

RULE.

1. Place the numbers as in Subtraction, the larger number uppermost with units under units, &c. and then draw a line below.

2. When the multiplier does not exceed 12 to begin at the right hand of the multiplicand, and multiply each figure contained in it by the multiplier, set-

ting down all over even tens and carrying as in addition.

3. When the multiplier exceeds 12; multiply by each figure separately, first by the units of the multiplier, as directed above, then by the tens, and the other figures in their order, remembering always to place the first figure of each product directly under the figure by which you multiply; having gone through in this manner with each figure is the multiplier, add their several products together, and the sum of them will be the product required.

EXAMPLES.

Multiply 5291 by 3.
 OPERATION.
 9 1 Multiplicand.
 3 Multiplier.

1 5 8 7 3 Product.

The numbers being placed as seen under the operation, say—3 times 1 is 3; which set down directly under the multiplier; then 3 times 9 is 27; set down 7 and carry 2. Again 3 times 2 is 6 and 2 I carry is 8; set down 8: then lastly, 3 times 5 is 15, which set down, and the work is done.

2. What is the product of 4175 multiplied by 37?

> 2 9 2 2 5 Prod. by the unit (7) of the mul-1 2 5 2 5 Product by the tens (3) [tiplier

1 5 4 4 7 5 Product or answer.

In this example, as the multiplier exceeds 12, therefore you must multiply by each figure separately. First, by the units (7) just in the manner of the other example. Secondly by the tens (3) in the same way excepting only, that the first figure of the product in the multiplication by 3, must be placed under the 3, that is, under the figure by which you multiply.

Lastly, add these two products together, and the sum of them is the answer.

Proof —The better way of proving Multiplication is by Division: but till the pupil shall have been instructed in that rule he may make use of the following

METHOD.

Cast the nines out of the Multiplicand, and set the remainder at the right hand of a cross; do the same with the Multiplier and set the remainder at the left hand of the cross; then multiply the figures at the right and left of the cross together, cast the nines out of the product, and set the remainder over the cross; also cast the nines out of the answer or product of the multiplicand and multiplier, and set the remainder under the cross, which will be the same as that over it if the work be right.

Note.—To east the nines out of any number, proceed thus: beginning at the right hand of the number, add the figures; when the sum exceeds 9, drop the sum and begin anew, by adding, first, the figures which would express it. Pass by the nines, and when the sum comes out exactly 9, neglect it; what remains after the last addition, will be the remainder sought; for example—suppose it be required to cast the 9's out of 576394, proceed thus:—5 to 7 is 12, which sum (twelve) as it exceeds 9 you must drop, and beginning anew, first add the figures (12) which would express twelve, saying 1 to 2 is 3 (proceeding with the other figures which remain to be added) and 6 are 9, being exactly nine, neglect it, and begin again; 3 to 9 are twelve; again drop the sum (twelve) and add the figures (12) which would express it, 1 to 2 is 3 and 4 are 7, which sum (7) is the remainder after the addition, or the thing sought, and is the remainder that would be defined after dividing the 576394 by 9.

3. Multiply 7 6 5 3 0 2 Multiplicand. 6 5 Multiplier.

4	9	7	4	. 4	6	3	0	Product.	1
4	5	9	1	8	1	. 2	,		2 × 5
							0		1
								•	PROOF.

Proof. I cast the 9's out of the Multiplicand and set the remainder (5) at the right hand of the cross; I do the same with the Multiplier, and set the remainder (2) at the left hand of the cross; these remainders I multiply together, and casting out the 9's from the product (10) the remainder is 1, which I set at the top of the cross; I then cast out the 9's from the Product (49744630) and set the remainder (1) at the bottom of the cross, which as it agrees with the remainder at top, I suppose the work to be right.

There is nothing more easy than proving Multiplication by this method so soon as the scholar shall have given it such attention, as to make it a little familiar.

Note. Should the Multiplier or Multiplicand, either or both, be less than 9, they are to be taken as the remainders.

4 Multiply 37846 by 235. Product, 8893810. 5. Multiply duct, 98

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5. Multiply 14356 by 646 Product, 9802688.

6. Multiply 29631 by 952. Pi - duct. 28599112.

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7. Multiply 93956 by 8704. Product, 817793024.

8.	Multiply 9	8	7	0	4	5	6	3	by	7	5	6	0	4	Prod.	7462459781052
9.	•	3	4	6	2	3	2	1	-	9	6	4	8	4	• '	334058579364
10.	•		5	2	7	5	3	5	-	1	5	7	2	8	•	8297070480
11.	•		2	7	5	8	2	7	-	1	9	7	2	5	•	5440687575
12.	•		6	9	6	3	7	4	- 4	6	3	9	5	7	-	323087591918

Contractions and varieties in Multiplication.

Any number which may be produced by the multiplication of two or more numbers, is called a composite number. Thus 15 which arises from the multiplication of 5 and 3, (3 times 5 is 15) is a composite number; and these numbers, 5, and 3, are called component parts. Therefore,

1. If the multiplier be a composite number; multiply first by one of the component parts, and that product by the other; the last product will be

the answer sought.

EXAMPLES.

1. Multiply 6 7 by 1 5 OPERATION.

67

5 one of the component parts.

3 3 5

3 the other component part.

1 0 0 5 Product of 67 mult. by 15.

2. Multiply 367 by 48, Product, 17616.

OPERATION.

Consider first what two numbers mutiplied together will produce 48; that is, what are the component parts of 48?—Answer, 6 and 8 (6 times 8 is 48) therefore multiply 367 first by one of the component parts, and the product thence arising by the other; the last product will be the answer sought.

3. Mult. 583 by 56. Prod. 32648. 4. Mult. 1086 by 72. Prod. 78192. OPERATION.

^{2. &}quot;When there are cyphers on the right hand of either the multiplicand or multiplier, or both, neglect those cyphers; then place the significant figures under one another, and multiply by them only; add them together as before directed, and place to the right hand as many cyphers as there in both the factors."

EXAMPLES.

1. Multiply 65430 by 5200.

OPERATION. 5 4 3 0 5 2 0 0

Here in the multiplication of 65430 by 5200, the cyphers are seen neglected, and regard paid only to the significant figures. To the product are annexed 3 cyphers; equal to the number of cyphers neglected in the factors.

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2. Mult. 3 6 5 0 0 8. Mult. 78000 by 600. 7 3 0 mar and make a

Product, 46800000.

3. When there are cyphers between the significant figures of the multiplier, omit the cyphers and multiply by the significant figures only, placing the first figure of each product directly under the figure by which you multiply, and adding the products together, the sum of them will be the product of the given numbers.

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EXAMPLES.

1. Mult. 154326 by 3007. OPERATION.

> 154326 3007

1080282 462978

464058282

In this example, the cyphers in the multiplier are neglected, and 154326 multiplied only by 7 and by 3, taking care to place the figure in each product directly under the figure from which it was obtained.

3. 4 8 8 7 6 8 5 0 4 0 0 0 3 0

1 9 5 9 2 2 0 9 3 0 5 5 0 0

4. When the Multiplier is 9, 99, or any number of 9's, annex as many cy pher's to the Multiplicand, and from the number thus produced, subtract the multiplicand, the remainder will be the product.

EXAMPLES.

1. Mult. 6547 by 999

OPERATION.

6 5 4 7 0 0 0

6 5 4 7

6 5 4 0 4 5 3

Write down the Multiplicand, place as many cyphers at the right hand as there are 9's in the Multiplier for a minuend; underneath write again the multiplicand for

underneath write again the multiplicand for a Subtrahand, subtract, and the remainder is the product of 6547 multiplied by 999.

2. 6473 99 Product, 640827 3. 7021 99 Product, 695079

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5 8 8 4 9 7 8 Product, 53844375024

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SUPPLEMENT TO MULTIPLICATION.

QUESTIONS.

- 1. What is Simple Multiplication?
- 2. How many numbers are required to perform that operation ?
- 3. Collectives are together, what are the given numbers called ?
- 4. Separately what are they called?
- 5. What is the result, or number sought, called?
- 6. In what order must the given numbers be placed for multiplication?
- 7. How do you proceed when the multiplier is Jess than 12?
- 8. When the multiplier exceeds 12 what is the method of procedure?
- 9. What is a composite number?
- 10. What is to be understood by the component parts of any number?
- 11. How do you proceed when the multiplier is a composite number?
- 12. When there are cyphers on the right hand of the multiplier, multiplicand, either or both, what is to be done?
- 13. When there are cyphers between the significant figures of the multiplier, how are they to be treated?
- 14. When the multiplier consists of 9's how may the operation be contracted?
- 15. How is Multiplication proved?
- 16. By what method do you proceed in casting out the 9's from any number ?
- 17. How is Multiplication proved by casting out the S's?

EXERCISES.

that each may receive 115 dollars. Ans. 3105.

1. What sum of money must ... Norz. The scholar's business in all be divided between 27 men, so questions for Arithmetical operations, is wholly with the numbers given; these are never less than two; they may be more, and these numbers in one way or another, are always to be made use of to find the answer. To these, therefore, he must direct his attention, and carefully consider what is proposed by the question to be known.

- 2. An army of 10700 men having plundered a city, took so much money, that when it was shared among them, each man received 46 dollars; what was the sum of money Ans. 492200. taken?
- 3. There were 175 men employed to finish a piece of work, for which each man was to receive 13 dollars: what did they all receive?

Ans. 2275.

- 4. Suppose a certain town contains 145 houses, each house two families, and each family 6 inhabitants; how many would be the inhabitants of that town? Ans. 1740.
- 5. If a man earn 2 dollars per week, how much will he earn in 5 years, there being 52 weeks in a year? Ans. 520 dolla

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6. How much wheat will 36 men 7. If the price of wheat he 1 dolthrash in 37 days, at 5 bushels per day each man?

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lar per bushel, and 4 bushels of wheat make I barrel of flour, what Ans. 6660 bushels. will be the price of 175 barrels of Bour ? Ans. 700 dolls.

Water Little

4. SIMPLE DIVISION.

SIMPLE DIVISION teaches, having two numbers given of the same denomination, to find how many times one of the given numbers contains the other. Thus, it may be required to know now many times 21 contains 7; the answer is 3 times. The larger number (21) or number to be divided, is called the Dividend; the lesser number (7) or number to divide by, is called the Divisor; and the answer obtained, (3) the Quotient.

After the operation, should there be any thing left of the Dividend, it is called the Remainder. This part, however, is uncertain; sometimes there is no remainder. When it does happen it will always be less than the divisor, if the work be right, and of the same name with the dividend.

RULE.

1. "Assume as many figures on the left hand of the dividend as contain "the divisor once or oftener; find how many times they contain it, and " place the answer as the highest figure of the quotient.

2. "Multiply the divisor by the figure you have found, and place the " product under that part of the dividend from which it was obtained.

3. "Subtract the product from the figures above it.

4. "Bring down the next figure of the dividend to the remainder and

" divide the number it makes up as before."

When you have brought down a figure to the remainder, if the number it makes up he still less than the divisor, a cycher must be placed in the quotient, and another figure brought down.

EXAMPLES.

1. Divide 127 by 5.

Divisor. Dividend. Quotient.

1 2 7 (2 5 5)

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The parts in Division are to stand thus, the dividend in the middle, the divisor on the left hand, the quotient on the right, with a half parenthesis on the right, with a half parenthesis separating them from the dividend.

2 Remainder.

Proceed in this operation thus—It being evident that the divisor (5) cannot be contained in the first figure (1) of the dividend, therefore assume the two first figures (12) and inquire how often 5 is contained in 12; finding it to be 2 times, place 2 in the quotient, and multiply the divisor by it, saying 2 times 5 is 10, and place the sum (10) directly under 12 in the dividend. Subtract 10 from 12 and to the remainder (2) bring down the next figure (7) at the right hand, making with the remainder 27. Again inquire how many times 5 in 27; 5 times; place 5 in the quotient, multiply the divisor (5) by the last quotient figure (5) saying 5 times 5 is 25, place the sum (25) under 27, subtract and the work is done. Hence it appears that 127 contains 5, 25 times, with a remainder of 2, which was left after the last subtraction.

This Rule, perhaps at first will appear intricate to the young student, although it is attended with no difficulty. His liability to errors will chiefly arise from the diversity of proceedings. To assist his recollection, let him notice that

1. Find how many times, ac.
2. Multiply,
3. Subtract.

(4. Bring down

It is sometimes practised to make a point (.) under the figures in the

dividend, as they are brought down, in order to prevent mistakes.

When the divisor is a large number, it cannot always certainly be known how many times it may be taken in the figures which are assumed on the left hand of the dividend till after the first steps in division are gone over, but the learner must try so many times as his judgment may best dictate, and after he has multiplied, if the product be greater than the number assumed, or that number in which the divisor is taken, then it may always be known that the quotient figure is too large; if after he has multiplied and subtracted, the remainder be greater than the divisor, then the quotient figure is not large enough, he must then suppose a greater number of times, and proceed again. This at first may occasion some perplexity, but he attentive learner after some practice, will generally hit on the right umber.

2. Let it be required to divide 7012 by 52.

OPERATIONDivisor. Dividend. Quotient.
5 2) 7 0 1 2 (1 3 4

. 2

181

252

4 4 Ranainder.

In this operation it is left for the scholar to trace the steps of procedure without having them particularly pointed out to him by words.

PROOF.

Division may be proved by multiplication.

RULE.

"Multiply the Divisor and Quotient together, and add the remander, if there be any to the product; if the work be right, the sum will be equal to the dividend."

Take the last Example.

The Quotient was 1 3 4 Multiply them together.

268

wings was a second

6 7 0 4 4 Remainder added.

7 0 1 2 Equal to the dividend.

Another and more expeditious way of proving Division is

By casting out the 9's: weeken to be seen in

Cast out the 9's from the Divisor and the Quotient, multiply the results and to the product, add the remainder if any after division; from the sum of these cast out the 9's, also cast out the 9's from the Dividend, and if the wolast results agree, the work is supposed to be right.

entry were the

6 8 Rem. 9's out of (Divid.) 17354 Rem. 2 1 together

4. Divide 153598 by 29. Quotient 5296. Rem. 14.

5 Divide 8893810 by 235. Quot. 37846.

8. Divide 30114 by 63. Quotient 478

7. Divide 9302688 by 648 Quot. 14356.

8 Divide 974932 by 365. Quotient 2671. Rem. 17

9. Divide 5221580 by 68705. Quot. 76.

10. Divide 3228242 dollars equally among 563 men; how many dollars must each man receive?

Ans. 5734.

From a view of the question, it is evident, that the dollars must be divided into as many parts as there are men to receive them; consequently, the number of dollars must be made the dividend, and the number of men the divisor; the quotient will then shew how many dollars each man must receive.

11. How many times does 1030603615 contain 3215?

Ans. 320561 times.

Contractions and varieties in Dirision.

I. When the divisor does not exceed 12, the operation may be performed without setting down any figures excepting the quotient, by carrying the computation in the mind. The units which would remain after subtracting the product of the quotient figure and the divisor from the figures assumed of the dividend, must be accounted so many tens, and be supposed to stand at the left hand of the next figure in the dividend, then consider again how often the divisor may be had in the sum of them. Proceed in this way till all the figures in the dividend have been divided. This is called short division. EXAMPLES.

1. Divide 732 by 3. OPERATION.

Here I say, how often 3 in 7, knowing it to be 2 times, I place 2 in the quotient, then considering that the quotient figure (2) and the divisor (3) multiplied together would be 6, and that this product

(6) subtracted from 7 in the dividend, would leave 1, I then consider this remainder (1) as standing at the left hand of the next figure (3) of the dividend, which together make 13. I now say how many times 3 in 13—4 times, therefore I place 4 in the quotient, which multiplied into the divisor (3) would be 12, and 12 subtracted from 13 would leave 1, which considered as standing at the left hand of the next or last figure (2) of the dividend would make 12; again, how many times 3 in 12-1 times-I then place 4 in the quotient, which multiplied into the divisor (3) is 12, this product (12) I consider as subtracted from 12, I find there will be no remainder, and the work is done.

2. Divide 37426 by 7.

OPERATION. 7) 3 7 4 2 6

Quot. 5 3 4 6 Rem. 4

- 3. Divide 310658023162 by 4 4. - - - 621075214621 - 5
- **5.** - 213524031628 6
- 6. - 306452706527 8

- - - 546321406968 - 9

Here I say how often 7 in 37? 5. times and two remain; then how often 7 in 24? 3 times and 3 remain; how often 7 in 32? 4 times and 4 remain; lastly, how often 7 in 46 ? 6 times, 4 remain.

Quot. 77664505790 124215042924 35587338604 38306588315 60702378552

II. When there are cyphere at the right hand of the divisor, cut them off, also out off an equal number of figures from the right hand of the dividend and place these figures at the right hand of the remainder.

A EXAMPLES to be received the street of the

1. Divide 6203946 by 5700.

OPERATION. 57 | 00)62039 | 46(1088 | · · · · · · · · ·

3. 18 & J. F.

 $V_{i}^{(1)} = \mathcal{X}_{i} V_{i}^{(1)} \mathcal{X}_{i}^{(2)}$

01	est e t
503 456	gd Au
479 456	opus a k

Here are two cyphers on the right hand of the divisor which I cut off, * And in also I cut off two figures (46) from the dividend and to the right hand of the remainder after the last division (23) Lplace the figures cut off from the dividend (46) which make the whole remainder 2346.

2. Divide 379432 by 6500 Quot. 58. Rem. 2439

3. Divide 2764503721'by 83000. Quot. 33307. Rem. 2272]

4. When the diveror is 10, 100, 1000, or 1, with any name of experies an nexed, cut off as many figures on the right hand of the dividend as there are cyphers in the divisor; the figures which remain of the dividend compose the quotient; those cut off, the remainder.

EXAMPLES.

- 1. Divide 1576 by 10. OPERATION.
- 1 | 0) 1 5 7 | 6
- Here we have one cypher in the divisor, therefore cut off one figure (6) from the dividend; what remains (157) is the quotient, and the figure cut off (6) the remainder.
- 2. Divide 3217 by 100. Quot. 32. Rem. 17.
 - 3. Divide 76421795 by 1000. Quest. 76421. Rem. 795

SUPPLEMENT TO DIVISION.

QUESTIONS.

- 1. What is Simple Division?
- 2. How many numbers must there be given to perform the operation?
- 3. What are the given numbers called?
- 4. How are they to stand for Division?
- 5. How many steps are there in Division?
- 6. What is the first? the second? the third? the fourth?
- 7. What is the result or answer called?
- 8. Is there any other or uncertain part pertaining to Division? What is it called?
- 9. Of what name or kind is the remainder?
- 10. What is short Division?
- 11. When there are cyphers at the right hand of the divisor, what is to be done?
- 12. What do you do with figures cut off from the dividend when there are cyphers cut off from the divisor?
- 13. When the divisor is 10, 100, or 1 with any number of cyphers annexed, how may the operation be contracted?
- 14. How many ways may Division be proved?
- 15. How is Division proved by Multiplication?
- 16. How may Division be proved by casting out the 9's?

EXERCISES.

- 1. Suppose an estate of 36582 dollars to be divided among 13 sons, how much would each one receive?

 Ans. 2814 dolls.
- 2. An army of 15000 men having plundered a city, and took 2625000 dollars, what was each man's share?

 Ans. 175 dolls.

- 3. A certain number of men were concerned in the payment of \$18950 and each man paid 25 dollars, what was the number of men ? Aus. 758.
- 4. If 7419 eggs be packed in 34 casks, how many in a cask? Ans. 218.

- 5. A farm of 375 acres is let for 1125 dollars; how much does it pay Ans. 3 dolls. per acre?
- 6. A field of 27 acres produces 675 bushels of wheat; how much is that per acre? Ans. 25 bushels.

- be 2555 dollars a year: how much by 13, that the product may be 871 is that per day, there being 365 days Ans. 7 dolls in a year
- 7. Supposing a man's income to 8. What number must I multiply Ans. 67.

5. COMPOUND ADDITION.

COMPOUND ADDITION is the adding of numbers which consist of articles of different value, as pounds, shillings, pence, and farthings, called different denominations; the operations are to be regulated by the value of the articles, which must be learned from the Tables.

RULE FOR COMPOUND ADDITION.

1. Place the numbers so that these of the same denomination may stand directly under each other.

2. Add the first column or denomination together, and carry for that number which it takes of the same denomination to make 1 of the next higher. Proceed in this manner with all the columns, till you come to the last, which must be added, as in Simple Addition.

1. OF MONEY.

TABLE 4 Farthings qr. 12 Pence 20 Shillings TABLE Penny, marked d. Shilling, s. Pound, £.

1. What is the sum of £61. 17s. 5d. £13. 3s. 8d. and of £5. 16s. 11d. when added together?

£. 61 13 5	s. 17 3 16	d.	Those numbers of the same denomination inder each other, as the rule directs.	placéd
80	18		*4	

I begin with the right hand column or that of pence, and having added it, find the sum of the numbers therein contained to be 24; now as 12 of this denomination make one of the next higher, or in other words 12 pence make one shilling, therefore in this or in the column of pence I must carry for 12; I now inquire how often 12 is contained in 24, the sum of the first column or that of pence; knowing it to be 2 times and nothing over, I set down 0 under the column of pence, and carry 2 to that of shillings, to be added into the second column, saying, 2 I carry to 6 are 8, and 3 are 11, and 7 are 18, and 10 to 18 are 28, and ten again are 38 (for so each figure in ten's place must be reckoned, I in that place, being equal in value to 10 units.) Now as 20 shillings make one pound, therefore in the column of shillings, I carry for 20; I then inquire how often 20 in 38? once, and 18 remains; therefore, I set down directly under the column of shillings 18, what 38 contains more than 20, and for the even 20 carry 1 to pounds of the last column, which is to be added after the manner of Simple Addition.

Note.—The method of proof for Compound Addition is the same as that

of Simple Addition.

	2.				•		3.		
£. 18 26 8	4 15 1	d. 11 3 7	qr 1 0 3		£. 371 5 68 7	2. 15 7 3	d. 6 4 2 5		9r. 2 0 1
	Supposing a	Pays for for	a dinner oats for	his hor		ı 1st da	y, - £0 - 0	1 0	- - - 6
·	15,	- for - for - for - to	r shoeing r supper r horse k r toll r breakfa the bart r dinner:	and lodg eeping 	ressing		- 0 - 0 - 0 - 0 - 0	1 2 1 1 2 1 3	2 0 10 6 0 6 5
Wh	at were the	gentie	man's exp	penses?	•	****			
	Suppose I a			n shillin	e and	ten ner	£.	*	~ 2 .
	Forty-one	-			_	·		• , •	
	Seventy-fi . Three po				s.		•		
Wh	nat is the su	m·I ow	e ?	. •	·	Anı		· · .	

6. A man purchases cattle; one yoke of oxen for £14 11 6; four cows, for £18 19 7; and other stock to the amount of £21 5; what was the knount of the cattle purchased?

Ans. £54 16s. 1d.

· è.

2. OF TROY WEIGHT.

By Troy Weight are weighed gold, silver, jewels, electuaries and liquors.

24 grains gra.	make one	Pennyweight,	marked part
20 Pennyweights		Ounce,	oz.
12 Ounces		Pound,	lb

EXAMPLES.

		1 .	
гь.	02.	pwt.	gra
70	. 10	13	• 4
3	9	7	• 1 ['] 8
28	0	0	5
7	3	6.	2

Because 24 grains make a pennyweight, you carry one to the pennyweight column for every 24 in the sum of the column of grains; because 20 penny-weights make one ounce, you carry for 20 in pennyweights, and because 12 ounces make one pound, you carry for 12 in the ounces. This is called carrying according to the value of the higher place.

				2.			
<i>lb.</i> 1 5 1 6 2 8	<i>oz.</i> 7 5 0	pwt. 1 9 6 1 4	. •	16.	oz. 7 2 1 1	pwi. 1 4 0 1 3	grs. 2 3 6 5
(4)	3	7	4	- 23.	10	·. 1 2	. 7
				Ž4			7
			1. T			;· ; - , - , - , - , - , - , - , - , - , -	
į.	, , , , , , , , , , , , , , , , , , ,			******			,
			•				

Note.—The fineness of gold is tried by fire, and is reckoned in carats, by which is understood the 24th part of any quantity; if it lose nothing in the trial, it is said to be 24 carats fine; if it lose 2 carats, it is then 22 carats fine, which is the standard for gold.

Silver which abides the fire without loss is said to be 12 ounces fine.—
The standard for silver coin is 11 oz. 2 pwts. of fine silver, and 18 verse of copper melted together.

3. OF AVOIRDUPOIS WEIGHT.

By Avoirdupois weight are weighed all things of a coarse and drossy nature, as tea, sugar, bread, flour, tallow, hay, leather, and all kinds of metals, except gold and silver.

	16 28 4	O P	ram unc ound	es ds ters	dr. weight	}	TABLE - make or	(Po Q	unce, ound, uarter of a 00 weight, on,	mazi hund. or 112	wei	ght, nds,	oz lb qr cwi
	-		, iunu	reu	weight	E	E <i>XAMPL</i> 1.	ÆS	•	on,			-4	
1 8	3 6 4 9 2		1	3 7 8 3	· · · · · · · · · · · · · · · · · · ·	97 2 0 3 1		2 2 2	5	oz. 1	7 7 2 5	1	dr. 8 6 5	

T.	cut.	gr.	и.	es .	dr
801	3	2	2 5	1 1	8
7	19	3	14	5	6
86	2	0	6	• 0	15
3	7	1	0	. 6	4

Note.—" 175 Troy ounces are precisely equal to 192 Avoirdupois Ounces, and 175 Troy pounds are equal to 144 Avoirdupois. 1 lb. Troy—5760 grains, and 1 lb. Avoirdupois—7000 grains."

4. OF TIME.

•	TABLE.	,	
60 Seconds s. 60 Minutes]	Minute, marked Hour	h.
24 Hours 7 Days	make one	week,	d. w.
4 Weeks 13 Months, 1d. & 1h.] [Month, * Julian Year,	mo. Y.

EXAMPLES.

ν,			255			
Y.	200 .	w.	d.	h.	m.	s.
16	10	3	6	23	57	43
28	7	2	5	16	28	3 2
39	6.	ì	3	17	38	11
8 7	4		1	1 4	15	17

				. 3	•	
Y.	mo.	70.	d	h.	m.	s.
8.9	11	3	6	2 2	45	36
36	10	2	5	6 "	5 5	44
8 7	2	1	0	1.1	22	3 3
3 6	4	3	3	5	, 8	7

The number of days in each Calendar month may be remembered by the following verse:

Thirty days hath September, April, June and November; February twenty-eight alone; all the rest have thirty-one.

* "The civil Solar year of 365 days being short of the true by 5h. 48m. 57s. occasioned the beginning of the year to run forward through the season nearly one day in four years on this account Julius Cæsar ordained that one day should be added to February every fourth year, by causing the 24th day to be reckoned twice: and because this 24th day was the sixth (sextilis) before the kalends of March, there were in this year two of these sextiles, which gave the name of Bissextile to this year, which being thus corrected, was, from thence called the Julian year."

5. OF MOTION.

TABLE.

60 Minutes	٠
30 Degrees 12 Signs, or	360
Degree	8

2 422/2220		
i :	Prime Minute, marked " Degree, Sign, The whole great circle of Zodiac.	•
make one	Sign, The whole great circle of	r. f tb

EXAMPLES.

	1.	•
•	•	
25	1 .7	18
17	49	56
6	3 5	24
10	17	16
2 5 1 7 6	1 7 4 9 3 5	5 6 2 4

•	:	2.	
•	1		
8.	•	•	•
9	. 8	5 5	4.4
1	26	4 4	5 5
8	1 8	8 6	1 2
1	: 9	₿3	2 2

6. OF CLOTH MEASURE.

TABLE.

Z	inches, one fifth in.
4	Nails, or 9 inches
4	Quarters of a yard or 36 inches
3	Quarters of a yard, or 27 inches
5	Quarters of a yard or 45 inches
	Quarters of a yard, or 54 inches
4	Quarters 1 inch and 1 fifth, or 37

LAKI.	7	. *	
	Ĺſ	Nail, # Quarter of a	arked na
		Quarter of a	yard, gr.
	;	Yard,	yd.
	,	Ell Flemish	Ĕ. Fl
make	one d	Ell English	E. E
	1	Ell French	E. Fr
)	EH Scotch	E. Sc.
	\ \frac{1}{2}	Ell Scotch Spanish Van	
	•		•

inches and one fifth
3 Quarters and two thirds

EXAMPLES.

	1.			2.	
Yds.	qrs.	n.	E. E.	qr.	ж.
6 1 4	3	3	19	3	2
36	1	2	5 6	1	3
7	0	1	7	2	2
1 5	3	2	18	2	0
-					

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7. OF LONG MEASURE.

By Long Measure are measured distances, or any thing where length is considered without regard to breadth.

	TABLE.	•	
3 Barley corns, bar. 12 Inches 3 Feet 51 Yards, or 161 feet 40 Poles 8 Furlongs 691 Statute miles, nearly, 360 Degrees	make one	Inch, marked Foot, Yard, Rod, Perch or Pole, Furlong, Mile, Degree of a great Circle. A great Circle of the Earth.	in. ft. yd. pol. fur. mile

							-			
	Dej	٠.	19	u.		fur.	pol.	ft.	in.	bar.
ı	Def 6	8	• 5	7		7	2.6	-i 5	11.	2
1	2	4	5	3		6	18	7	6	1
	7	9	3	6		1	7	. 9	10	0
		4		7		.3	. 0	3	2	1
					· .		·			

	•	S.	.		
Deg.	mi.	fur.	pol.	ſt.	in.
13	56	5	13	8	1
49	18	1	2.7	16	· 2
2:67	12	: :3	16	9	. 0
2 9	. 8	0	5	3	1
			·····		
		,			

F

8. OF LAND OR SQUARE MEASURE.

By Square Measure are measured all things that have length and breadth.

		TABLE.	
	Inches)	Square Foot.
	Feet	i l	— Yard.
50 1	Yards, or } Feet '		Pole.
4 0	Poles	make one {	Rood.
4	Roods 160 rods or 4840 yards		- Acre.
640	Acres	j	— Mile.

EXAMPLES.

Acres.	rood.	pol.	ft.	in
376	3	3 6	9 3	121
568	,• 1	27	58	76
247	2	3 5	6 1	24

9. OF SOLID MEASURE.

By Solid Measure are measured all things that have length, breadth and thickness.

	TABLE	angungan ing ing panggang terthological panggang ang sa
1728 Inches 27 Feet 40 Feet of round timber or 50 feet of hewn timber 128 Solid feet, i. e. 8 in length, 4 in breadth and 4 in height	make one	Foot. Yard. Ton or load. Cord of wood.

EXAMPLES.

	1.		•••		2.	
Ton.		in	Cord.		76.	172 ~
6 5	ft. 3 7	229	39	् 🖠	1 8 🗀	1021
19	26	1207	: 4	8	56	137
36	1.7	5.4	18	+- · .	72	~ 6 ·5 9
5 7	33 .	6	29		86	1 2 4

10. OF WINE MEASURE.

By Wine-Measure are measured Rum, Brandy, Perry, Cider, Mead, Vinegar and Oil.

		TABLE.		
2	Pints pts.) · (Quart, market	d qt.
4	Quarts	- 1	Gallon,	gal.
10	Gallons	1 1	Anchor of Brandy,	anc.
18	Gallons	1 1	Runlet,	run.
311	Gallons	make one	Half Hogshead.	₹hhd.
42	Gallons .	i 1	Tierce,	tier.
63	Gallons	1	Hogshead,	hhd.
2	Hogsheads		Hogshead, Pipe or Butt,	P. or B.
2	Pipes	} (Tun.	$oldsymbol{T}$

EXAMPLES.

		-	•
Hhd. 3 9	gal. 5 2	ges. 3	pts. 1
16	· 2 7	1	. 0
3 5	12	0	-1
2 9	3 8	2	0

		2.		
T,	hhd.	gal. 5 3	gts.	ple
86	2	5 3	3	1.
3 5	1	36	1	•
17	. 0	29	2	1
			·	
			*	

N. B. A Pint Wine Measure is 287 cubic inches.

11. OF ALE OR BEER MEASURE.

TABLE.

2	Pints	·	Quart,	marked	qts
4	Quarts	i i	Gallon, .		gal.
3	Gallons		Firkin of Ale	e in London,	A. fir
81	Gallons	1	Firkin of Al-	e or Beer.	•
9	Gallons	make one	Firkin of Be	er in London,	B. fir.
2	Firkins '	make one {	Kilderkin,	-	kill.
2	Kilderkins	i	Barrel,	• .	bar.
11	Barrels, or 54 gallons	- 1	Hogshead of	Beer,	hhd.
2	Barrels		Puncheon,	• • •	pun.
3	Barrels, or 2 hogsheads	l i	Butt,		butt.
11	Barrels, or 54 gallons Barrels		Hogshead of Puncheon,	Beer,	hhd. pun.

27 16 0 36 8 0	hhd. 3 2 7 2 8 1 7 3	1. gall. 4 8 5 1 2 4	qts. 2 3 1	B. fir. 2 3 4 5 9 8	2. gal. 6 2	qts. 2 3 1
	27	16	0	3 6	8	0
				_		-

N. B. A Pint Beer Measure, is 351 cubic inches,

12. OF DRY MEASURE.

By Dry Measure are measured all Dry Goods, such as Com, Wheat, Seed, Fruit, Roots, Salt, Coal, &c.

			TABLE.	A STATE OF THE STA	
2	Pints	<u> </u>		Quart, marked	qts.
2	Quarts		•	Pottle,	pot.
2	Pottles			Gallon,	gal.
2	Gallons	[Peck,	pk.
4	Pecks			Bushel,	bush.
	Bushels			Strike,	str.
2	Strikes		make one {	Coom,	co.
2	Cooms			Quarter,	gr.
	Quarters	1		Chaldron,	ch.
41	Quarters			Chaldron in London.	-
5	Quarters			Wey,	wey
	Wevs	j	(Last,	last

EXAMPLES.

1.			2.				
bush.	pk.	qt.	pt.	Ch.	òuch.	_ på,	gts.
27	2	6	1	37	16	3	5
18	8	7	0	2 6	28	3	7
2 0	. 0	· 1	1	18	1 2	1 -	Ŏ
• 0	1	8	0	1 7	25.	3	6

N. B. A gallon, Dry Measure, contains 2684 cubic inches

The following are denominations of things counted by the

- 12 Particular things make 1 Dozen,
- 12 Dozen 1 Gross,

12 Gross or 144 doz. . 1 great Gross.

ALSO,

20 Particular things make 1 Score.

Denominations of Measures not included in the Tables.

- 6 Points make 1 Line,
- 12 Lines . Inch,
- 4 Inches . . Hand, which is the state of Section of Section 1997.
 - 66 Feet, or 4 Poles, a Gunter's Chain,
 - 3 Miles . . League.
- A Hand is used to measure Horses. A Fathom to measure depths.

 A League in reckening distances at Sea.
 - Ni B A Quintal of Fish weighs 1 cwt. Avoirdupois.

35 M 45 65

4 6. COMPOUND SUBTRACTION.

COMPOUND SUBTRACTION teaches to find the difference between any two sums of diverse denominations.

RULE FOR COMPOUND SUBTRACTION.

"Place those numbers under each other, which are of the same denomination, the less being below the greater; begin with the least denomination, and if it exceed the figure over it, borrow as many units as make
one of the next greater; subtract it therefrom; and to the difference
add the upper figure, remembering always to add one to the next superior denomination for that which you borrowed.

Proof.—In the same manner as Simple Subtraction.

1. OF MONEY.

1. Supposing a man to have lent £185 10s. 7d. and to have received again of his money, £93 15s. how much remains due?

			1.	,		2
	£		8.	,	d.	£. s
Lent	18	5	1	0	7	From 3 1 0
Received	9	3	1	5	0	Take 8 5 1 5
_ ; -						***************************************
Due	9	1	1	5	7	
n			•	_		•
Proof	18	5	1.	v	7	

				3.		
	_	2	7		8.	d.
Lent	6	3	7	1	7	8
	(1	6	3	2	5
Received	•		7	8 -	4	
at sundry	₹.		1	9	15	11
times.	•	1	3	9	6	8
1	(3	2	6	1	1	4
	-	_	_			

Vet due

The sum of the several payments must first be added together, and the amount subtracted from the sum lent.

mes.	(32	1 3	3 9 3 1	6 1	8 4	4. From £39 7s. 6d. 1 £7 13s. 11 d. and what will a	emain
ceived n all						.dns. £31 13s.	6 gas

5. A certain man sold a lot of land for £735 11s. 6d: he received at one time £61 5s: at another time, £195 13s. 11d. how much is there yet due?

Ans. £478 12s. 7d.

2. OF TROY WEIGHT.

		1.	,	• • • • •	•	<u>&</u>	
From Take	7 6 ·	8	pwt. 1 6 1 7	grs. 1 3 6	<i>l</i> b. 7 2	ar 3 8	764. 5 9
P amaina			· · · · · · · · · · · · · · · · · · ·				

Proof.

3. OF AVOIRDUPOIS WEIGHT.

,	1.	,			•	2.		
	للبط :					-		
b.	·		T.	· · · capt.	ar.	lb.	œ.	dr
9 1	5	6	6	1 1	ำ	1 4	7	3
9 1	s	7	Ĭ	· 5	Ī	1 6	9	8

4. OF TIME

			1.			
T.	mo.	₩.	d.	h.	m.	
. T. , 3∶9	6	3	6	20	4 4	5 5
4 1 .6	9	ľ	2	1:8	59	5.7
						

5. OF MOTION.

	Į.	
•	•	•
1 6 8	2 7 3 4	3 3 2 3

	z,	
s.	• .	•
6	8	5 1
3	9	5 7
-	-	

6. OF CLOTH MEASURE.

	1.	
Yde.	gr.	n.
27	<i>qr</i> . 1	2
16	1	3

		2.	
E. 2		gr.	a. 1
1	7	3	1.

7. OF LONG MEASURE.

_				•			
Deg.	ànd.	fur.	p.	. જુલોકે '	ſ£.	· W	bar.
Deg. 5 6	1.3	ັ 5	2 6	2	1	. 8	1
17	. 1 5	2	27	1	2	. 9	1

8. OF LAND OR SQUARE MEASURE.

1.			2.			
4.	R.	pol. 1: 7	pol.	ft.	â.	
4. 1 7	1	Î 7	<i>pol.</i> 1-8	fi. 16	1.1	
16	1	1 6	10	201		
					~	

9. OF SOLID MEASURÉ.

1.			2.			
Tons.	ft.	in.	Cords.	ft.	276.	
4 5	ž 9	186	68	23	8 1 0	
19	3 4	1237	6	127	8 1 0 1 5 2 9	

10. OF WINE MEASURE.

Hhd. 6 6	1. <i>gal</i> . 3 1	qte. 2	Tun. 7 5	2. Hhd. 1	gal. 1 6
17	3 3	. 3	.2 4	5, 4 1	4 3
****	19:534 · · +++	****	, 		

11. OF ALE AND BEER MEASURE.

Hhd.	gal.	ges.	Butt.	khd.	eai.
8 9 3 7	gal. 1 9 2 5	2	6 3	1	gai. 1 6
3 7			2 9		10

12. OF DRY MEASURE.

1.			🚅 e e e e e e 🚅				
Bu. 6 1 5	pk. 1 1	91s. 2. 4	<i>Chal.</i> 1 7 1 7 6	šu. 1 8 2 2	pk. 1 2		

SCHOLAR'S ARITHMETIC.

OBSERVATIONS.

2000

The Scholar has now surveyed the ground work of Arithmetic. It has before been intimated that the only way in which numbers can be affected, is by the operations of Addition, Subtraction, Multiplication and Division. These rules have now been taught him, and the exercises in a supplement to each, suggest their use and application to the purposes and concerns of life. Further, the thing needful, and that which distinguishes the Arithmetician, is to know how to proceed by application of these fortrules to the solution of any arithmetical question. To afford the scholar this knowledge is the object of all succeeding rules.

SECTION IL.

RULES ESSENTIALLY NECESSARY FOR EVERY PERSON TO FIT AND QUALIFY THEM FOR THE TRANSACTION OF BUSINESS.

These are ten: Reduction, Fractions,* Federal Money, Exchange, Interest, Compound Multiplication, Compound Division, Single Rule of Three, Double Rule of Three, and Practice.

A thorough knowledge of these rules is sufficient for every ordinary occurrence in life. Short of this a person in any kind of business will be liable to repeated embarrassments. It is the extreme usefulness or these rules which commends them to the attention of every Scholar.

^{*} Fractions are taken up here no further than is necessary to shew their signification and to illustrate the principles of Federal Money.

1. REDUCTION.

" REDUCTION teaches to bring or exchange numbers of one denom-" ination to others of different denominations, retaining the same value."

IT IS OF TWO KINDS.

1. When high denominations are to be brought into lower, as pounds into shillings, pence and farthings; it is then called REDUCTION DESCENDING, and is performed by Multiplication.

2. When lower denominations are to be brought into higher, as farthings into pence, or into pence, shillings and pounds; it is then called REDUCTION AS-

CENDING, and is performed by Division.

REDUCTION DESCENDING.

RULE.

MULTIPLY the highest denomination by that number which it takes of the next less to make one of that greater; so continue to do till you have brought it as low as your question requires.

Proor-" Change the order of the question, and divide your last pro-

duct by the last multiplier, and so on."

EXAMPLES.

1 In £17 13s. 6d. Sqrs. how many farthings?

d. 8. 13

In this example, the highest denom . ination is pounds, the next less, is 2 0 Shillings in a pound. shillings, and because 20 shillings make one pound, therefore, I multiply 3 5 3 Shillings in £17 13s. £17 by 20, increasing the product by 1 2 Pence in a Shilling. the addition of the given shillings

(13) which it must be remembered, 4 2 4 2 Pence in £17 13s. 6d. must always be done in like cases: 4 Farthings in a penny, then because 12 pence make one shilling, I multiply the shillings (353) by

A. 1 6 9 7 1 Farthings. 12, adding in the given pence (6d.) lastly, because 4 farthings make one penny, I multiply the pence (4242) by 4, and add in the given farthings (3qrs.) I then find that in £17 13s. 6d. 3971. there are 16971 farthings.

~				PROOF.				
4)	1	6	9	7	1	3qrs.		
1:	2)	4	2	4	2	6 <i>d</i> .		
	2 0)			5 3		13s.		
		3	E1	7	_			

To prove the above question, change the order of it, and it will stand thus: in 16971 farthings, how many pounds?

Divide the last product by the last multiplier the remainder will be farthings. Proceed in this way till all the steps of the operation have been retraced back; the last quotient with the remainders will be proof of the accuracy of

the operation if they agree with the sum given in the question.

- 2. In £7 14s. 6d. 1qr. how many farthings? Ans. 7417grs.
- 3. In £7 6s. 4d. how many pence? Ans. 1756d.

- 4. In 29 guineas, at 28s. each, 5. In £173 15s. how many six-pen how many farthings? Ans. 38976 grs. ces? Ans. 6950.

- 6. In 12 crowns at 6s. 7d. how many pence and farthings? Ans. 948d. 3792qrs.
- 7. In 671 eagles, at 10 dolls. each, how many shiftings, three-pences, pence, and farthings? Ass. 40200s. 161040 three-pences, 483120 rence, and 1932480grs.

REDUCTION ASCENDING.

RULE.

Divide the lowest denomination given by that number which it takes of the same to make one of the next higher, and so continue to do till you have brought it into the denomination which your question requires.

EXAMPLES.

•

1. In 16971 farthings how many pounds?

Farthings in a penny 4)16971 3qrs.

Pence in a shilling 12)4242 6d.

Shillings in a pound 2|0)35|3 13s.

Reduction descending and ascending reciprocally prove each other.

Ans. £17 13s. 6d. 3qrs.

2. In 1765 pence, now many 3. In 3 guineas?

3. In 38976 farthings how many guineas?

Ans. 29

4. In 6950 sixpences, how many pounds?

Ans. £173 15s.

And reserved A beautiful 1 is

Broke Broke Broke Broken

5. In 3792 farthings, how many crowns?

Ans. 12.

He personal to sever.

- 6. In 48960 farthings, how many nence, three-pences, six-pences and collars?
- 7. In 6952 three-pences, how many pistoles at 22: Ans. 79

Ans. 12240 pence, 4080 three-pences, 2040 six-pences, 170 doll ars.

REDUCTION ASCENDING & DESCENDING.

1. MONEY.

1. In 57 moidores, at 36s. each, how many dollars?

Aus. \$342.

In this question the first step will be to bring the moidores into shillings: lastly bring the shillings into dollars.

2. In 75 pistoles how many pounds 2. Ans. £82 10s.

3. In £73 how many guineas?
Ans. 52 guineas, 4s.

 In £83 and 5 guiness, how many dollars? Am. £233 2c. "When it is required to know how many sorts of win of different value, and of equal number are contained in any number of wother kind; reduce the several sorts of coin into the lowest denomination mentioned, and add them together for a divisor; then reduce the money given into the same denomination for a dividend, and the quotient arising from the division will be the number required."

Note Observe the same direction in weights and measures.

1. In 54 guineas, how many pounds, dollars and shillings of each an aqual number?

OPERATION.
£1 is 20 shillings
1 dollar is 6 shillings
1 shilling is 1 shilling

Divisor 27 shillings

1 dollar is 6 shillings
1 shilling is 28 shillings is a guinea

432

Dividend 1512 shillings.

27)1512(56 of each; that is, 54 guineas include the value of one pound, 135 one dollar, and one stilling 56 times.

162 162

2. In 172 meidores how many eagles, dollars and nine-pences, of each the like number?

Ans. 92 of each, and 68 nine-pences over.

NOR STORE TO PROSE CORP. LEADING STORE OF THE STORE OF TH

3. In 137 guiness how many moidores, pistoles, pounds, and dollars each the like number?

das. 79 of each

TROY WEIGHT.

1. In 415. Sez and 16pasts how many grains?

lb. oz. par. 4 5 13 12 oz. in a pound.

53 ounces.

20 pwts. in an ounce.

1076 penny weights. 24 grains in 1 pwt.

4304 £152

Proof 24)25824 grains, the Ans. 20)1076 16 pwts.

12)53 5 oz.

4lb.

2. In 1015. of silver, how many spoons, each weighing 5os. 10 puts.?

S In 202210 girins of silver, how many pounds !

Ans. 49

4. In 45681 grains of silver, how many pounds?

dusare 7th 11oz. Sprats. 9grs.

5. In 4560 grains of silver, now many tea spoons, each one ounce?

Ans. 94 ica spoons.

3. AVOIRDUPOIS WEIGHT.

Cart. 1 In 67	gr.	13. 13	oz. 11, how many draws?			
269 28			. 1	PROOF. 6)1931696		
2165				16)120731	1102.	
538				28)7545	13%	
7545 16	68 - 03, 83, 95	ig way to	* + 1	4)269 67	1gr.	
45281 7545						
12C731 16						
724386 120731	,					
1931696						

2. In 14048oz. how many hundred weight?

Ans. 7C. Sgrs. 101b.

4. In 17Cist. 1qr. Cl3 of Sugar, how many parcels, each 17f5. ?

Aut. 114 surcels.

4. TIME:

1. Jn 121812 seconds how many hours?

OPERATION.	PROGF.
6 0)12181 2 12 sec.	H. m. 1
	33 <i>5</i> 0 1
6 0)203 0 80m.	60
	2030
Ans. 33h. 50m, 12s.	60 ·
	121812

2. Supposing a man to be 21 years old, how many seconds has he lived, allowing 365 days 6 hours to a year?

Ans. 662709609 seconds.

3. How many minutes from the commencement of the war between America and England, April 19, 1775, to the settlement of a general peace, which took place, January 20, 1783?

Ass. 4079160 manutes.

4. In 413280 minutes how many weeks?

Ans. 41 weeks.

5. LONG MEASURE.

5.	Reduce	16	miles	to	barley	corns.
----	--------	----	-------	----	--------	--------

OPERATION. 16 Miles. 8	PROOF. 3)S041280 12)1013760
128 Furlongs.	3)84480'
40	†11)28160
5120 <i>Rode.</i> 5 <u>1</u> *	2560
2500 2560	4 0)512 0
23160 Yards. 3	8)128
84480 Feet. 12	76, Miles.

1013760 Mehm.

the quotient by 2. The reason is because 51 reduced to half yards is 11.

in A parional los a result

- * To multiply by one half (1/2) it is only to take half the multiplicand.
- 2. In 47520 feet how many leagues?

Answer, 3041280 bar. corns.

Ans. 3 leagues.

3. How many times does the wheel which is 18 feet 6 inches in circumforence, turn round in the distance of 150 miles?

Ans. 42810 times, and 180 inches over

4. How many barley corns will reach round the Globe, it being 380 degrees? Ans. 4755801600.

6. LAND OR SQUARE MEASURE.

1. In 13 acres, 2 roods, how many poles?

PERATION. Ac. R.		PROOF. 4 0)216 0
13 54	13 2 4	4)54
40		13Ac. 2R.

Ans. 2130 Poles.

2. In 2852 rods how many acres?

Ans. 17A. 3R. 12P

1296000 Inches.

7. SOLID MEASURE.

1. In 1296000) sold inches now many tom	Of Mean amost :
OPERATIO	N.	PROOF.
,	5 O .	15
1728)1296000		50
12006		-
	15 Tons, the Answer.	750
8640	10 1010, 200 020,00000	1728
8640		
		6000
		1500
•	•	5250
		750

2. In 5529600 solid inches, how many cords of wood f

Aug. 28.

3. How many solid inches in a cord?

Ans. 221184.

8. DRY MEASURE.

1. In 75 bushels of corn how many pints?

OPERATION.

75

4

300

8

2400

75 Bushels.

2. In 9376 quarts how many bushels?

Ans. 4800 pts.

Ans. 293.

It would be needless to give examples of Reduction in all the weights and measures. The understanding which the attentive Scholar must already have acquired of this rule, by the help of the tables, will ever be sufficient for his purpose.

EUPPLEMENT TO REDUCTION.

QUESTIONS.

- 1. What is Reduction?
- 2. Of how many kinds is Reduction? What are they called? Wherein do these kinds differ one from the other? Which of the fundamental rules are employed in their operation?
- 3. How is Reduction Descending performed?
- 4. How is Reduction Ascending performed?
- 5. When it is required to know how many sorts of coin, weights or measures of different values, of each an equal number, are contained in any other number of another kind, what is the method of procedure?

EXERCISES.

1. In 36 guineas, how many crowns?

Ans. 153 crowns & 9d. over.

2. How many rings, each weighing 5pwts. 7grs. may be made of 3lb. 5oz. 16pwts. 2grs. of gold?

Ans. 158

SECT. II. 1.

3. How many steps of 2 feet 5 inches each, will it require a man to take, travelling from Leominster to Boston, it being 43 miles?

Ans. 93947

4. Let 70 dollars be distributed among three men in such manner that as often as the first has 5s. the second shall have 7s. and the third 9s. What will each one receive?

Ans. first \$16 4s. second \$23 2s. third \$30.

5. How many square seet in a square mile?

Ans. 27878400

6. If a vintner be desirous to draw off a pipe of Canary into bottles, containing pints, quarts, and 2 quarts, of each an equal number, how many must be have.

Ans. 144 of each.

7. There are three fields, one contains 7 acres, another 10 acres, and the other 12 acres and 1 rood: how many shares of 76 perches each, are contained in the whole?

disc. 61 shares and 44 perches over

8. There are 106lb. of silver, the property of 3 men; of which A receives 17lb. 10oz. 19pwts. 19grs. of what remains, B shares 1oz. 7grs. se often as C shares 13pwts. What are the shares of B and C?

Ans. B's share 53lb. 8oz. 5pwts. 5grs. C's share 34lb. 4oz. 15pwts

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§ 2. FRACTIONS.

WHEN the thing or things signified by figures are whole ones, then the figures which signify them are called integers or whole numbers. But when only some parts of a thing are signified by figures, as two thirds of any thing, five sixths, seven tenths, &c. then the figures which signify these parts of a thing being the expression of some quantity less than one, are called FRACTIONS.

Fractions are of two kinds, Vulgar and Decimal; they are distinguished by the manner of representing them; they also differ in their modes of eperation.

VULGAR FRACTIONS.

To understand Vulgar Fractions, the learner must suppose an integer (or the number 1) divided into a number of equal parts; then any number of these parts being taken would make a fraction, which would be represented by two numbers placed one directly over the other with a short line between them thus, \(\frac{1}{4}\) two thirds, \(\frac{1}{4}\) three fifths, \(\frac{1}{4}\) seven eighths, \(\frac{4}{4}\)c.

Each of these figures have a different name and a different signification. The figure below the line is called the denominator, and shews into how many parts an integer, or one individual of any thing is divided—the figure above the line is called the numerator, and shews how many of those parts

are signified by the fraction.

For illustration, suppose a silver plate to be divided into nine equal parts. Now one or more of these parts make a fraction which will be represented by the figure 9 for a denominator placed underneath a short line shewing the plate to be divided into nine equal parts; and supposing two of those parts to be taken for the fraction, then the figure 2 must be placed directly above the 9 and over the line (3) for a numerator, shewing that two of those parts are signified by the fraction, or two ninths of the plate. Now let 5 parts of this plate, which is divided into 9 parts be given to John, his fraction would be 3 three ninths; let 3 other parts be given to Harry, his fraction would be 3 three ninths; there would then be one part of the plate remaining still (5 and 3 are 8) and this fraction would be expressed thus 3 one ninth.

In this way all vulgar fractions are written; the denominator or number below the line, shewing into how many parts any thing is divided, and the numerator, or number above the line, shewing how many of those parts

are taken or signified by the fraction.

To ascertain whether the learner understands what has now been taught him of fractions, let us again suppose a dollar to be cut into 13 equal parts;—let 2 of those parts be given to A; 4 to B; and 7 to C.

Required of the learner that he should write A's fraction —
B's fraction —
C's fraction —

It is from division only that fractions arise in Arithmetical operations: the remainder after division is a portion of the Dividend undivided; and is always the numerator to a fraction of which the Divisor is the Denominator The quotient is so many integers.

The Arithmetic of Vulgar Fractions is tedious and even intricate to beiginners. Besides they are not of necessary use. We shall not therefore into any further consideration of them here. This difficulty arises from the variety of denominators, for when numbers are divided

into different kinds, or parts, they cannot be easily compared. This consideration gave rise to the invention of

DECIMAL FRACTIONS

Decimal Fractions are also expressions of parts of an integer; or are in value something less than one of any thing, whatever it may be which is

signified by them.

In decimals an integer, or the number one, as I foot, I dollar, I year, &c. as conceived to be divided into ten equal parts, (in vulgar fractions, an integer may be divided into any number of parts) and each of these parts is subdivided into ten lesser parts, and so on. In this way the denominator to a decimal fraction in all cases, will be either 10, 100, 1000, or unity (1) with a number of cyphers annexed; and this number of cyphers will always be equal to the number of places in the numerator. Thus, 4 47 444 are Decimal Fractions, of which the cyphers in the denominator of each are equal to the number of places in its own numerator.

" As the denominator of a decimal fraction is always 10, 100, 1000, &c. " the denominators need not be expressed; for the numerator only may be " made to express the true value; for this purpose it is only required to " write the numerator with a point (,) before it, called a separatric, at the " left hand, to distinguish it from a whole number; thus, 16 is written ,6;

* 17 ,27; 155 ,685, &c."

When integers and decimals are expressed together in the same sum, that sum is called a mixed number; thus, 25,63 is a mixed number; 25, or all the figures to the left hand of the separatrix being integers, and ,63 or all the figures to the right hand of the same point being decimals.

The first figure on the right hand of the decimal point signifies tenth parts; the next, hundredth parts; the next, thousandth parts, and so on.

.7 seven signifies seven tenth parts.

seven hundredth parts. ,07

two tenth parts and seven hundredth parts; or twenty seven hundredths.

three tenth parts, five hundredth parts, and seven thousandth parts; or 357 thousandths.

five, and seven tenth parts.

- five and seven thousandths.

The value of each figure from unity, and the decrease of decisads toward the right hand may be seen in the fellowing vanished rul .

TABLE.

XU 9 8 7 6 5 4 3 2 1, 2 3 4 5 6 7 8 9 and 7 and A

Cyphers placed to the right hand of decimals do not after their value. Placed at the left hand they diminish their value in a tenfold proportion.

ADDITION OF DECIMALS.

RULE.

" 1. PLACE the numbers whether mixed or pure detimals, under each other according to the value of their places.'

"2. Find their sum as in whole numbers, and point off so many places " for decimals as are equal to the greatest number of decimal places in any " of the given numbers."

EXAMPLES.

1. What is the amount of 73,612 guineas, 436 guineas, 3,27 gumeas, ,8632 of a guinea, and 100,19 guineas when added together.

> OPERATION. ,8632 100,19

. 345,601....

The decimals are arranged from the separatrix towards the right hand, and the whole numbers from the same point towards the left hand. The greatest number of decimal places in any of the numbers is four, Ans. 613,9352 gaineas. consequently four figures in the product must be pointed off for decimals.

> 3. Required the sum of 37.821+ **546,35+8,4+37,325.**

Ans. 629,596.

572.313

dred twenty-nine and seven tenths; sandths, and four thousandth and thirty-seven and one hundred and three hundredths? sixty-two thousandths; and sixteen Sum 4600,035. hundredths, when added together? - Ans. 367,022.

4. What is the sum of three hun- 5. Add six hundred and five thou-

Note.—When the numerator has not so many places as the denominator has cyphers, prefix so many cyphers at the left hand as will make up the defect; so view is written thus, ,005, &c.

SUBTRACTION OF DECIMALS.

RULE.

" Place the numbers according to their value; then subtract as in whole numbers, and point off the decimals as in Addition."

EXAMPLES.

1. From 716,325 take 81,6201.

2. From 119,1384 take 95,91. Rem. 23,2284.

OPERATION. From 716,325 Take 81,6201

634,7049

3. What is the difference between 287 and 3,115? Ans. 283,885.

4. From 67, take ,92. Rem. 66, 08.

All the operations in Decimal Fractions are extremely easy; the only liability to error will be in placing the numbers and pointing off the deci mals; and here care will always be security against mistakes.

MULTIPLICATION OF DECIMALS.

RULE.

"1. Whether they are mixed numbers or pure decimals, place the factors, and multiply them as in whole numbers."

"2. Point off so many figures from the product as there are decimal places in both the factors; and if there be not so many decimal places in the product, supply the defect by prefixing cyphers."

EXAMPLES.

1. Multiply ,0261 by ,0035. OPERATION.

> ,0261 ,0035

1305 783

In this example, the decimals in the two factors taken together are eight: the product falls short of this number by four figures, consequently, four cyphers are prefixed to the left hand of the product.

.00009135 Product.

2. Multiply 31,72 by 65,3. Product, 2071,316.

3. Multiply 25,238 by 12,17 Product, 307,14646.

OPERATION.

3 1,7 2 6 5,3

4. Multiply ,62 by ,04. Product, ,0248.

5. Multiply 17,6 by ,75 Product, 18,2.

DIVISION OF DECIMALS.

RULE.

"1. The places of decimal parts in the divisor and quotient counted together must be always equal to those in the dividend, therefore divide as in whole numbers, and from the right hand of the quotient, point off so many places for decimals, as the decimal places in the dividend exceed those in the divisor.

"2. If the places of the quotient be not so many as the rule requires,

supply the defect by prefixing cyphers to the left hand.

"3. If at any time there be a remainder, or the decimal places in the divisor be more than those in the dividend, cyphers may be annexed to the dividend or to the remainder, and the quotient carried on to any degree of exactness."

EXAMPLES.

Divide 2,735 by 51,2. OPERATION. 51,2)2,735(,0534+ 2,560

> 1750 1536

> > 2140 2048

> > > 92

In this example there are five decimals in the dividend (counting the two cyphers which were added to the remainder of the dividend after the first division) that the decimals in the divisor and quotient counted together may equal that number, a cypher is pushed to the left hand of the quotient.

In the division of decimals it is proper to add cyphers so long as there continues to be a remainder, this however is not practised, nor is it necessary; four or five decimals being sufficiently accurate for most calculations.

2. Divide 3156,293 by 25,17.

Quotient, 1253+

Norz. The separatrix is omitted in the answers to the examples on this page to exercise the scholar implacing it according to rule; to this the Instructor should be particularly attentive.

3. Divide 5737 by 13,8. Quotient, 431353+

4. Divide 173948 by 375. Quotient, 463861+

5. Divide 2 by 53,1 Quetient, 037+

6. Divide ,012 by ,005. Quotient, 24.

REDUCTION OF DECIMALS.

CASE 1.

TO REDUCE VULGAR FRACTIONS TO DECIMALS.

RULE.

Annex a cypher to the numerator and divide it by the denominator, annexing a cypher continually to the remainder. The quotient will be the decimal required.

EXAMPLES.

1. Reduce 3 to a decimal.

5)3,0(,6 Ans. 3 0

The numerator in these operations is considered as an integer, and always requires the decimal point to be placed immediately as

ter it, the cyphers annexed occupy the places of decimals, the quotient must be pointed off according to the rule in division.

2. Reduce 4 to a decimal

3. Reduce 1, 1, and 2 to decimals. Answers, 25, 5., 75.

4. Reduce 4, 116, and 1188 to decimals. Ans. ,1923+,025,00797+

CASE 2.

To reduce numbers of different denominations, as of Money, Weight and
Measure to their decimal values.

RULE.

"1. Write the given numbers perpendicularly under each other to dividends, proceeding orderly from the least to the greatest.

"II. Opposite to each dividend on the left hand, place such a number " for a divisor as will bring it to the next superior denomination and draw "a line perpendicularly between them.

"III. Begin with the highest and write the quotient of each division, as " decimal parts on the right hand of the dividend next below it, and so on, "!ill they are all used, and the last quotient will be the decimal sought."

EXAMPLES.

1 Reduce 10s. 64d. to the fraction of a pound. . OPERATION.

e 🏂 albeit was en 🦮 aan s

and all and set with

The given numbers arranged for the op-12 6,75 eration, all stand as integers. I then sup-20 10,5625 pose 2 cyphers annexed to the 3(3,00) which divided by 4, the quotient is 75, which

which divided by 4, the quotient is 75, which 1,528125 Ans. I write against six in the next line, and the sum thus produced (6,75) I divide by 12, placing the quotient, (5625) at the right Land of the 10; lastly, I divide by 20 and the quotient (,528125) is the decimal required.

Company and the second

who was the define one of the Born of the section of a

2. Reduce 13s. 51d. to the decimal of a pound. Ans. ,6729+ decimal of an ounce. Ans. ,6291.

Wight the of the Agriculture

CASE 3

To find the value of any given decimal in the terms of an integer. melanore A content of the owner RULE. The content of the content o

engager and all of the energy Multiply the decimal by that number which it takes of the next less denomination to make one of that denomination in which the decimal is given, and cut off; so many figures for a remainder to the right hand of the quotient, as there are places in the given decimal. Proceed in the same manner with the remainder, and continue to do so through all the parts of the integer, and the several denominations standing on the left hand make the answer.

EXAMPLES.

1. What is the value of ,528125 of a pound?

	OPERATION.			M.		
	,5	2	8	1	2	
					×	<u> </u>
Shilling #4	0,5	6	2	5	0	0
					1	2
Pence	6,7	5	0	0	0	0
*						4
Farthings Ans.	3,0	0	0	0	0	0

This question is the first example in the preceding case inverted, by which it will be seen that questions in these two cases may reciprocally prove each other.

The given decimal being the decimal of a pound, and shillings being the next less inferior denomination, because 20 shillings make one pound. I multiply the decimal by 20, and cutting off from the right hand of the product a number of figures, for a remainder equal to the number of

figures in the given decimal, leaves 10 on the left hand which are shillings. I then multiply the remainder, which is the decimal of a shilling by 12, and cutting off as before, gives 6 on the left hand for pence; lastly, I multiply this last remainder, or decimal of a penny by 4, and find it to be 3 farthings, without any remainder. It then appears that ,528125 of a pound is in value 10s. 64d.

2. What is the value of ,73968 of a pound?

Ans. 14s. 9jd.

What is the value of ,768 of a pound Troy?
 Ans. Son. Apast. 711*grs.

* 17 is the last remainder, 680 reduced to its lowest terms. A fraction is said to be reduced to its lowest terms, when there is no number which will divide both the numerator and denominator without a remainder.—Thus, set to the fraction its proper denominator 1995, then divide the numerator and the denominator by any number which will divide them both, without a remainder, continue to do so as long as any number can be found that will divide them in that manner.

8) 1888 == 155 == 17.

SUPPLEMENT TO FRACTIONS.

QUESTIONS.

- 1. What are fractions?
- 2. What are integers or whole numbers?
- 3. What are mixed numbers?
- 4. Of how many kinds are fractions?
- 5. How are Vulgar Fractions written?
- 6. What is signified by the denominator of a fraction?
- 7. What is signified by the numerator?
- 8. How are Decimal Fractions written?
- 9. How do Decimals differ from Vulgar Fractions?
- 10. How can it be ascertained what the denominator to a Decimal Fraction is if it be not expressed?
- 11. How do cyphers placed at the left hand of a Decimal Fraction affect its value?
- 12. How are Decimals distinguished from whole numbers?
- 13. In the addition of Decimals what is the rule for pointing off?
- 14. What is the rule of pointing off Decimals in Subtraction? In Multi-A substitute of the effects of the tiplication? and in Division?
- 15. In what manner is the reduction of a Vulgar Fraction to a decimal performed?
- 16. How are numbers of different denominations, as pounds, shillings, peace, &c. reduced to their decimal values?
- 17. If it be required to find the value of any given decimal in the terms of an integer, what is the method of procedure?

"EXERCISES.

1. What is the sum of 791 61 and of # when added together. OPERATION.

79.5 6,25

,75

86.50 Ans.

2. From 17 take #. OPERATION.

. 16,25 Remainder.

In Case 1. Ex. 3d, under Reduc- tion of decimal fractions, the Scholar may notice that 1, 1 and 7 reduced to decimals are, ,25, ,5 and ,75. When numbers, therefore, for operations in either of the fundamental Rules, are incumbered with these fractions 1, 7, 3, substitute for them 3. Multiply 681 by 51. operation.

6 8, 2 5 5, 5

34125

3 7 5, 3 7 5 Product.

their equivalent decimal fractions, that is, for \$\frac{1}{4}\$,25 for \$\frac{1}{4}\$,5 for \$\frac{3}{4}\$,75 then proceed according to the rules already given for these respective operations in decimal fractions.

4. Divide 261 by 21.

OPERATION.
2,5)26,25(10,5 Quotient.
25

125 125

Many persons are perplexed by occurrences of a similar nature to the examples above. Hence is seen in some measure the usefulness of fractions, particularly decimal fractions. The only thing necessary to reader any person adroit in these operations is to have riveted in his mind the rules for pointing as taught and explained in their proper places. They are not burthensome; every scholar should have them perfectly committed.

5. If a pile of wood be 18 feet long, 111 wide, and 72 high, how many cords does it contain?

Ans. 12 cards, 68 feet, 432 inches. and 4 in height.

A cord of wood is 128 solid feet; the proportions commonly assigned are, 8 feet in length, 4 in breadth, and 4 in height.

The contents of a load or pile of wood of any dimensions may be found by multiplying the length by the breadth, and this product by the height; or, by multiplying the length, breadth and height into each other. The last product divided by 128 will shew the number of cords the remainder, if any, will be so many solid feet.

^{*} The 432 inches is the fraction, ,25 of a foot, valued according to Case 3, Reduction Decimal Fractions.

6: If a load of wood be 9 feet long, 3½ feet wide, and 4 feet high, how many square feet does it contain?

Ans. 126 feet, which are two feet short of a cord.

7. What is the value of ,725 of a day?

Ans. 17 hrs. 24 min.

8. What is the value of ,0625 of a shilling?

Ane. 3 farthings.

alue of ,0625 of a 9. Reduce 3Cmt. Ogrs. 7lb. 8oz.

Ans. 3 farthings. to the decimal of a ton.

Ans. ,15334821+

10. Reduce 3 farthings to the decimal of a shilling * Ans. ,0625.

11 Reduce of to a decimal fraction. And 0125.

3. FEDERAL MONEY.

FEDERAL MOREY is the coin of the United States, established by Congress, A. D. 1786. Of all coins this is the most simple, and the operations in it the most easy.

The denominations are in a decimal proportion, as exhibited in the fol-TABLE.

lowing

10 Mills make one Dollar, marked thus, \$ 10 Cents 10 Dimes 10 Dollars

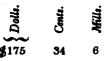
The expression of any sum in Federal Money is simply the expression of a mixed number in decimal fractions. A dollar is the Unit Money; dollars therefore must occupy the place of units, the less denominations, as dimes, cents, and mills, are decimal parts of a dollar, and may be distinguished from dollars in the same way as any other decimals by a comma or separatrix. All the figures to the left hand of dollars, or beyond units place are eagles. Thus, 17 eagles, 5 dollars, 3 dimes, 4 certs, and 6 mills are written-

Of these, four are real coins, and one is imaginary. The real coins are the Eagle, a gold coin; the Dollar and the Dime, silver coins; and the Cent, a copper coin. The Mill is only imaginary, there being no piece of money of that denomination.

There are half eagles, half dollars, double dimes,

balf dimes, and half cents, real coins.

These denominations, or different pieces of money, being in a tenfold proportion, consequently my sum in Federal Money does of itself exhibit the particular number of each different piece of money contained in it. Thus, 175,346 (seventeen eagles, five dollars, three dimes, four cents, six mills) contain 175346 mills, 17534 6 cents, 1753 46 dimes, 175 346 dolls. 17 tests eagles. Therefore, eagles and dollars reckoned together, express the number of dollars contained in the sum; the same of dimes and cents; and this indeed is the usual way of account, to reckon the whole sum in dollars, cents, and mills, thus:



The Addition, Subtraction, Multiplication and Division of Federal Money is performed in all respects as in Decimal Fractions, to which the Scholar is referred for the use of rules in these operations.

ADDITION OF FEDERAL MONEY.

1. Add 16 Eagles; 3 Eagles, 7 Dollars 5 Cents; 26 Dollars, 6 Dimes, 4 Cents, 3 Mills; 75 Cents, 8 Mills, 40 Dollars, 9 Cents together.

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2. If I am indebted 59 dollars, 112 dollars, 98 cents, 113 dolls. 15 cts. 15 dollars, 21 dollars, 50 cents, 200 dollars, 73 dollars, 35 dollars, 17 cents, 75 dollars, 20 dollars, 40 dollars, 33 cents and 16 dollars. What is the sum which I owe? Ans. \$781 13.

AMERICAN & LAND

All the second s

4 0, 0 9

\$2 6 4, 5 4 1

Or the sums may be all reckoned in dollars, cents and mills, thus,

Cents.

DETERMINE OF FROSER MONTH.

t trymps by he is af wheat cost front, how much is it fer that!!

Which the divider Obstant of district of the colors of the

Accountants generally with the comma, and distinguish cents from dollars oy setting them apart from the dollars.

14000 1361**0**

SUBTRACTION OF FEDERAL MONEY.

1. From \$8832 prinks \$69, 82.

9:20 Fröm \$684 takie \$57,63, 2 :sn one Rimainder, \$623,876 r. 23 :20 C. 20,1 \$... \$623,876 r. 23

8 6 3, 1 7 6 9, 8 2

fiemainder, 7 9 3, 3 5

MULTIPLICATION OF FEDERAL MONEY.

1. If flour be \$10.25 per barrel, what will 27 barrels cost?

1 0, 2 5 2 7 7 1 7 5 2 0 5 0 \$2 7 6, 7 5 Ans.

2. Multiply \$76,35 by \$37,46. Product, \$260,0710. Point off the decimals in the product according to the rule in Multiplication of decimals; if at any time there shall be more than three decimal figures, all beyond mills or the third place, will be decimal parts of a mill.

3. Multiply \$24,675 by \$13,63.

Product, \$336,32074.

Ranksking All on very keep one of

DIVISION OF FEDERAL MONEY.

1 If 2728 bushels of wheat cost \$2951, how much is it per bushel?

Bushels. Dolls. D. d. c. m. 2798)\$961(1, 0 8 5 Ans. 2728

with the rest time to the time comment.

When the dividend consists of dollars only, if there be a remainder after division, cyphere must be annexed as in division of decimals.

23300 21824

> 14760 13640

278**1420** - 32 279 573 565 245 575 537 537 756 equally among - - 24 5 **2. Divide \$1**

2. Divide \$2756 equally among 13 mong what will each man receive?

Ans. \$288,923.

Quotient, 62 cents

3 & £

1000 1 15 1 1 3 3 3 3 3 3

SUPPLEMENT TO FEDERAL MONEY.

QUESTIONS.

- 2. What is FEDERAL MONEY? When was its establishment, and by what authority?
- 2. What are the denominations in Federal Money?
- 3. Which is the Unit Money?
- 4. How are dollars distinguished from dimes, cents, and mills?
- 5. What places do the different denominations occupy, from the decimal point?
- Solution of Federal Money performed? Subtraction? Multiplication? Division?

EXERCISES.

1. A man dies, leaving an estate 2. A man sells 1225 bushele of of \$71600, there are demands against wheat at \$1,33 per bushel, and rethe estate of \$39876,74; the residue ceives \$93,76 for transportation: is to be divided between 7 sons; what does he receive in the whole? what will each one receive? Ans. \$4531 89cts.

المكافرين الأراب والمراكب المراوي ومراوا فقراطهم

Francisco de la compansión de la compans

Ane. \$1723,01.

3. What will 3 hogsheads of sugar 4. Divide seven thousand six dol-

Pleasing to fail to begin the top our and in House of the control of the second section of the secti

4.44.* 1 3

Electrical Established to the Company of

Francisco Company

Alta Alianda de Caractería de

A Section Control

tost, each weighing 3Cart. 2grs. 7lb. lars, one cent and three mills, by at 18cts. 7mills per lb. five hundred seventy six dollars, thirty four cents and two mills. Ans. \$12,155

. .

1100

N HY OR A PAMA EXCHANGE AREA AND S

Exchange is the giving of the bills, money, weight, or measure of one place or country, for the like value in the bills, money, weight or measure of another place or country.

Note 1. The Currencies in the New England States, and in Virginia, are the same and will be all comprehended under the term M. E. currency ; those of New York, North Carolina and Ohio, are the same, and will be comprehended under the term W. Fork Currency; those of N. Jersey, Pennsylvania, Delaware and Maryland, are the same, and will all be comprehended under the twin Penn. Currency.

Norg. 2. It will be sufficient perhaps in most cases, that the pupil be required 40 work this rule in the currency of that State only to which he belongs.

CASE 1.

To change New England Acc and New-York, Sc. Currencies to Federal Money. RULE.

1314919575 Set down the pounds, and to the right hand write half the greatest even number of the given shillings: then consider how many farthings there are bontained in the given period and farthings, and A the sum exceed 12, increase it by 1, or if it exceed 88, increase it by 2, which sum set down to the right hand of half the greatest even number of shillings before written; remembering to increase the second place; or the place next to shillings by by if the shiftings be an odd number; to the whole saw that produced, annex a cypher, and divide the sum by 3, if It be Mi England currency, and by 4 if it be New-York; cut off the three right hand figures in the quotient, which will be cents and mills; the rest will be dollars.

EXAMPLES.

1. Change £47 7s. 103d. to dollars, cents and mills.

In this example to the right hand of pounds (47) I write 3, half the greatest even number with the feather a might the given shillings (7); the furthings in 101d.

of this specific and the second place increased by a be-The pounds.
Half the even number of The farthings in pence ings increased according Cypher annexed. erolino de cause the shillings were an odd number, make 95, which sum written to the right hand of the 3, a cypher annexed, and the sum divided by 3 gives the answer 157 dollars, 98 cents, and 3 mills for N. England currency; the same sum (473950) divided by 4, gives 118 dollars, 48 cents, 7 mills for N. York currency.

Divide by 3) 4 7 3 9 5 0

Dolls. 1 5 7,9 8 3

If there be no shillings, or only 1 shilling in the giren sum, so there be no even number, write a cypher in place of half the even number of shillings, then proceed with the pence and farthings as in other cases.

If pounds only are given to be changed, annex a cypher and divide as before, the quotient will be dollars. If there be a remainder, annex 3 more cyphers and divide, the quotient will be cents and mills.

If rounds and an even number of shillings only be given, to the pounds annex half the even number of shillings, divide as before, and the quotient will be dollars

A little practice will make these operations extremely easy.

2. In £763 N. E. and N. Y. currencies, how many dollars, cents, and dollars, cents and mills?

Ans. \$2543 33cts. 3m. N. E. cur. 1907 50 N. Y. —

Comment of the contract of Asserted to the second of the second then I have been the 3. In £17 1s. 61d. how many Ans. \$56 92 3. N. E. cur. 42 69 2. N.Y. 🕿

dollars and cents?

saved not with a growing of the work of a green med wated to a domination of the contract of

6. Exchange £1 1. 101d. to 7 Exchange £10 41d. to Fede Federal Money.

16 Mb. C. Max. \$3,646 N. E. cur. 2786 W.IV. Fas N. N. 1 11 61

4. In £109 3s. 8d. how many 5. In £86 6s. 51d. how many dollars and cents?

Ans. \$363,94 N. E. cur.

272,95 N. Y. — 215,805 N. Y. —

30 July 1883

as a transmitter of the form of a first something the transmitter of

ral Money.

The second of the self-one of the second care

Ass. \$33:596 N. E. car. 1 1 10:00 25,047 N. V. 1 10:00 10:00 1 10:00 25,047 N. V. 1 10:00 10:00 - 17. 0 5 771

8. Exchange £103 to Federal Money.

Ans. \$343,333 N. E. cur.

5. Exchange 684 delians to pouch and shilmers. Ass. £200 46 N. E. eur.

273 12 . V. V. cur.

9. Exchange 23d. to Federal Money.

Ans. 3cts. 6m. N. E. cur 2- 7- N. Y. -

4. Fy hange 134 dollars 65 cents en per u te stiffinge, pance and far

Post 200 12 1996 N. B. Mr. 23 27 24 A. V. 24th

CASE 2.

To Exchange Federal Money to New-England and New-York Currencies. RULE.

If there be no mills in the given sum, reduce it to mills by annexing cyphers; multiply the given sum by 3, if it be required to change it to N. E. currency; but if to the currency of N. York, by 4; cut off the four right hand figures, which will be decimals of a pound, the left hand figures will be the pounds. To find the value of the decimals, double the first figure for the call the figures in the legislation of third places, after deducting then call the figures in the legislation of third places, after deducting the figures in the legislation of the call the call the figures in the legislation of the call the ca in the second places so many farthings, abating when the gre above and 2, when they are above \$6. S Sp A. F. Car

EXAMPLES.

1. Change 255 dollars, 40 cents, 6 mills, to pounds, shillings, pence and Arthines.

OPERATION.	OPERATION.
2 5 5 4 0 6	255406
7 6 6 2 1 3	1 0 2 1 6 2 4

Ans. £76 12s. 5d. £102 3s. 3d. Having multiplied and cut off the four right hand figures as the rule directs, to find the value of the figures cut off, I double the first figure (6) N. E cur. which

N. E. cur. N. Y. cur. gives 12 for shillings; the figures in the second and third places (21) abating 1 for being over twelve (20) are to be considered so many farthings, which reduced to pence are 5. The 3s. 3d. N. Y. cur. are obtained after the same manner. The dou-

ble of the first figure cut off (1) is 2, and because the figure in the second place (6) is more than 5, I add mother shilling, making 3s. then the figures in the second and third places (62) after deducting the 5 for 1 shilling from the 6, are 12, which reduced to pence are 3.

The 8 and the 4 in the fourth places, being something less than one far-

ching, are lost, not being reckoned.

If there be neither cents nor mills, that is, if the given sum be dollars, mul tiply by 3 and cut off one figure only.

2. In \$392,75 how many pounds, shillings, pence and farthings?

Ans. £117 16s. 6d. N. E. cur. 157 2 0 N.Y. -

3. In \$39,635 how many pounds, shillings, peoce, &c. ?

Ans. £11 17s. 91d. N. E. cur. 15 17 1 N. Y. cur.

4. Exchange 134 dollars 65 cents to pounds, shillings, pence and farthings.

Ans. £40 7s. 103d. N. E. cur. 53 17 21 N.Y. cur.

5. Exchange 684 dollars to pounds and shillings.

Same and the men we consider the

Control of a warmer of the west 1981. The transfer of the transfer

Ans. £205 4s. N. E. cur. 273 12 N. Y. cur.

6. Exchange 71 cents to shillings,

Aus. 4s. 3d. N. E. cur. 5 81 N. Y. cur.

and the state of t 7. Exchange 13cts. Jan. to pence which is a first send farthings, a source additionance Ann 94d. N. Ec out.

13d M.V. cur o

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CASE 3.

To change New-Jersey, Pennsylvania, Delaware and Maryland Currency to Federal Money.

RULE.

Reduce the given sum to pence, annex a cypher, divide these pence by 9, and add the quotient to the pence; from the sum point off three figures. which will be cents and mills; those to the left hand will be dollars.

If there are farthings in the given sum, in place of the cypher annex 2 for

1 farthing; 5 for 2 farthings; 7 for 3 farthings, and proceed as before.

If the given sum be pounds only, multiply by 8, annex 3 cyphers to the product, and divide by 3; the quotient will be the answer, pointing of the three right hand figures for cents and mills.

EXAMPLES.

1 Change £17 1s. 61d. to Federal Money.

I first reduce the given sum to pence, to which (4098) I annex the figure 5 for the 1d. and divide by 9; the quotient added to the pence and the three right had figures pointed off give the answer, 45 dollars, 53 cents and 8 mills

9)40985

Ans. 45,538

- * This quotient figure (3) might with propriety have been put down 4, the 2's in 36 coming so near producing it, and it would have been nearer the true value; the mills in the answer would then have been 2 in place of 8.
- 2. In £109 5s. 8sl. how many dol- 3. Change £736 to Federal Money. lars; cents and mills?

 Ans. £1962,666. Ane. \$291,155.

dollars, cents and mills? Ans. \$230,191.

Purchase of the Control of the Contr

1.00 mg 1 1 1 1 1 2 2 1 1 1 1 2 1

4. In £86 6s. 51d. how many 6. Change 61d. te Federal Money An 7cts. 4 mills.

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三部 實制 混造 一級

CASE 4.

To change Federal Maney to New-Jersey, Pennsylvania, Delaware and Mary-land Currency.

RULE.

If there be no mills in the given sum, reduce it to mills by annexing cyphers, subtract one tenth of itself, the remainder, except the right hald figure, will be peuce, which must be reduced to pounds; to find the value of the right hand figure, if it be 2, reckon 1 farthing; If 5, reckon it 3 farthings.

Note.—Subtracting the tenth of the gives sum from itself, may, be done in this monner:—Suppose the sum 6452. Write the given sum under uself, removing 6 4 5 2 the figures one place towards the right hand and dropping the fight hand 6 4 5 figure; whereas and the remainder will be the sum required.

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EXAMPLES! Of high at 7.2 agnost) i

1. Change \$45,538 to pounds, shiftings, pence and farthings.

OPERATION.

This is the first example in the former Case in the first example in the former Case that the note above, the right hand figure in the relation of the mainder (5) being to be reckaged 2 farthings, I set it down in the answer 1d.—the other figures of the remainder (4098) being pence, I divide by 12, in doing which there is a remainder of 6.

Ans. £17 1s. 61d. by 12, in doing which there is a remainder of o, which are pence; these I also set down in the answer. The shillings (3.1) divided by 20 cutting of one figure around the divisor and one from the divided as is naught prosting the divided as shillings to pounds, give £17, and the I cut of from the divided is a shilling, which completes the answer.

- 2. Change \$135 to pounds, &c.
 Ans. £50 12s. 6d.
- 3. Change \$287,74 to pounds
 Ans. £107 18s. 01d.

4. In £56 & 61 but many & Change Sp. & to Februs Money Politars, cents and mills? Anti-Joseph P. (125 4 101) & Anti-Joseph P. (125 4 101) &

To change the New-England to the New-York currency; add one third. To change the New-York to the New-England currency; subtract one fortething from And

To change the New-England to the Pennsylvania currency; add one fourth. To change the Pennsylvania to the New-England currency; subtract one fiften in the land and a second of

The change the New York to the Pennsylvania currency; subtract one sixteenth.

LAgickange the Renneskoania to the New-York currency? said one fifteenth.

1. Lot on Price one acceptingly **TO BUT SUPPLEMENT TO EXCHANGE**

randomination of the three QUESTIONS.

m bas 210 1 A w w ne -on -: conservat to the section of 1. What is Exchange?

: 2 How do you change N: England and Virginia currencies to Federal Money ?-New-York currency? and wherein consists the difference?

Service of the servic

- 3. If pounds only are given to be changed, how do you proceed? "given sum, how do you proceed?
- 4. When there are no shillings, high only Jens in the given sum; " " only, how do you proceed?" how do you proceed?
- N. York currency ?-Wherein consists the difference?
- Money to N. England currency?

- 2. How do you change Pennsylvania. &c. currency to Federal Money ?
- 3. If there are farthings in the
- 4. If the given sum be pounds
- . f. How do you change Federal How do you change Federal Money to Pennsylvania, &c. currency?
- 6. How do you change New-England to New-York currency ?-New - York to New-England -- New-England to Pennsylvania ?- Pennsylvania to New England !- New York to Pennsylvania !- Pennsylvania to New-

York surrency! at some sail seconds of the propose to be of the Commence of the second second by New Proposed marrency

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CASE 4.

To change Federal Money to New-Jersey, Pennsylvania, Delaware and Mary-land Currency.

RULE.

If there be no mills in the given sum, reduce it to mills by anaexing cyphers, subtract one tenth of itself, the remainder, except the right hand figure, will be peuce, which must be reduced to pounds; to find the vaffic of the right hand figure, if it be 2, reckon 1 farthing; if 5, reckon it 2 farthings.

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5807

EXAMPLES! Of his at 7.2 again) 1

1. Change \$45,538 to pounds, shillings, pence and farthings.

OPERATION.

This is the first example in the former Case inverted. Having subtracted one tenth of the given sum from itself in the manner directed in the note above, the right hand figure in the remainder (5) being to be reckoned 2 farthings, I set it down in the answer \$\frac{1}{4}\$.—the other figures of the remainder (4098) being pence, I divide by 12, in doing which there is a remainder of 6, which are pence; these I also set down in the

answer. The shillings (341) divided by 20 conting of one figure from the divisor and one from the dividend as is navelly practized in seducing shillings to pounds, give £17, and the 1 cut off from the dividend is 1; shilling, which completes the answer.

- 2. Change \$135 to pounds, &c.
 Ans. £50 12s. 6d.
- 3. Change \$287,74 to pounds
 Ans. £107 18s. 01d.

4. In £56 62. 64.1 hove money in Change Cot to Federal Money deltam, cents and onlike?
And collection of the Court of the To change the New-England to the New-York currency; add one third.

To change the New-York to the New-England currency; subtract one fourth are more lived

To change the New-England to the Pennsylvania currency; add one fourth. To change the Pennsylvania to the New-England currency; subtract one fiften et til vid vid de en er e

To change the New York to the Pennsylvania currency; subtract one sixteenth.

To change the Rangelpania to the New-York currency? and one fifteenth.

A Lite of the more from the second of the second **SEE O SUPPLEMENT TO EXCHANGE**

was and the or so to have QUESTIONS.

2. How do you change Peansylvania. &c. currency to Fede-

But the state of the state of the state of . governor by many and 1. What is Eichange ?

2 How do you change N. England and Virginia currencies to Federal Money ?-New-York cur-

But the market and a second

- ral Money ? rency !- and wherein consists the difference?
- 3. If there are farthings in the 3. If pounds only are given to be changed, how do you proceed? given sum, how do you proceed? 4. When there are no shillings, 4. If the given sum be pounds is only how in the given sum; " " only, how do you proceed? how do you proceed?
- How slow ground change. Federal ... 15. How ide. you change: Federal Money to Pennsylvania, &c Money to N. England currency? N. York currency ?-Wherein currency? consists the difference?
- 6. How do you change New-England to New-York currency ?-New - York to New-England -- New-England to Pennsylvania ?- Pennsylvania to New-England ?- New-York to Pennsylvania ?- Pennsylvania to New-

York surrency! all some with a profession and a section e and the true of the forest entrency

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TABLE

FOR REDUCING THE CURRENCIES OF THE SEVERAL UNITED STATES TO FEDERAL MONEY.

; ÷	ana gyman.	N. Hamp.	New-York	N. Jersey, Pennsylva'a	S. Carolina.
15 CM 2 1 1		Rh. Island. Conn. and Virginia.	and N. Carolina.	Delaware, and Maryland,	and Georgia.
Farthings.	1 2 3	D. cts. m., 3, 7, 10, 14	D. cts. in. , 3 , 5 , 8	D. cts. m.	D. cts. m. 4 9 , 14 . 18
	2 3 4	, 28 , 42 , 56 , 69	, 21 , 31 , 42 , 52	, 22 , 33 , 44 , 56	, 36 , 54 , 71 , 89
Pence.	6 7 8 	, 83 , 97 ,111 , 125 ,133	, 62 , 73 , 82 , 94 ,104	, 67 78, 89,	,107 ,125 ,143 ,161
	11 1 2 3	,153 ,167 ,333 ,500	,104 ,114 ,125 ,250 ,375	,111 ,122 ,133 ,267 ,400	,179 ,196 ,214 ,429 ,643
· Section of the control of the cont	4 5 27 48 6 4 0.24	,666 ,833 3,000	,500 ,625 ,780 ,780	,533 ,667 7437 390 53	,857 1,071 (3): 3):386
Shillings.	8 9 1 0 11	1,333 1,500 1,667 1,838 2,000	1,000 1,125 1,250 1,375 1,500	1,067 1,200 1,833 1,467 1,600	1,714 1,929 2,143 2,357 2,571
•	13 14 15 16	2,167 2,333 2,500 2,667	1,625 1,750 1,875 2,000	1,733 1,867 2,000 2,133	2,785 3,000 3,214 2,428
,	17 18 19	2,839 3,000 3,167	2,125 2,250 2,375	2,267 2,400 2,533	3,643 3,857 4,071
,	17		$(C_{i},C_{i},C_{i},C_{i})$		

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TABLE FOR REDUCING THE CURRENCIES, &c. CONTINUED.

College A	New-Hamp.	New-York,	New-Jersey, &c.	S. Carolina, &c.
	£. D. c. m.	D. c. m.	D. c. 10.	D. c
	3,333	2,5	2,666	4,286
	6,667	5,0	5,333	8,571
į	10,000	7,5	8,000	12,357
	13,333	10,0	19,667	17,143
	16,667	12,5	13,333	21,429
	\$0,000	15,0	16,000	25,714
	23,333	17,5	12,667	30,000
	26,667	20,0	21,333	34,286
	30,000	22,5	24.000	38,571
. 10	33,333	25,0	20,667	×42,857
´ , 2 (50,0	53,333	85,714
, S		75,0	80,090	128,571
. 40		100,0	106,667	171,429
, "		125,0	133,383	211,286
64	200,000	150,	160,000	\$57,143
. 70		175.	186,667	3 (H),000
81		200,	213,333	342,857
90	300,000	225,	240,000	38 5,714
100		250.	266,667	488,571
200	666,667	500	533,355	847,113
300	1000,000	750.	800,020	1295,714
400	1333,333	1000,	1066,667	1744,286
500		1250	1337,383	2142,857
600	2000,000	1500 ₄ c	1600,000	2571,429
700	2333,333	1750.	1866,667	3000,000
800		2000,	2133,398	3428,571
900	3000,000	2250,	2400,000	3857,143
100		2500,	2666,667	4285,714

TABLE

FOR REDUCING FEDERAL MONEY TO THE CURRENCIES OF THE SEVERAL UNITED STATES.

	New-Hamp. &c. &c. poll. 6s.	New-York, &c. Doll. 8s.	N. Jersey, &c. &c. poll. 7s. 6d.	S. Carolina,
D. etz.	£. s. d. y.	£. s. d. q.	£. s. d. q.	£. s. d. q.
, ;;,01	3	1 10	1.00	ેં તે હતું છું
,02	19	2.0	1.3%	D-10
.63	2.1	3 0	2 (3)	e 1 3
,04	3.0	3.3	3 (2)	95.1
,05	3,2	4.3.	4 (2).33	ુ જુ 3
,06	41	5.3	5 311	8 1
07	5.0	6.3	6:1::	4-54-0
.08	5.3	7.3	741:0	5.42.2
	6.2.12		8 200	HREND
,10	1 77	9 2	90'	5.8

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TABLE
FOR REDUCING THE CURRENCIES, &c. CONTINUED.

	New-Hamp.	New-York, &c.	New-Jersey, &c.	S. Carolina, &c.
Doll. cts. ,20 ,30 ,40 ,50 ,60 ,70 ,80 ,90 11 22 3 4 4 5 6 7 8 9 10 20 30 40 50 60 70 80 90 100 200 300 400 500	£. s. d. q. 1 2 2 1 9 2 2 4 3 3 0 0 3 7 1 4 2 2 4 9 2 5 4 3 6 0 0 12 0 0 1 10 0 0 1 16 0 0 2 2 0 0 2 8 0 0 2 14 0 0 3 0 0 0 6 9 12 15 18 21 24 27 30 60 90 120 150	£. s. d. q. 1 7 1 2 4 3 3 2 2 4 0 0 4 9 2 5 7 1 6 4 3 7 2 2 8 0 0 1 4 0 0 1 12 0 0 2 8 0 0 2 16 0 0 3 12 0 0 4 0 0 0 8 12 16 20 24 28 32 36 40 80 120 200 200 200 200 200 200 200 200 20	£. i. d. q. 1 6 0 2 3 0 3 0 0 3 9 0 4 6 0 0 6 9 0 7 6 0 1 10 0 0 1 17 6 0 2 12 6 0 3 15 0 7 10 0 11 5 0 18 15 0 21 0 0 18 15 0 33 15 0 37 10 0 112 10 0 115 0 0 112 10 0 115 10 0 115 10 0	£ s. d. q. 11 1 1 4 3 1 10 2 2 4 0 3 3 1 3 8 3 4 2 2 4 0 0 1 18 8 0 1 12 8 0 1 12 8 0 1 17 4 0 2 6 8 0 1 17 4 0 2 6 8 0 1 13 4 7 0 6 8 11 13 4 7 0 6 8 11 13 4 7 0 6 8 11 13 4 7 0 6 8 11 13 4 7 0 0 8 11 13 4 7 0 0 8 11 13 4 11 0 0 0 16 6 8 18 13 4 7 0 0 0 9 3 6 8 11 13 4 11 0 0 0 11 13 4 11 0 0 0 11 13 4 11 0 0 0 11 13 4
700 800	180 210 240	240 280 320	285 0°0 262 10°0 300°0 0	146 U 0 163 6 8 186 13 4
900 1000 2000	270 300 600	560 400 800	337 10 0 375 0 0 -	210 0 0 238 6 8 466 13 4
3000 4000 5000 6000	900 1200 1500 1800	1200 1600 2000	1126 / 1500 / 1875 /	760 0 0 935 6 8 1166 13 4 1466 0 0
8000 9000	2100 2400 2700 3000	2800 3200 3600	2625 3000 (3375	1633 6 8 1866 13 4 2100 0 0

. 6 5. SIMPLE INTEREST

INTEREST is the allowance given for the use of money, by the borrower to the lender. It is computed at so many dollars for each hundred lent for a year, (per annum) and a like proportion for a greater or less time. The highest rate is limited by our laws to 6 per cent,* that is 6 dollars for a hundred dollars, 6 cents for a hundred cents, £6 for a £100, &c. This is called legal interest, and is always understood when no other rate is mentioned.

There are three things to be noticed in Interest.

- 1. The PRINCIPAL; or meney lent.
- 2. The RATE; or sum per cent. agreed on.
- 3. The Amount; or principal and interest added together.
 Interest is of two sorts, Simple and Compound.
- 1. Simple Interest is that which is allowed for the principal only.
- 2. Compound Interest is that which arises from the interest being added to the principal, and (continuing in the hands of the lender) becomes a part of the principal at the end of each stated time of payment.

GENERAL RULE.

- 1. For one year, multiply the principal by the rate, from the product cut off the two right hand figures of the dollars, which will be cents, those to the left hand will be dollars; or, which is the same thing, remove the separatrix from its natural place two figures towards the left hand, then all those figures to the left hand will be dollars, and those to the right hand will be cents, mills, and parts of a mill.
- In the same way is calculated the interest on any sum of money in pounds, shillings, pence and farthings, with this difference only, that the two figures cut off to the right hand of pounds, must be reduced to the lowest denomination, each time cutting off as at first.

2. For two or more years, multiply the interest of one year by the number of years.

3. For months, take proportional raliquot parts of the interest for one year, that is, for 0 months, $\frac{1}{4}$; for 4 months, $\frac{1}{4}$; for 3 months, $\frac{1}{4}$, 3c.

For daws, the proportional or aliquot parts of the interest for one month, allow — ys to a month.

EXAMPLES.

1. What is the interest of \$36,446 for one year, at 6 per cent?

Dolls. cts. mills.

86 44 6 principal. 6 rate.

5 18 67 6 interest.

In the product of the principal multiplied by the rate is found the answer.

Thus cutting off the two right hand figures from the dollars leave five on the left hand which is dollars; the two figures cut off (18) are cents, the

. z

next figure (6) is mills; all the figures which may chance to be at the right band of mills, are parts of a mill; hence we collect the Ans. \$5 18cts. 675 m

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(i) a grant per tro referenced et al., and all properties of a second expension of the properties.

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2. What is the interest of \$365 14cts: 6mills, for three years 7 months and 6 days?

6 months 1)2 1 9 0, 8 7 6 interest for T year, touched edit of restored and the second second

Because 7 months are not an even part of a year, take two such numbers as are even pasts, and which added together will linke TO and 1) 6 months are 1 of a year, therefore for 6 months, divide the interest of one year by 2; again 1 month is 1 of 6 months, therefore, for 1 month is 1 of 6 months, therefore, for 1 month or of 30 days, therefore for 6 days, divide the interest of 1 month by 5. Lastly add the interest of all the parts of the time together, the sum is the answer.

3. What is the interest of Evi 7s. 6fd. 4. What is the interest of for 1 year at 8 per cent? 16s. 8d. for I year and or interest of the intere

there figures to the left had not be closed and points it is at 2 to a will be cents, note, and parts of a not.

th the scan ray is established the extension of any such to such the first time of the first time to the first time to the first time of the such that the suffer of the first time the such that the first time cannot be first cash to the such time cannot of the first cannot be first can

2. For two or mark many man, dy the superstanting the ber of years.

3. The result of the space of the state of t

Four that he for a mention I, not a now the first a new or the for dament in the graves of the four control of the four contro

> Dollé eta milia. 36 - ak 18 policificak

> > . 44 6 7

A 18 67 6 Septem

the control of the second of the state of the control of the contr

Wdien the rate is at 6 per cent, there is not perhaps a mora concine and easy way of custing interest, entany sum of money in Bellum, Cents, and Man, thus by the following

METHOD.

Write down half the greatest even number of months for a multiplier; at there be an odd month it must be reckoned 30 days, for which and the given days, if any, seek how many times you can have six in the sum of them, place the figure for a decimal at the right hand of half the even number of months, already found, by which multiply the principal; observing in pointing off the product to remove the decimal point or separatrix two figures from its natural place towards the left hand, that is, point off two more places for decimals in the product, than there are decimal places in the multiplicand and multiplier counted together; then all the figures to the left hand of the point will be dollars, and those to the right hand, dimes, cents and mills, &c. which will be the interest required.

Should those be a tempital armid laking end a inthrof the days, teduce it to a wulgar frattion, for which take aliquot parts of the multiplicand. The

1, 4, 64	"If the remai	nder be 1	, divide	the	Mul	iplic	and	by 6	
9 - 4	Tribe remain	' しゅ ' ' 2 当4	ļ,	-			-	by 3	
	Francisco Crisco	ال ينيز (1 2) الم	ļ	-				by 2	
	If * 11	14 14 July					-	by 3 twice	
1.1	A indicatorial	NIT - 1	and 1.	•			•	by 2 and 3	j.
	THE TOWN OF STREET		, amu 3,	•			•	<i>by ~ and 0</i>	•

The quotients which in this way occur, must be added to the product of the principal multiplied by half the months, &c. the sum thus produced will be the interest required.

When there are days, but a less number than 6, so that 6 cannot be contained in them, put a cypher in place of the decimal at the right hand of the months, then proceed in all respects as above directed.

Note. In casting interest, each month is reckoned 30 days.

EXAMPLES.

1 What is the interest of \$76,54 for 1 year, 7 months and 11 days? OPERATION.

76,54 to terraine ad 22 Trace it's

The number of months being 19, the greatest 9 5 9 2 4 tained in 41, (the sum of the flays in the order of month and given days). I find it will be 6 times.

3 8 2 7 which I set down at the right hand of helicity. I design of the faithy by liet colony appropriate the intercent at a eyen number of months for a decimal by which 6 2 one sixth of the days (41) there will be a ge-mainder of 5 i and i for which I take, first one half the multiplicand, that is, divide the multiplicand by 2, then by 3, and these quotients added, with the products of half the even number of months, &c. the sum of them will

shew the interest required, observing to count off two more figures for decimals in the product than there are decimal figures in both the multiplier and multiplicand counted together.

For the conciseness and simplicity of the above method it is conceived that instructors will recommend it to their pupils in preference to any other.

- 2. What is the interest of \$5,93 for 2 years and 8 months ?
 - Ans. 94cts. 8m.
- 3. What is the interest of \$67,62 for 3 years and 2 months? Ans. §12 64cts. 7m.

- cents for 27 years?
- When the interest on any sum is required for a great number of years it will be easier first to find the interest for 1 year, then multiply the interest so found by the number of years.
- 5. What is the interest-of \$2870,32 for 10 days ! Ane. \$4 78cts 3m. Contract of the contract and the contract of the

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When the rate is any other than 6 per cent, first find the interest at 6 ser ceut, then divide the interest so found by such parts as the interest at the rate required exceeds or falls short of the interest at 6 por cent, and the quotient added to or subtracted from the interest at 6 per cent, as the case may be, will give the interest at the rate required.

Programme Commence To the

6. What is the interest of \$137, 84
7. What is the interest of \$79,07
for 2 years and 6 months, at 5 per for 10 months at 8 per cent?
cent?
Ass. \$17,23.

· Complete the second of the control of the second between the second se

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- 8. What is the interest of \$2,29 for 1 month 19 days at 3 per cent? Ans. 9 mills.
- 9. What is the interest of \$18 for 2 years 14 days, at 7 per cent! Ans. \$2 56cts. 9m.
- 10. What is the interest of \$1600 for 1 year and 3 months?

Ans. \$120.

- 11. What is the interest of \$5,811 for 1 year and 11 months? Ans. 66cts. 8m.
- 12. What is the interest of \$17,63 for 11 months and 28 days? Ans. \$1,054.

13. What is the interest of \$861,12 for 9 months 25 days, at 7 per cent? Ans. \$49,394.

- 14. What is the interest of \$105 ,61 for 1 year 7 months and 6 days? Ans \$10 13cts. 8m.
- 15. What is the interest of \$86 for 9 months? Ans. \$3,87.
- 16. What is the interest of \$78,36 for 5 years 10 months and 3 days?

17. What is the interest of \$812 30 cents for 2 years 8 months and Ans. \$27 46cts. 5m. 4 days? Ans. \$130,509. To this mode of computing interest, I would add from the "Massachusetts

Justice" a

METHOD

Of computing the interest due upon Bonds, Notes, &c. when partial payments may at different times be made, as established by the Courts of Law in Massachusetts.

RULE.

Cast the interest up to the first payment, and if the payment exceed the interest, deduct the excess from the principal, and cast the interest upon the remainder to the time of the second payment. If the payment be less than the interest, place it by itself, and cast on the interest to the time of the next payment, and so on until the payments exceed the interest, then deduct the excess from the principal and proceed as before.

EXAMPLES.

Suppose A should have a bond against B for 1166 dollars 66 cents and 6 mills, dated May 1, 1796, upon which the following paymerts should be made, viz

• •	Dolls. Mills.	Months. Days.
1. December 25, 1796	- 166,666	7 24
2. July 10, 1797	- 16,666	6 15
3. September 1, 1798	- 50,000	13 21
4. June 14, 1799	- 333,333	9 13
5. April 15, 1800	- 620,000	10 1
What will be due upon it August 3, 180	1?	15 18
•		Ans. \$237,76.

To facilitate the operation, let the space of time from the date of the Bond to the day of the first payment, and from the time of one payment to that of another, and from that of the last payment to the time of settlement, be first computed and set down against the day of payment as above. -- Then set down the sum on which the interest is to be cast, with the interest and payments in columns thus.

	Principal.	Ti	me.	Interest.	Payments.	Excess.	
	Dolls. Mills.		. Da.	Dolls. M.	Dolls. M.	Dolls. M.	1
	1166,666 121,167	7	24	45,499	166,666	121,167	32 °
2	1045,499	6	15	33,973	16,666		
3	1045,499	13	21	71,616	50,000		
4	1045,499	9	13	49,312	333,333		
. ,	245,093			154,906	399,999	245,093	
-5	900,406 579,847	10	1	40,153	620,000	579,847	+:
	220,559	15	18	17,203		·	
	The k				220,559		ŗ
	Intere	st fro	m the	17,203	and the second s	:	
	Sem d	ue At	igust S	3, 1801	237,762		

2. Supposing a note of 867 dollars 33 cents, dated January 6, 1794, upon which the following payments should be made, viz.

1. April 16, 1797 \$136,44cts.
2. April 16, 1799 319,
3. Jan. 1, 1800 518,68

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What would be due July 11, 1301? Ans. \$215,108

SUPPLEMENT TO SIMPLE INTEREST.

QUESTIONS.

- 1. What is Interest?
- 2. What is understood by 6 per cent? 3 per cent? 8 per cent, &c
- 3. What per cent per annum is allowed by law to the lender for the use of his money?
- 4. What is understood by the principal? the rate? the amount?
- 5. Of how many kinds is interest? in what does the difference consist
- 6. How is simple interest calculated for one year in Federal Money?
- 7. For more years than one, how is the interest found?
- 8. When there are months and days, what is the method of procedure ?
- 9. What other method is there of casting interest on sums in Federa. Money?
- 10. When the days are a less number than 6, so that 6 cannot be contained in them, what is to be done?
- 11. How is simple interest cast in pounds, shillings, pence and farthings:
- 12. When partial payments are made at different times, how is the interest calculated?

EXERCISES.

1. What is the interest of \$916,72 for 1 year and 4 months ? 1976 - 1.00 Atts:/848/937:

11 364 Joh

22 What is the interest of \$93. 17eth for 14 days ? FEW 3-

No transfer to the second

Ans. 17 cents.

Sure a training to the body at the se 3. What is the interest of \$5,19 4. What is the midrest of \$1.07 for 7 months?

Ans. 18cts. 1m for 3 years: 6 cicins and 15 ays? fr: 22cts 7m.

- 5. What is the interest of two bundred dollars and six cents, 4 days?

 Ans. 13cts. 3m.
- 6. What is the interest of nine cents 45 years 7 months and 11 days?

 Ans. 24cts. 6m.

- 7. What is the interest of half a mill 567 years? Ans. 1ct. 7m.
- 8 A's note of \$365,37 was given Dec 3, 1797; June 7, 1800 he paid \$97,16; what was there due Sept. 11, 1800? Ans. \$328,32.

- 9. B's note of \$175 was given Dec. 6, 1798, on which was endorsed one year's interest: what was there due Jan. 1, 1803?

 Ans. \$207,22.
- 10. C's note of \$56,75 was given June 6, 1801, on interest after 90 days; what was there due Feb. 9, 1802?

- dollars and seventeen cents was given Oct. 5, 1808, on interest after 3 months; Jan. 5, 1809, he paid fifty dollars; what was there due May 2d, 1811?

 Ans. §174, 53.
- 12. E's note of eight hundred seventy dollars and five cents, was given Nov. 17, 1300 on interest after 90 days; Feb. 11, 1805 he paid one hundred eighty six dollars and six cents; what was there due Dec. 23, 1807?

 Ans. \$1045, 34.

13. What is the interest of £41 11s. 34d. for a year and 2 months?

Aps. £2 18s. 21d.

14. What is the interest of \$273,51, at 7 per cent for / year and 10 days ?

Ans. \$19,677.

15. Supposing a note of \$317,92, dated July 5, 1797, on which were the following payments—Sept. 13, 1799, \$206,04; March 10, 1800, \$76, what was the sum due Jan. 1, 1801?

Ans. \$83,991.

COMPOUND INTEREST

Is calculated by adding the Interest to the principal at the end of each year, and taking the amount the principal for the succeeding year; then the given principal subtracted from the last amount, the remainder will be the compound interest.

A concise and easy method of casting Compound Interest, at 6 per cent on any sum in Federal Money.

RULE.

Multiply the given sum, if	•
'For 2 years by 112,36	For 7 years by 150,3630
3 years — 119,1016	8 years — 159,3848
4 years 126,2476	9 years — 168,9478
5 years — 133,8225	10 years — 179,0847
6 years — 141,8519	11 years — 189,8298

Note 1. Three of the first highest decimals in the above numbers will be sufficiently accurate for most operations; the product remembering to remove the separatrix two figures from its natural place towards the left hand, will then shew the amount of principal and compound interest for the given number of years. Subtract the principal from the amount and it will shew the compound interest.

2. When there are months and days; first find the amount of principal and compound interest for the years, agreeable to the foregoing method, then for the months and days cast the simple interest on the amount thus found; this added to the windows will ghout the waste has a some a gain and the statement of the

3. Any sum of filoney at Compound Threfiest, will double itself in 44 years 10 months and 22 days.

EXAMPLES.

1. What is the compound interest of \$56 -5 for 11 years?

2. What is the amount of \$233 at compound interest for 4 years, 7 months and six days?

	OPERATION.							OPERATION.						•						
			5 6, 7 5 1 8 9, 8 2 9								2 6		6, 2		7 3					
		_	4	5	14	3	5 0		5		2		7	8	7 7 .9	4	2	_	8	·
		5 6	4	0		6				· {	3 2	9	7,	9		4 6	3	3	6	Amount for 4 yrs.
1	0 5	7, 6,	7	2 5	7 p:	9 in	5 cip	7 al	5 Amount. subtracted.	8	7 9	8	7 8	6 3	6 2	4				

^{§ 5 0, 9 7} compound interest. §1 0, 7 2 5 9 8 4 interest for 7 mo. 6 days. 2 9 7, 9 4 4 amount for 4 years added.

^{48 0} B, 6.6 h

6. COMPOUND MULTIPLICATION.

COMPOUND MULTIPLICATION is when the Multiplicand consists of several denominations. It is particularly useful in finding the value of Goods.

The different denominations in what was formerly called Laxful Money, render this rule with some others in Arithmetic, as Compound Division and Practice, rules of great usefulness, quite tedious, and the variety of cases necessarily introduced, extremely burthensome to the memory.—This lumber of the mind might be almost wholly dispensed with, were the habit of reckoning in Federal Money generally adopted throughout the United States.

For important feasons, pounds, skillings, pence and farthings, ought to fall wholly into disuse: "Federal Money is our national currency; the scholar might encompass the most useful rules in Arithmetic in half the time; the value of commodities bought and sold, might be cast with half the trouble, and with much less liability to errors, were all the calculations in money universally made in Dollars, Cents, and Mills. But this, to be practised, must be taught; it must be taught in our schools, and so long as the prices of goods, and almost every man's accounts are in Lounds, Shillings, Pence and Furthings, this mode of reckoning must not be felt untaught.

To comprise the greater usefulness, and also to shew the great advantage which is gained by reckoning in Federal Money, I have contrasted the two modes of account, and in separate columns on the same page, have put

the same questions in Old Lawful and in Federal Money.

OPERATIONS.

IN POUNDS, SHILLINGS, PENCE, FARTH.

CASE I.

When the quantity does not exceed 12 yards, pounds, &c. set down the price of one yard or pound, and place the quantity underneath the lowest denomination for a multiplier. Begin by multiplying the lowest denomination, and carry by the same rules from one denomination to another, as in Compound Addition.

EXAMPLES.

1. What will 7 yards of cloth cost at 9s. 5d. per yard.

£. s. i blue miles.

O 9. 5 price of 1 yard.

7 yards.

Ans. 3 8 11 price of 7 yards.

I say 7 times 5 is 35 pence=2s. 11d.
I set down 1 haid earry 2, saying 7 times 9 is 63, and 2 I carry are 65s.

£3 5s. which I set down.

· / IF DOEQUES, CENTS, MILLS.

IN ALL CASES.

Multiply the price and the quantity together, according to the rules of multiplication in Decimal Fractions, and the product will be the answer. That is,

Multiply as in Simple Multiplication, and from the product point off so many places for cents, and mills, as there are places of cents and mills

in the price.

EXAMPLES.

1. What will 7 yards of cloth cost ut \$1,57 (equal to 9s. 3d.) per yard?

CPERATION.

D. cts. As there are

1. 47 paics, two decimal

7 quantity, places in the
price, so I

Ans. 10 99 price of make two in 1 yards, the product.

PRIVIL BELLING, PERSE, FARTE.

2. What will I possis of segar ' case as 31st pers h. '

DOLLARS, CEFTS, MILLS.

2. What will 9 pounds of sugar cent at \$0, 430 per lb. ! Aus. \$1,251

2. What will 5 week of clock cost e fi its be per rad! 下ひずに

3. What will 6 years of cloth cost at \$5,07 per yard'! **be. \$30,42.**

CASE 2

When the quantity exceeds 12, and u any number within the Multiplication Table, muitiply by two such numbers as when multiplied together, will

produce the given quantity.

If two numbers will not do this exactly, multiply by two such numbers as come the nearest to it, and by the deficiency or excess multiply the multiplicand, and this product added to or subtracted from the first product as the case may require, gives the answer.

EXAMPLES.

1. What will 42 yards of cloth cost at 15s. 9d. per yard?

OPERATION. £. s. d.

0 15 9 price of 1 yd.

Multiplied by

4 14 8 price of 8 yds.

Multiplied by

Ans. 33 1 6 price of 42 yds. Because 6 times 7 is 42, I multiply the price of 1 yard by 6, and this product by 7. as the rule directs.

4. What will 42 yards of cloth cos at \$2,625 per yard ?

OPERATION.

D. cts. 62

25 105 00 0

Ans. 110

POUNDS, SHILLINGS, PENCE, FARTH.

2. What will 125 yards of cloth cost at 5s. 7d. per yard?

Ans. £34 17s. 11d.

DOLLARS, CENTS, MILLS.

5. What will 125 yards of cloth cost at 93 cents per yard?

Jane. \$116,25.

3. What will 51 pounds of tea cost at 3s. 6d. per lb.?

Ans. £8 18s. 6d

1. 2 to n + 2 to

6. What will 51 pounds of tea cest at \$0,563 per lb. ?

Ans. \$29,733.

4. What will 130 yards of cloth cost at £2 3c. 9d. per yard?

.ans. £284 7c. 6d.

7. What will 130 yards of cloth cost at \$7,25 per yard?
.des. \$943,50.

CASE 3.

When the multiplier, that is, the quantity, exceeds 144, multiply first by 10, and this product again by 10, which will give the price of 100 yards, &c. and if the quantity be even hundreds, multiply the price of 100 by the number of hundreds in the question, and the product will be the answer; if there be odd numbers, multiply the price of 10 by the number of tens, and the price of unity, or 1, by the number of units, then these several products added together will be the answer.

TABLE
FOR REDUCING THE CURRENCIES, &c. CONTINUED.

	New-Hamp. &c. &c.	New-York, &c.	New-Jersey,	S. Carolina, &c.
Doll, cts.	£. s. d. q.	£. s. d. q.	£. s. d. q.	£. s. d. q.
,20	122	171	160	1 4 11 1
,30	192	243	230	2 1 4 3
,40	243	3 2 2	300	1 10 2
,50	300	4 0 0	390	2 4 0
,60	371	492	460	292
,70	422	571	530	
,80	492	6 4 3	600	, 383
,90	543 600	722	6 9 0 7 6 0	1 , 4 2 2
	12 0 0	800	7 6 0 15 0 0	4 8 0
. 3	18 0 0	1 4 0 0	1 2 6 0	93 14 0 7
4	1 4 0 0	1 12 0 0	1 10 0 0	18 8 0
5	1 10 0 0	2 0 0 0	1 17 6 0	1 3 4 0
···ě	1 16 0 0	2 8 0 0	2 5 0 0	1 8 0 0
7	2 200	2 16 0 0	2 12 6 0	1 12 8 0
8	2 800	8 400	3 000	1 17 4 0
9	2 14 0 0	3 12 0 0	3 7 6	2 2 0 0
10	3 000	4 000	3 15 0	2 6 8 0
20	8	8	7 10 0	4 13 4
30	9	12	11 50	7 0 0
40	12	16	15 0 0	1 3.0 8
5 0	15	20	18 15 0	11 13 4
60	18	24	22 10 0	1400
70 80	21 24	28	26 5 0	16 6 8
90	27	32 36	30 0 0	18 13 4
100	30	40	33 15 0 37 10 0	21 0 0
200	60	80	37 10 0 75 0 0	23 6 8 46 13 4
300	90	120	112 10 0	70 0 0
400	120	160	150 g 0 0 a	75 93 116: 38 74
500	150	200	187 10 0	116 13 4
: 600	-180 -25-27-54	240 mm	220 0.0	140 U 30"
700	210	280	262 10 0	163 6 8
800	240	320	300``0 0	186 13 4
900	270	560	337 10 0	210_0_0
1000	300	400	375 0 0	233 6 8
2000	600	800	750	466 13 4 .
3000	900	The state of the s	1126	790 0 0
4000 5000	1200 ° 1500		1500	933 6 8
_ : : :	1800 4		and the second	1166.13 4
	2100			1400 0 0
	2400			1633 6 8
1	2700	· · · · · · · · · · · · · · · · · · ·	3000	1866 13 4 2100 0 0
	9000	11111 F		2833 6 8
	$\widetilde{\mathfrak{o}}$			

• § 5. SIMPLE INTEREST

INTEREST is the allowance given for the use of money, by the borrower to the lender. It is computed at so many dollars for each hundred lent for a year, (per annum) and a like proportion for a greater or less time. The highest rate is limited by our laws to 6 per cent, that is 6 dollars for a hundred dollars, 6 cents for a hundred cents, £6 for a £100, &c. This is called legal interest, and is always understood when no other rate is mentioned.

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- GENERAL RULE.

 1. For one year, multiply the principal by the rate, from the product cut off the two right hand figures of the dollars, which will be cents, those to the left hand will be dollars; or, which is the same thing, remove the separatrix from its natural place two figures towards the left hand, then all those figures to the left hand will be dollars, and those to the right hand will be cents, mills, and parts of a mill.
- In the same way is calculated the interest on any sum of money in pounds, shillings, pence and farthings, with this difference only, that the two figures cut off to the right hand of pounds, must be reduced is the lowest denomination, each time cutting off as at first.

2. For two or more years, multiply the interest of one year by the num-

ber of years.

3. For months, take proportional r aliquot parts of the interest for one year, that is, for 0 months, $\frac{1}{4}$; for 4 months, $\frac{1}{4}$; for 3 months, $\frac{1}{4}$, 3c.

For daw, the proportional or aliquot parts of the interest for one month, allow — ys to a month.

EXAMPLES.

1. What is the interest of \$36,446 for one year, at 6 per cent? OPERATION.

Dolls. cts. mills.

86 44 6 principal. 6 rate.

5 18 67 6 interest.

In the product of the principal multiplied by the rate is found the answer.

Thus cutting off the two right hand figures from the dollars leave five on the left hand which is dollars; the two figures cut off (18) are cents, the

next figure (6) is mills; all the figures which may chance to be at the right band of mills, are parts of a mill; hence we collect the Ans. \$5 18cts. 6756m

[.] In New-York the law allows 7 per ceut.

Then set down the sum on which the interest is to be cast, with the interest and payments in columns thus.

	Principal.	Ti	me.	Interest.	Payments.	Excess.	
	Dolls. Mills.	Mo	. Da.	Dolls. M.	Dolls. M.	Dolls. M.	ŀ.
1	1166,666	7	24	45,499	166,666	121,167	· .
••	121,167				1	·	
2	1045,499	6	15	33,973	16,666		
3	1045,499	13	21	71,616	50,000		
4	1045,499	9	13	49,312	333,333		ì
	2 45,093			154,906	399,999	245,093	
5	900,406	10	1	40,153	620,000	579,847	:
	579,847					a y St.	
	220,559	15	18	17,203			
	The la	ast re	mainde	er ·	220,559	in the second	•
	Intere	st fro	m the	last payment	17,203	Ş	

Scm due August 3, 1801

237,762

2. Supposing a note of 867 dollars 33 cents, dated January 6, 1794, upon which the following payments should be made, viz.

\$136,44cts. 1. April 16, 1797 April 16, 1799
 Jan. 1, 1800 319,

What would be due July 11, 1801?

518,68 Ans. \$215,105 Allow British Control of the Control

> and the highest attendance with the Committee of the first the committee of Commence of the state of the st wall to the training the same and the same of

September 1 to 1 to 1

SUPPLEMENT TO SIMPLE INTEREST.

QUESTIONS.

- 1. What is Interest?
- 2. What is understood by 6 per cent? 3 per cent? 8 per cent, &c
- 3. What per cent per annum is allowed by law to the lender for the use of his money?
- 4. What is understood by the principal? the rate? the amount?
- 5. Of how many kinds is interest? in what does the difference consist
- 6. How is simple interest calculated for one year in Federal Money?
- 7. For more years than one, how is the interest found?
- 8. When there are months and days, what is the method of procedure?
- 9. What other method is there of casting interest on sums in Federa. Money?
- 10. When the days are a less number than 6, so that 6 cannot be contained in them, what is to be done?
- 11. How is simple interest cast in pounds, shillings, pence and farthings:
- 12. When partial payments are made at different times, how is the interest calculated?

EXERCISES.

1. What is the interest of \$916,12 for 1 year and 4 months ? 1 Pro 2 2011 Albay \$48 937: 6

BAR. PAR 1

2. What is the interest of \$93. 1760 Phr 44 days 1 :-PEW 3- 1 CO

2. 10 3 . . .

Ans. 17 cents.

to the transfer to the think at the law 3. What is the interest of \$5,19 for 7 months? Ans. 18cts. 1m

4. What is the interest of \$1.07. for 3 years: 6 chains and 15 ays? . fr. 22cts im.

- 5. What is the interest of two bundred dollars and six cents, 4 days?

 Ans. 13cts. 3m.
- 6. What is the interest of nine cents 45 years 7 months and 11 days?

 Ans. 24cts. 6m.

- 7. What is the interest of half a mill 567 years? Ans. 1ct. 7m.
- 8 A's note of \$365,37 was given Dec 3, 1797; June 7, 1800 he paid \$97,16; what was there due Sept. 11, 1800? Ass. \$328,32.

- 9. B's note of \$175 was given Dec. 6, 1798, on which was endorsed one year's interest: what was there due Jan. 1, 1803?

 Ans. \$207,22.
- June 6, 1801, on interest after 90 days; what was there due Feb. 9, 1802?

 days 558-19.

- 11. D's note of two hundred three dollars and seventeen cents was given Oct. 5, 1808, on interest after 3 months; Jan. 5, 1809, he paid fifty dollars; what was there due May 2d, 1811?

 Ans. \$174, 53.
- 12. E's note of eight hundred seventy dollars and five cents, was given Nov. 17, 1300 on interest after 90 days; Feb. 11, 1805 he paid one hundred eighty six dollars and six cents; what was there due Dec. 23, 1807?

 Ans. \$1045, 34.

13. What is the interest of £41 11s. 3\d. for a year and 2 months?

the Marchael Commence of

Age. £2 18s. 21d.

14. What is the interest of \$273,51, at 7 per cent for I year and 10 days?

Ans. \$49,677.

15. Supposing a note of \$317,92, dated July 5, 1797, on which were the following payments—Sept. 13, 1799, \$208,04; March 10, 1800, \$76, what was the sum due Jan. 1, 1801?

Ans. \$83,991.

7.0

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,20	122	171	160.	ا اللا ب
,30	192	2 4 3 3 2 2	230 300	9 1 4 3
,40	243	3 2 2 4 0 0		1 10 2
,50 ,60	371	492	390	2 4 0
,70	422	571	530	3 3 3 1
,80	492	6 4 3	600	, 200
,90	5 4 3	7 2 2	690	3 4 9 9
1,00	600	800	760	4 80
2	12 0 0	16 0 0	15 0 0	1 121 9 4 3
. 3	1800	1 400	1 260	14 0 3
4	1 4 0 0	1 12 0 0	1 10 0 0	18 8 0
5	1 10 0 0	2 000	1 17 6 0	1 3 4 0
6	1 16 0 0	2 8 0 0	2 5 0 0	1 8 0 0
7	2 200	2 16 0 0	2 12 6 0	1 12 8 0
8	2 8 0 0	8 400	3 000	1 17 4 0
9	2 14 0 0	3 12 0 0	3 7 6	2 2 0 0
10	3 000	4 000	3 15 0	2,680
20	6	8	7 10 0	4 13 4
30 40	9	12	11 5 0	7 0 0 9 6 8
50	13 / · · · · · · · · · · · · · · · · · ·	16	15 0 0	9 6 8
60	18	20 24	18 15 0	11 13 4
70	21	28	22 10 0 26 5 0	14 0 0 16 6 8
80	24	32	30 0 0	1 773.5
90	27	36	33 15 0	18 13 4 21 0 0
100	30	40	37 10 0	23 6 8
200	60	80	7500	46.13 4
300	90	120	112 10 0	70 0 0
400	120	160	150 0 0	2,93 1 6; 1814
500	150	200	187 10 0	116 13 4
	180	240	220 0.0	140 0 0
700	210	280	262 10 0	163 6 8
800	240	320	300 0	186 13 4
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1000	300	400	375 0 0	233 6 8
2000	600	800	750	466 13 4
3000	900	1	1126	700 0 0
4000	1200 °		1500	933 6 8
5000 6000	1500		1875	1166-13 4
6000 7000	1800		2250	1466 0 0
8000	2100 2400	[2625	1633 6 8
9000		7	3000 ·	1866 13 4
10000			1	2100 0 0
	10000	TUUU 1.	37 <i>5</i> 0	2833 6 8

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[.] In New-York the law allows 7 per cent.

Divide £297 2s. 3d. among 4 men, 6 boys, and give each man 3 times so much as one boy; what will each man share, and each boy?

OPERATION. d. £. s. d. 3 - (16 10 1 The men have triple shares, therefore mul-18)297 2 tiply the number of men 18 (4) by 3, and add the number of boys, (6) 117 10 2=1 man's share. for a divisor. 108 PROOF. £49 10 men. bous. 9 4 & 6 20 3)182(10 198 1 O men's share 12 18 6 2 and . 16 10 1 2 18 the number of 12 equal shares in 99 0 O boys' share. the whole .= Divisor.)27(1 () added 18 £297 2 The Life Court of the Street Street

10. Divide £39 12s. 5a. among 4 men, 5 women, and 9 boys; give each man double to a woman, each woman double to a hoy.

£. s. d.
1 1 5 a boy's share.
2 2 10 a woman's share.
4 5 8 a man's share.

Annie der begehen al Perference Communication of the small fix Membership of the small

§ 8. SINGLE RULE OF THREE.

THE Single Rule of Three, sometimes called the Rule of Paorontion is known by having three terms given to find the fourth.

It is of two kinds, Direct and Indirect, or Inverse.

SINGLE RULE OF THREE DIRECT.

The Single Rule of Three Direct teaches, by having three numbers given to find a fourth, which shall bear the same proportion to the third that the second does to the first.

It is evident, that the value, weight and measure of any commodity is preportionate to its quantity, that the amount of work, or consumption is preportionate to the time; that gain, less and interest, when the time is fixed, is proportionate to the capital sum from which it arises; and that the effect produced by any cause is proportioned to the extent of that cause.

These are cases in direct proportion, and all others may be known to be so, when the number cought increases or diminishes along with the term

from which it is derived. Therefore,

If more require more, or less require less, the question is always known

to belong to the Rule of Three Direct.

More requiring more, is which this third term is greater than the first, and requires the fourth term to be greater than the second.

Less requiring fees, is when the third term is less than the first and requires the fourth term to be less than the second.

RULE.

"1. State the question by making that number which sake the question, "the third term, or putting it in the third place; that which is of the same name or quality as the demand, the first term, and that which is of "the same name or quality with the answer required, the second term."

"2. Multiply the second and third terms together, divide by the first, and the quotient will be the answer to the question, which (as also the remainder) will be in the same denomination in which you left the second term, and may be brought into any other denomination required."

The chief difficulty that occurs in the Rule of Three, is the right placing of the numbers, or stating of the question; this being accomplished, there

is nothing to day but to multiply and divide; and the work is done.

To this end the nature of every question must be considered, and the circumstances on which the proportion depends, observed, and common sense will direct this if the terms of the question be understood.

.The mathed of proof is by inverting the order of the question.

Note 1. If the first and third terms, both or either, be of different denominations, both terms must be reduced to the lowest denomination men-

tioned in wither, before stating the question.

2. If the second term consists of different denominations, it must be reduced to the lewest denomination, the fourth term or answer will then be found in the same denomination, and must be reduced back again to the highest denomination possible.

3. After division if there be any remainder, and the auctient be not in the lowest denomination, it must be reduced to the next less denomination, dividing as before. So continue to do till it is brought to the lowest de-

nomination, or till nothing remains.

4. In every question there is a supposition and a demand; the current is implied in the two first terms of the statement, the demand

5. When any of the terms are given in Federal Money the operation is conducted in all respects as in simple numbers, observing only to place the point or separatrix between dollars and cents, to point off the results according to what has been taught already in Decimal Fractions, Federal

Money, and further illustrated in Compound Division.

When any number of barrels, bales, or other packages, or pieces are given, if they be of equal contents, find the contents of one barrel or piece, &c. in the lowest denomination mentioned, which multiply by the number of pieces, &c. the product will be the contents of the whole-if the pieces, &c. be of unequal contents, find the content of each, add these together, and the sum of them will be the whole quantity. The the standard of the

7. The term which asks the question, or that which implies the demand: is generally known by some of these words going before it of Hew much ! How many? How long? What cost? What will? &c. The transfer at the at

EXAMPLES.

1. If 9lbs. of tobacco-cost 6s. what will 25 lbs cost?	er um grander
As 9: 6:: 25 to the answer. tion, (what will 25) 25 the third term, by third place: 9lbs, be 30. 12 anne name with the second term.	heaks, the ques- bs. frc.) is made being put in the eing of the same and 6s. of the term sought, the
9)150(16 8 courses, 1 multiply the second terms together, and first. The remaind to pence, and divide questions make the	d divide by the ler (6) I reduce as before. The answer 16: 8d.
9)72(8) 72	tem jakoriorikansi. Jargi sepal saasaa m

By inverting the order of the question it will stand thus, at some 2. If 6s. buy 9!bs. of tobacco, what will 16s. 8d. buy feet have self of

s. d.	Minimizer បានប្រើប្រើប្រជាជាធិបាន សម្រើនិង សម្រើប្រើប្រាស់
6 16 8	Here the term which tasks the
12 12	question (16s. 8d.) is of different de-
$\underbrace{\qquad}_{i=1}^{n} (-i) = (i + 1)^{n} \underbrace{\qquad}_{i=1}^{n} (-i) = (i + 1)^{n} \underbrace{\qquad}$	nominations; it must, therefore, be
72 pence. 200 pence.	reduced to the lowest denomination
	mentioned (pence) as must also the
pence. lbs. pence.	other term of the same name, come-
	quently, to be the first term.
	time of their north panes will by barrier

California exceptione more of the progress

Water a section of the common of La ting half half so sold income

als all to come term terms of the slave as

a few teachtrice was start to believe there at the

72)1860(2515. answer line to take all words to an early write. It mark of more if more than one feel of

560

Again—By inverting the order of the question.

3. If 16s. 8d. (=200 pence) buy 25lbs. of tobacco, how much will 6s. (=72 pence) buy?

OPERATION. lbs. d. ... As 200 : 25 : 72 , 72

50 175

2|00)18|00(9lbs. Ans. 18

These three questions are only the first varied; they shew how any question in this rule may be inverted.

4. If loz. of silver cost (s. 9d. what will be the price of a silver cup that weighs 9oz. 4pwt. 16grs. ?

> Note.-As each of the terms contain different denominations, they must all be reduced to the lowest denomination mentioned.

Ans. 747 pence, $3\frac{3}{8}q$, which must be reduced to the highest denomier expedite with by principle, our armore a mation, thus,

and graph the management of a system of the configuration of pence. 20,747 Rem. 3d.

Burney Burney

and the contract of the contra and the second of the way of the bank of the same of t

breaker to a time defined the a store per ounce, I demand the weaper Dai Beile Bereit 32 10

Commence of Selection and the account of the to price on the following the company of the same and the same of the dans And if the rate

> E. Hith oracle pare their, Hickory Burn Burn Carlo Carlo Burn Burn Com Com Contraction Per Clarker out a partie 🔻 وقري والإنجاب والمعار ويحمد فقو

5. If 6 herses eat 21 bushels of oats in 3 weeks, how many bushels will 20 horses eat in the same time?

Ans. 70 bushels.

The same question inverted.

6. If 20 horses eat 70 bushels of oats in 3 weeks, how many bushels will 6 horses eat in the same time?

Ans. 91 bushels.

The statement of every question requires thought and consideration;—
here are four numbers given in the
question; to know which three are to
be employed in the statement, there can be no difficulty if the scholar proceed deliberately and as his rule directs—first consider which of the given
numbers it is that asks the question; that determined on, put it in the
third place, then seek for another number of the same name, or kind, put
that in the first place, the second place must now be occupied by that
number which is of the same name or kind with the number sought; when
these steps are cautiously followed, the scholar cannot fail to make Lis
statement right.

- 7. If an ingot of silver weigh 36oz. 10put. what is it worth at 5t. per ounce? Ans. £9 %. 6d.
- 8. A Goldsmith sold a Tankard for £10 12s. at the rate of 5s. 4d. per ounce, I demand the weight of it.

 Ans. 39os. 15pms.

9. If the moon move 13deg. 10min. 35sec. in one day; in what time does at perform one revolution?

Ans. 27days. 7hrs. 43min.

10. If a family of 10 persons spend 3 bushels of malt in a month, how many bushels will serve them when there are 30 in the family?

Ame. 9 bushele

to a forgation to be an early for a company of the contract of

11. If a family of 30 persons spend 9 bushels of malt in a month, how many bushels will serve a family of 10 persons the same time?

Ans. 3 bushels.

12. If 12 acres, 3 goods, produce 78 courters 3 pecks, how much will 35 acres, 1 reed, 20 goles produce?

Ans. 216 grs. 5 bush. 12 pecks.

s american 14 le le la company

ساسست يور ورو فرور وروايون

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And Alexander of the control of t

13. If 5 acres. 1 rood produce 26 quarters, 2 bushels, how many acres will be required to produce 47 quarters, 4 bushels? Ans. 9 acres, 2 roods

ALCOHOLD BEACH BEING

14. If 365 men consume 75 barrels of provisions in 9 months, how much will 500 men consume in the same time? Ans. 10244 barrels.

The first partition of the second section of the

A Committee of the state of

15. If 500 men consume 10244 barrels of provisions in 9 months, how much will 365 men consume in the same time ?

المعاري أوالحؤر والوالي المووود العالما المالي

Commence of the second contract of the second

OPERATION. outers at courtels will be at

Multiplied by

The transport of the state of t 73 the denominator of the fraction.

306 714

Add 54 the numerator.

As 500 : 7500 :: 365

7500

182500 2555

5|00)27375|00 73)5475(75 *A*ns.

511

365 365

Note. In the 15th example, in order to embrace the fraction (#4 of a barre!) the integers 102 barrels must be multiplied by the denominator of the fraction (73) and the numerator, (54) added to the product.

After division, the quotient must be divided by the denominator of the fraction, and this last quotient will be the answer, all which may be seen in the example.

The Scholar must remember to do the same in all similar cases.

16. How much will 4 pieces of linen containing, viz. 351, 36, 371, and 38 yards come to at 79 cents per yard? Ans. \$116,13.

\$100 for 12 months, what must ! give for 357,82 the same time?

Ans. \$21,469.

17. If I give \$6 for the use of . . 18. How many tiles of 8 inches square will lay a floor 20 feet long, and 16 feet broad?

Ans 720.

19. If 2lb. of sugar cost 25 cents, what will 100/b. of coffee cost, if 8lb. of sugar are worth 5lb. of coffee? Ans. \$20.

20. It £3 sterling be equal to £4 N. England currency, how much N. England currency will be equal to £1000 sterling?

Ans. £1333 6s. 8d.

21. If I buy 7lb. of sugar for 75 cents, how much can I buy for 6 Ans. 561b. dollars ?

N. B Sums in Federal Money are of the same denomination when the decimal places in each are equal.

To reduce sums in Federal Money to the same denomination, annex so many cyphers to that sum which has the least number of decimal places. or places of cents, mills, &c. us shall make up the deficiency

SINGLE RULE OF THREE DIRECT. Sect. 11. 8.

22. If I buy 76 yards of cloth for 23. A man spends \$3,25 per \$113,17, what did it cost per Ell week, what is that per annum? English?

Ans. \$1,861.

Ans. \$169,464.

124

24. If 3 horses and 4 oxen be worth 9 cows, how many cows will 6 horses and 8 oxen be worth i Ass. 18.

25. Bought a silver cup, weighing 9oz. 4pwt. 16grs. for £3 2s. 3d. 33q what was that per ounce?

Ans. 6s. 9d.

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26. There is a cistern which has 4 cocks, the first will empty in 10 minutes, the second in 20 minutes, the third in 40 minutes, and the fourth in 80 minutes; in what time will all four running together empty it?

Min. Cist. Min. Cist.

20 : 1 :: 60 : 3
40
80
In 1 hour the 4 cocks
would empty - - - 11,25 Cist.
Then, Cist. Min. Cist. Min.

Cist. Min. Cist. Min. As 11,25: 60: 1: 5,33 Ass.

27. A man having a place of land to plant, hired two men and a boy to plant it, one of the men could plant it in 12 days, the other in 16 days, and the boy in 27 days; in how long time would they plant it if they all worked together?

Ans. 5,346 days.

28. A merchant bought 270 quintals of cod fish, for \$780; freight \$37,70; duties and other charges \$30,60; what must be sell it at per quintal to gain \$143 in the whole?

Ans. \$3,671.

The sum of all the expenses of the fish with the Merchan's gain must be found for the second term. 29. If a staff 5ft. 8in. in length cast a shadow of 6 feet; how high is that steeple whose shadow measures 153 feet?

Ans. 1441 feet.

30. Bough 12 pieces of cloth each 10 yards, at \$1,75 per yard, what each containing \$4 Elm English. for came they to !

31. Bopght 4 pieces of Helland, \$96; how much was that per yard? Ans. 80 cents

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32. Bought 9 chests of ten, each weighing 3C. 2prs. 218. at £4 9a An. £147 130. 8jd. per cast, what came they to ?

Carl Late & to great an extension & 182 Company of the second of the second of and the state of the state of the state of The first term of the manufactor of the in a constant of the state of the state of

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Sugar Salar

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33. A bankrupt owes in all 972 dollars, and his money and effects are but \$607,50; what will a creditor receive on \$11,333? Am. \$7,063

The state of the s 34. Bought 126 gallons of rure for \$110, how much water must be added to it to reduce the first cost to 75 cents per gallon? Ans. 201 gal. The state of the s

The state of the s

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Secretary of the same of the same

35. A owes B £3475, but B compounds with him for 13s. 4d. on the \$145 pays \$12,63 of parish taxes, pound; what must be receive for how much should a person pay his debt Ass. £2316 13c. 4d.

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> whose rent is \$378? Ane. \$22,925.

Inverse Proportion.

IN some questions the number sought becomes less, when the circumstances from which it is derived become greater. Thus when the price of goods increase the quantity which may be bought for a given sum, is smaller When the number of men employed at work is increased, the time in which they may complete it becomes shorter; and when the activity of any cause is increased, the quantity necessary to produce any given effect is diminished.

These and the like cases belong to the

SINGLE RULE OF THREE INVERSE.

The Single Rule of Three Inverse teaches by having three numbers given to find a fourth, having the same proportion to the second, as the first has to the third.

If more require less, or less require more, the question belongs to the Single Rule of Three Inverse.

More requiring less, is when the third term is greater than the first, and

requires the fourth term to be less than the second.

Less requiring more, is when the third term is less than the first, and requires the fourth term to be greater than the second.

"Space and reduce the tamps as in the rule of three directs; then multiply the first and second terms together, divide the product by the third, and the quotient will be the answer in the same denomination with the econd term."

EXAMPLES.

1. If 48 men build a wall in 24 days, how many men can do the same in 192 days?

OPERATION.

Men. Days. Men. As 48: 24:: 192
48

--

192 • • 96

192)\$152(6 UnSber.

Here the third term is greater than the first, and common sense teaches the fourth term, or answer must be less than the second; for if 48 men can do the work in 24 days, certainly 192 men will do it in less time. In this way it may be determined if a question belong to the Rule of Three Tilverse.

3. How many yards of sarcenet, 3qrs. wide, will line 9 yards of cloth of 8qrs. wide?

Ans. 24 yards.

2. If a board be 9 inches broad, how much in length will make a square foot?

Ans. 16 inches.

- 4. Lent a friend 292 dollars for 6 months; some time afterwards he lent me 806 dollars: how long may I keep it to balance the favor?

 Ans. 2 months, 5 days.
- 5. A garrison had proving for 8 months, at the rate of 15 ounces to each person per day; how much must be allowed per day in order that the provision may last 91 months?

 Ans. 1244 ounces.

6 A garrison of 1200 has provisions for 9 months at the rate of 14 ounces per day, how long will the provisions last at the same allowance if the garrison be reinforced by 400 men?

Pas 67 months.

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the first the state of the state of the state of

7.——How must the daily allowance be in order that the provisions may last 9 months after the garrison is reinforced?

Aus. 104 ounces.

War to the property of the property

8. How much land at \$2,50 per acre should be given in exchange for 360 acres at \$3,75 per acre?

Ans. 540 acres.

Committee of the second of the second

What sum should be put to interest to gain as much in 1 month as \$127 would gain in 12 months?
 Ans. \$1524.

The second of th

- 10. If man perform a journey in . 15 days, when the day is 12 hours long, in how many will he do it when the day is but 10 hours?
 - Ans. 18 days.
- 11. If a piece of land 40 rods in length, and: 4 in breadth make an acre, how wide must it be when it is but 25 rods long? Ans. 62 rods.

- 12. There was a certain building raised in 8 months by 120 workmen, but the same being demolished, it is required to be built in two months; I demand how many men must be employed about it? Ans. 480 men
- 13. How much in length, that is 3 inches broad, will make a square foot? Ans. 48 inches.

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and the part of the augment of the Section with the second to the second at the second They gest on a second of the The street of the two was exercise in the product of advantage with the companie Contract to the Surge Sept of

14. There is a cistern having 1 pipe which will empty it in 10 hours, how many pipes of the same capacity will empty it in 24 minutes? Ans. 25 pipes.

15. If a field will feed 6 cows 91 days, how long will it feed 21 cows ? Ans. 26 days.

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16. If the quartern loaf weigh 41 pounds when wheat is \$2 per bushel, what must it weigh when wheat is \$1.50 the bushel? Ans. Clb.

17. How many yards of baize, 3 quarters wide, will line a cloak which has in it 12 yards of camblet, half yard wide?

Ans. 8 yards.

GENERAL RULE

For stating all questions whether direct or inverse.

1. Place that number for the third term, which signifies the same kind of thing, with what is sought, and consider whether the number sought will be greater or less. If greater, place the least of the other terms for the first; but if less, place the greater for the first, and the remaining one for the second term.

Multiply the second and third terms together, divide the product by the

first, and the quotient will be the answer.

EXAMPLES.

1. If 30 borses plough 12 acres, how many will 40 plough in the same time? OPERATIONS.

H. H. 30:40::12

12

30) 480(16 Ans.

Here because the thing sought is a number of acres, we place 12, the given number of acres, for the third term; and because 40 horses will plough more than 12, we make the lesser number, 30, the first term, and the greater number 40, the second term.

2. If 40 horses be maintained for a certain sum on hay at 5 cents per stone, how many will be maintained, on the same sum, when the price of hay rises to 8 cents per stone?

C. C. Н.

8:5::40

8)200(25 Ans. 16

Here, because a number of horses is sought, we make the given number of horses, 40, the 40. third term, and because fewer will be maintained for the same money, when the price of hay is dearer, we make the greater price 8 cents. the first term, and the lesser price, 5 cents, the second.

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The first of these examples is Direct, the second Inverse.

Every question consists of a supposition and a demand.

In the first the supposition is, that 30 horses plough 12 acres, and the demand how many 40 will plough? and the first term of the proposition, 30,

is found in the supposition in this and every other direct question.

In the second, the supposition is that 40 horses are maintained on hay at 5 cents per stone, and the demand, how many will be maintained on hay at 8 cents? and the first term of the proportion, 8, is found in the demand, in this and every other inverse question.

3. If a quarter of wheat afford 60 it?

tenpenny loaves, how many eight- gain 6 dollars interest, what will gain penny loaves may be obtained from the same sum in 5 months? Ans. 240 dellare Ans. 75 loaves.

4. If in 12 months, 100 dollars

SUPPLEMENT TO THE SINGLE RULE OF THREE.

QUESTIONS.

- 1. What is the Single Rule of Three; or the Rule of Proportion?
 - 2. How many kinds of Proportion are there?
- 3. What is it that the Single Rule of Three Direct teaches?
- 4. How can it be known that a question belongs to the Single Rule of Three Direct?
 - 5. What is understood by more requiring more and less requiring less?
 - 6. How are questions in the Rule of Three stated?
- 7. Having stated the question, how is the answer found in direct proportion?
- 8. What do you observe of the first and third terms concerning the different denominations, sometimes contained in them?
- 9. When the second term contains different denominations, what is to be done?
- 10. How is it known what denomination the quotient is of?
 - 11. If the quotient or answer be found in an inferior denomination, what is to be done?
 - 12. When the terms are given in Federal Money, how is the operation conducted?
- 13. How are the sums in Federal Money reduced to the same denomination?
- 14. When any number of barrels, bales, places, &c. are given, what is
- 15. What is it that the Single Rule of Three Inverse teaches?
 - 16. How are the questions stated in Inverse Proportion?
- 17. What is understood by more requiring less and less requiring more?
- 18. How is the answer found in the Rule of Three Inverse?
 - 12. What is the general Rule for stating all questions, whether Direct or Inverse?

EXERCISES.

. If my horse and saddle are worth 18 guineas, and my horse be worth reses so much as the saddle, pray what is the value of my horse?

Ans 72 dollars.

- 2. How many yards of matting that is half a yard wide will cover a room that is 18 feet wide and 30 feet long?

 Ans. 120 wards.
- 3. Suppose 800 soldiers were placed in a garrison, and their provisions were computed anticient for two months; how many soldiers must depart that the provision may serve them 5 months? Ans. 480.

- 4. I borrowed 185 quarters of corn when the price was 19s. how much must I pay to indemnify the lender when the price is 17s. 4d.?

 Ans. 20241.
 - 5. Bought 45 barrels of beef at \$3,50 per barrel, among which are 16 barrels, whereof 4 are worth no more than 3 of the others; how much must I pay?

 Ans. \$143,50.

Method of assessing rooms or good to rive so

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6. A and B depart for the same place and travel the same road; but Lagore 5 days before. B at the rate of 20 miles per day; B follows at the rate of 25 miles per day; in what time and distance will be overtake A?...

Ans. B will overtake A in 20 days, and travel 500 miles.

Here two statements will be necessary, one to ascertain the time, and the other to ascertain the distance.

and the more was the control of the

Method of assessing town or parish taxes.

1. An inventory of the value of all the estates, both real and personal, and the number of polls for which each person is rateable, must be taken in separate columns. Then to know what must be paid on the dollar, make the total value of the inventory the first term; the tax to be assessed the second; and 1 dollar the third, and the quotient will shew the value on the dollar.

Nove. This method is taken from Mr. Pixx's Arithmetic, with this difference, that here the meany is reduced to Federal Ourroscy.

- 2. Make a table, by multiplying the value on the dollar by 1, 2, 3, 4, 5, &c.
- 3. From the Inventory take the real and personal estates of each man, and find them separately, in the table, which will shew you each man's proportional share of the tax for real and personal estates.

If any part of the tax be averaged on the polls, before stating to find the value on the dollar, deduct the sum of the average tax from the whole sum to be assessed; for which average make a separate column as well as for the real and personal estates.

EXAMPLES.

Suppose the General Court should grant a tax of 150000 dollars, of which a certain town is to pay \$3250,72 and of which the polls being 624 are to pay 75 cents each; the town's inventory is 69568 dollars; what will it be on the dollar; and what is A's tax (as by the inventory) whose estate is as follows, viz. real, 856 dollars; personal, 103 dollars; and he has 4 polls?

Pol. Cts. Pol. Dolls.

1. As, 1: ,75: 624: 468 the average part of the tax to be deducted from \$3250,72 and there will remain \$2782,72.

Dolls. Dolls. Cts. Dolls. Cts.

2. As 69568: 2782,72::1: 4 on the dollar.

TABLE.

Dolls.	Dolls, cts.	Dolls.	Dolls.	çts.	Dolls.	Dolls.
1 is	4	20 is	1	80	200 is	8
2 —	8 .	30 —	1	20	300	12
š —	12	40	1	60	400	16
4 —	16	<i>8</i> 0 —	2	00	500	'20
5 —	20	60	2	40	600:	24
6 —	24	70		80	700	28
7 —	28	80 —		20	800	32
8 —	32	90	3	60	900	36
9 —	36	100 —	. 4	00-	1000	40
10 —	40			:	•	

Now to find what A's rate will be. His real estate being 856 dollars, I find by the Ta ble that 800 dollars is \$32 cts.

2 that 50 -that 6 — —

Therefore the tax for his real estate is 34 24

In the like manner I find the tax }
r his personal estate to be for his personal estate to be

His 4 pells, at 75 cents each, are

\$41 36

Real. Dolls. Cts.	Personal. Dolls. Cts.	I	Po Dolls	lls. . Cts.	F.	Tot Dolls.	al. Cts.	· . · . :'		
34 24	4 12	·	3	0	F	4.1	38	.1	•	

. 9. DOUBLE RULE OF THREE.

THE Double Rule of Three, sometimes called Compound Proportion, teaches by having five numbers given to find a sixth, which, if the proportion be direct, must bear the same proportion to the fourth and fifth as the third does to the first and second. But if the proportion be inverse, the sixth number must bear the same proportion to the fourth and fifth, as the first does to the second and third.

RULE.

1. "State the question, by placing the three conditional terms in such order that that number which is the cause of gain, loss, or action, may possess the first place; that which denotes space of time, or distance of place, the second; and that which is the gain, loss, or action, the third."

2. " Place the other two terms, which move the question, under those

of the same name."

- 3. "Then, if the blank place, or term sought, fall under the third place, the proportion is direct, therefore, multiply the three last terms together, for a dividend, and the other two for a divisor; then the quotient will be the answer."
- 4. "But if the blank fall under the first or second place, the proportion is inverse, wherefore multiply the first, second and last terms together, for a dividend, and the other two, for a divisor; the quotient will be the answer."

EXAMPLES.

If 100 dollars gain 6 dollars in 12 months, what will 400 dollars gain in 8 months?

Statement of the question.

D. M. D.

100: 12:: 6 Terms in the supposition, or conditional terms.

400: 8 Terms which move the question.

Of the three conditional terms, it is evident that 100 dollars put at interest, is that one which is the cause of gain; consequently 100 dollars must be the first term; and because 12 months is the space of time in which the gain is made, this must be the second term; and 6 dollars which is the gain, the third erm. The other two terms must then be arranged under those of the same same:

Now as the blank falls under the third place, therefore, the question is in direct proportion, and the answer is found by multiplying the three last terms together for a dividend, and the two first for a divisor.

OPERATION.

100 : 12 :: 6

400 8 Then, 12|00)192|08(

8

Dolls. 16 Sign

1200 Divisor, 19200 Dividend.

2. If 100 dollars gain 6 dollars in 12 months, in what time will 400 dol wain 16?

OPERATION. D. M. D. Here the blank falling under the second term, the 100:12::6 400 16 proportion is indirect. 12 Therefore multiply the first, second and last terms 6 together for a dividend, and the other two for a divisor. 2400 div. 192 100

19200 dividend.

M.

Then 24|00)192|00(8 Answer.

192

3. A Farmer sells 204 dolls. worth of grain in 5 years, when it is sold at 60 cents per bushel, what is it can reap 100 acres in 5 days? per bushel when he sells 1000 dolls. worth in 18 years, if he sell the same quantity yearly?

Cts. Y. D.

M. D. A.

7:12::84 5:: 100 · 20 Ans.

4. If 7 men can reap 84 acres of

wheat in 12 days, how many men

80 : 5 : 204 cts. m. 18 : . 1000 : ,816 Ans.

5. If a family of 9 persons spend 450 dollars in 5 months, how much would be sufficient to maintain them 8 months, if 5 persons more were added to the family? Ans. \$1120.

SUPPLEMENT TO THE DOUBLE RULE OF , THREE.

QUESTIONS.

- 1. What is the I ouble Rule of Three; or Compound Proportion?
- 2. How are questions to be stated in the Double Rule of Three?
- 3. How is it known after the statement of the question, whether the Proportion be Direct or Inverse?
- 4. When the Proportion is Direct, how is the answer to be found?
- 5. When the Proportion is Inverse, how is the answer to be found!

EXERCISES.

1 If 6 men build a wall 20 feet long, 6 feet high and 4 feet wide in 16 days, in what time will 24 men build one 200 feet long, 8 feet high and 6 thick? Ans. 80 days.

The solid contents
in each piece of wall
according to the given
dimensions, must be
found before stating
the question.

2. If 40lb. at Boston make 36 at Amsterdam, and 90lb. at Amsterdam make 116 at Dantzick, how many lb. at Boston are equal to 260lb. at Dantzick?

Ans. 224 4alb

Catholina significance of the control of

 $v_{\rm c} \approx 2.00$ m, $v_{\rm c} \approx 200$ m, and $v_{\rm c} \approx 2.00$ m, and the vertical value of the $v_{\rm c} \approx 2.00$

N. B. The answer to this question is found by two statements in the Rule of Three Direct

3. If the freight of 12Cwt. 2grs. 6lb. 275 miles cost \$27,78; how far may 60Cwt. 3qrs. be shipped for \$234,78? Ans. 480 miles.

4. An asurer put out 75 dollars, at interest, and at the end of eight months received for principal and interest, 79 dollars; I demand at what rate per cent he received interest? Ans. 8 per cent.

5. If 7 men can make 84 rods of wall in 6 days; in what time will 10 men make 150 rods?

Ans. 71 days.

140 SUPPLEMENT TO THE DOUB R. OF THREE. Sect. II. 9.

6. If the freight of 9hhds. of sugar, each weighing 12Cwt. 20 leagues, cost £16; what must be paid for the freight of 50 tierces ditto, each weighing 21 Cwt. 100 leagues?

Ans. £92 11s. 102d

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10. PRACTICE.

"PRACTICE is a contraction of the Rule of Three Direct, when the first term happens to be an unit or one; it has its name from its daily use among Merchants and Tradesmen, being an easy and concise method of working most questions which occur in trade and business."

Proor. By the Single Rule of Three, Compound Multiplication, or by varying the parts.

Before any advances are made in this rule, the learner must commit to memory the following

TABLES.

d. s. and £. 6 is is in the state of the sta	Pts. of a pound. s. d. is £. riety of cases, the multiple of which serves little 6 8	else than a mind of the method, and the ew cases, and easy ar in his
1 — 13 — 110 2 — 10 — 10 1 — 14 — 110	1 8 for the scholar to be 1 4 i memory. 1 3 Rhe small simples	of exam- will be plement; olar to a

OPERATIONS.

POUNDS, SHILLINGS, PENCE, FARTH.

When the price of the given quantity is £1. 1s. 1d. per pound, yard, &c. then will the quantity itself be the answer at the supposed price.—
Therefore,

CASE 1.

When the price of 1 yard, pound, &c., consists of farthings only; If it be one farthing, take a fourth part of the quantity; if a half penny, take a half; if three farthings, take a half and a fourth of the quantity and add them. This gives the value in pence, which must be reduced to pounds.

DOLLARS, CENTS, MILLS.

RULE.

Multiply the quantity by the price of one pound, yard, &c. the product will be the answer.

At the tend formy 988 the walk to

EXAMPLES.

1. What will 362 yards cost at 7 mills per yard?

OPERATION.
2)362
12)181 pence.

15s. 1d. Ans.

Here the quantity stands for the price at one penny per yard, but as two far hings are but half one penny, therefore dividing the quantity by 2, gives the price at half a penny per yard, which must be reduced to shillings.

2. What will 3541 yards cost at 1d per vard?

OPERATION.

4)354 2

12)68 · 2 · fres.

Committee and the second section of the sec

The second section is

English Committee Committee

4. What will 816 yards cost at 1q. oer yard? Aus. 17s.

DOLLARS, CENTS, MILLS.

1. What will 362 yards cost at 7 mills per yard?

OPERATION.
3 6 2 quantity.
,0 0 7 price.

\$2, 5 3 4 Aus.

Note. The answers in the different kinds of money will not always compare, because in the reduction of the price, a small fraction is often lost or gained.

2. What will 3541 yards cost at 3 mills per yard?

OPL TATION.

e garago e como en espera de la care de

3 5 4 ,5 quantity.

,0 0 3 price.

\$1,0635

· •

S. What will 263 yards cost at 1 cent per yard?

Ans. \$2,63.

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4. What will 816 yards cost at 3 mills per yard? Ins. \$2,448.

5. What will 97 yards cost at 3q. per yard?

Ans. 6s. 03d.

6. What will 126 yards cost at 1d. per yard?

Ans. 5s. 3d.

POLLARS, CENTS, MILLS.

5. What will 97 yards cost at 1 cent per yard?

Ans. .97cts.

6. What will 126 yards cost at 7 mills per yard?

Ans. \$0,882.

CASE 2.

When the price of 1lb. 1yd. &c. consists of pence, or of pence and farthings; if it be an even part of a shilling, find the value of the given quantity at 1s. per yard, (the quantity itself expresses the price at 1s. per yard; if there are quarters, &c. write for 1 3d. for 1 6d. for 3 9d.)
and divide by that even part which the price is of I shilling. If the price be not an aliquot or even part of one shilling, it must be divided into two or more aliquot parts; calculate for these separately, and add the values; the answer will be obtained in shillings, which must be reduced to pounds.

EXAMPLES.

1. What will 476 yards cost at 71d. per yard?

OPERATION.

6d. | \frac{1}{4} | 476 Price at 1s. per yard.
1\frac{1}{4}d. | \frac{1}{4} | 238 Price at 6d. per yard.
59 6d. price 1\frac{1}{4}d. per yard.

2|0)29|7 6d. price at 7\frac{1}{2} per yd. £14 17s. 6d. Ans.

PROOF.

1. By the Rule of Three.

Y. £. s. d. Y. As 476: 14 17 6::1

> 297 12

476)3570(7d. 3332

238

)952(2*qr*. 952

2. By Compound Multiplication.

£. s. d.

7½ price of 1 yard.

6 3 price of 10 yards. 10

3 2 6 price of 100 yards.

12 10 0 price of 400 yards.

2 3 9 price of 70 yards.

3 9 price of 6 yards.

£14 17 6 price of 473 yards.

DOLLARS, CENTS, MILLS.

7. What will 476 yards come to al 10 cents 4 mills per yard?

operation.
476
,104

1904 4760

\$49,504 Ams.

PROOF.

cts. m. D. cts. m. yds. ,10 4)49 50 4(476 4 1 6

> 7 9 0 7 2 8

> > 624

What will 176 yards cost at 91d. per yard?

OPERATION.

6d.	ł	176 value at 1s. per yard.
3d.	ŧ	88 value at 6d. per yard. of 44 value at 3d. per yard.
<u> </u> d.	1 # c	of 44 value at 3d. per yard. 7 4d. val. at ‡d. per yd.

2|0)13|9 4d.—at 9\d. per yd. \(\frac{1}{2}\) £6 19s. 4d. Ans. PROOF.

Conservation fifty to the second of the said Carried and the second of the

3. What will 5684 yards cost at 9. What will 5684 yards cost at 7d. per yard? Ans. £16 11s. 54d

Commo and them to the fit

DOLLARS, CRETS, MILLS.

8. What will 176 yards cost at 13 cents, 2 mills, per yard?

Ans. \$23,232.

9 cents 7 mills per yard? Ans. \$55,12.

٠1.

4. What will 685? yards come to at 21d. per yard?

Ans. £7 2s. 101d.

DOLLARS, CENTS, MILLS. 10. What will 6857 yards come to at 3 cents 5 mills per yard?

Ans. \$24,001.

5. What will 649} yards cost at 0d. per yard? Ans. £27 1s. 0}d.

11. What will 649‡ yards cost at 13 cents 9 mills per yard? Ans. \$90,245.

6. What will 683‡ yards cost at 12. What will 683‡ yards 8½d. per yard? Ans. £23 103. 0¾d 11 cents 7 mills per yard? 13 Maria Patricia

12. What will 683# yards cost at Secretary and

CASE 3.

If the price of 1lb. 1yd. &c. be shillings and pence and an even part of £1, Divide the value of the given quantity at £1 per yard by that even part, which the price is of £1. The quotient will be the answer.

EXAMPLES.

1. What will 7191 yards cost at 1s. 4d. per yard? OPERATION.

£. s. | 1s. 4d. | 1 | 719 10 price at £1 [per yd. 143 18 price at 4s. [per yd.

Ans. 47 19 4d. at 1s. 4d. per yd.

Here for the sake of ease in the operation, because 5×3=15, therefore I divide the price at one pound per yard by 5, and that quotient by 3 which gives the answer.

2. What will 648 yards cost at 14. What will 648 yards cost at 1s. 8d. per yard? Ans. £54.

3. What will 1671 yards cost at 3s. 4d. per yard . Ans.£27 18s. 4d. 55 cents, 6 mills per yard?

a con street girlt how has been a

real of the later

DOLLARS, CENTS, MILLS.

13. What will 7194 yards cost at 22 cents, 3 mills per yard? Ans. \$160,448.

27 cents and 8 mills per yard? Ans. §180,144.

15. What will 1874 yards cost at Ans. \$93,13.

4. What will 687 j yards cost at 5e. per yard? Ans. £171 17s. 6d.

CASE 4.

When the price of 1yd. 4rc. is shilings, or shillings, pence and farthings, and not an even part of £1. Multiply the value of the quantity at 1s. cer yard by the number of shillings; or the pence and farthings, take parts, as in case 2, the results added vill give the answer, which must be reduced to pounds.

If the price be shillings only, and an even number; multiply by half the price or even number of shillings for one yard, double the unit figure of the product for shillings, the remain-

og figure will be pounds.

Note. When the quantity conains a fraction, work for the integers, and for the fraction take proportional parts of the rate.

EXAMPLES.

1. What will 167½ yards cost at 17s. 6d. per yard?

OPERATION.

| 6d. | 1 | 167 17 1169

> 2839 price at 17s. per yd. 83 6—at 6d. per yard. 8 9 price of 1 yard.

2|0)203|1 3d.

167

Ans. £118 11s. 37.

DOLLARS, CENTS, MILLS.

16. What will 687 | yards cost at \$3 cents, 3 mil's per yard?

Auc. \$572,667.

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1. 新加州 南美國 美国新 美线 化碳烷 (c)

2. What will 5482 yards cost at 12s. 44d. per yard?

Ans. £3391 19s. 9d.

DOLLARS, CENTS, MILLS.

18. What will 5482 yards cost at \$2,063 per yard?

Au. \$11309,366

3. What will 614 yards cost at 16s. per yard?

OPERATION. 614

8 haif the price.

4912 double the first figure £491 4s. Ans. [for shell.

4. What will 175 yards cost at 20. What will 176 yards cost at 12s. per yard? Ans. £105 12s. 42 per yard? Ans. \$352.

TO, What will been properties to 1.61 & .sex. 1 trasy 1891 53

5. What will 36 yards cost at ". 6d. per yard ? Ana. £13 Ka

19. What will 614 yards cost at \$2,667 per yard? Ass. \$1637,538.

Sec. 4" 1

the sax of street a cold there is a Mile THE EDUCATION OF HIS MAKE THE

21. What will 26 yards cost at \$1,25 per vard?

CASE 5.

When the price of 1yd. 1lb. &c. is pounds, shillings and pence; multiply the quantity by the pounds, and if the shillings and pence be an even part of a pound, divide the given quantity by that even part, and add the quotient to the product for the answer; but if they are not an even part of £1, take parts of parts and add them together. Or, you may reduce the pound in the price of 1 yard, &c. to shillings, and proceed as in the case before.

EXAMPLES.

1. What will 59 yards cost, at £6 7s. 6d. per yard?.

OPERATION.

50. is } of £1. 59 value of £1 per yd.

354 at £6 per yd.

2s. 6d. is 1 of 5. 14 6s. at 5s. per yd. 7 1 6d. at 2s. 6d. [per yd. 4s. 6376] 8d. at 68

Ans. £376) , 6d. at £6 [7s. 9d.

3. What will 163 yards cost, at £2 8s. per yard? Aus.,£391 4s.

DOLLARS, CENTS, MILLS

22. What will 59 yards cost, at \$21,25 per yard?

D. C.

21,25 59

191 25 1062 5

\$1253 75 Am. 104 .22

23. What will 163 yards; cost, at \$8 per yard? Am. \$1304.

The transfer the time with the

POUNDS, SHILLINGS, PENCE, FARTH. 3. What will 76 yards cost at £3 2s. 7d. per yard?

OPERATION.

6d. is 1 of 1s. 76 value at 1s. per yd. 62-shillings in £3 2s.

152 value at 2s. per yd. 456 —at 60s. per yd. 1d. is i of 6d. 38—at 6d. per yard. 6 4d.—at 1d. per yd.

210)475|6

- Aus. £237 16s. 4d.

4. What is the value of 84 yards at £2 14s. per yard?

Profession Committee to the con-

Promote the dock of the

But the training from the are the endings of a fire

DOLLARS, CENTS. MILLS. 24. What will 76 yards cost at \$10,43 per yard ?

at \$9 per yard ?

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SUPPLEMENT TO PRACTICE.

QUESTIONS.

- 1. What is Practice?
- 2. Why is it so called?
- 3. When the price of 1 yard, &c. is farthings, how is the value of any given quantity found at the same rate?
- 4. When the price consists of pence and farthings, and is an even part of 1s. how is the value of any given quantity found?
- 5. When the price is pence and farthings and not an even part of 1: what is the method of procedure?
- 6. When the price consists of shillings, pence and farthings, how as the when of envious quantity found?

 So When the price contains slithings and pence and an even part of £1,
- how is the operation to be conducted?
- 8. When the price consists of shillings only, and an even number, what is the most direct way to find the value of any given quantity?
- 9. When the quantity contains fractions, as 1, 1, 2, &c. how are they to be treated?
- 10. When the price consists of pounds, and lower denominations, how is the value of any given quantity found?
- 11. When the prices are given in dollars, cents, and mills, how as the value of any given quantity found in Federal Money?
- 12, What is the method of proof?
- 13. How are operations in Federal Money proved?

EXERCISES IN PRACTICE.

In the following exercises the attention of the scholar must be excited first to consider to which of the preceding cases each question is to be referred. That being ascertained, he will proceed in the operation according to the instruction there given.

1. What will 745‡ yards cost at 11d. per yard?

Ans. £34 3s. 71d.

Under which of the preceding cases does this question properly belong?

What must be done with the fraction (3 of a vard) in the quantity?

2. What will 984 yards cost at 1s. 8d. per yard? Ass. £80 6s 8d. OPERATION

5. What will 567) yards cost, at 34d. per yard? Au. £3 10s. 111d.

6. What will 9131 yards cost, at 6d. per yard ? be. £22 16e. 9d.

7. What will 9123 yards cost, at . 8. What will 76 yards cost, at 2d 9d. per yard?

Ans. £34 4s. 41d. per yard?

9. What will 845 yards cost, at 8s per yard? Au. £338.

The first of the same beg

10. What will 91 yards come to at 16s. per yard?

. A REPORT TO A CONT. अंद्रशं के । कर

11. What will 1561 yards conie to at 6e. 4d. per yard? Ans. £49 11s. 2d.

-3 & 5 \$7 00 00 00th A The state of the

12. What will 96 yards cost at 10e. 11d. per yard? Ane. £48 121.

施 海路通过交易管理 指电电气管 法 may to see and see 13. What will 67½ yards cost, at 14. What will 843 yards cost, at 12. 2d per yard? Ans. £41 1s. 3d. 6s 8d. per yard? Ans. £281.

15. What will 75 yards cost, at £3 3c. 4d. per yard?

Ano. £237 10c.

16. What will 59 yards come to, at £8 7c. 6d. per yard?

Ano. £237 2c. 6d.

17. What will 593 yards come to, 18. What will 68 yards cost, at at £3 6s. 8d, per yard 2 £4 6s. per yard?

Ans. £199 3s. 4d.

Ans. £292 8s.

- N. B. The following questions are left without any answers, that the Scholar may operate and prove each question.
 - 19. What will 11 yards of flannel, at 2s. 6d. per yard come to?

 OPERATION. PROOF

20. What will 13lb. of cotton cost at 3s. 4d. per 15. ?.

21. What will 183 yards of ribbon come to at 8d. per yard?

SCHOLAR'S ARITHMETIC

SECTION III.

RULES OCCASIONALLY USEFUL TO MEN IN PARTICULAR CALLINGS AND PURSUITS OF LIFE.

1. 1. 1. 1.

1. INVOLUTION.

Involution, or the raising of powers, is the multiplying of any given number into itself continually, a certain number of times. The quantities in this way produced, are called powers of the given number. Thus,

4×4= 16 is the second power or square of 4.

4×4×4= 64 is the 3d power, or cube of 4.

4×4×4=258 is the 4th power or, bideadrate of 4.

The given number, (4) is called the first power; and the small figure, which points out the order of the power, is called the *Index* or the *Exponent*.

8 2. EVOLUTION

Evolution, or the extraction of roots, is the operation by which we

find any root of any given number.

The root is a number whose continual metaplication into itself produces the power, and is denominated the square, cube, biquadrate, or 2d, 3d, 4th, root, &c. accordingly as it is, when raised to the 2d, 3d, 4th, &c power, equal to that power. Thus, 4 is the square root of 16, because 4×4=16. 4 also is the cube root of 64, because 4×4×4=64; and 3 is the square root of 9, and 12 is the square root of 144, and the cube root of 1728, because 12×12×12=1728, and so on.

To every number there is a root, although there are numbers, the precise roots of which can never be obtained. But by the help of decimals, we can approximate towards those roots, to any necessary degree of exactness. Such roots are called Surd Roots, in distinction from those perfectly accurate, which are called Rational Roots.

The square root is denoted by this character \checkmark placed before the power; the other roots by the same character, with the index of the root placed over it. Thus the square root of 16 is expressed 16, and the cube root

of 27 is \$\frac{7}{27}, &c.

When the power is expressed by several numbers, with the sign + or between them, a line is drawn from the top of the sign over all the parts of it; thus the second power of 21-5 is $\sqrt{21-5}$, and the 3d power of むた えたがわ エモデ 56+8 is $\sqrt{56+8}$, &c.

The second, third, fourth and fifth powers of the nine digits may be seen STORY OF BUILDING

in the following

TABLE.

Roots	or 1st Powers	1	2	3	4	5	6	7	8	9
Squares	or 2d Powers	1	4	9	16,	25	36	49	- 64	81
	or 8d Powers						216	343	512	729
Biquadrates	or 4th Powers	1	16	81	256	625	1296	2401	4096	6561
Sursolids	or 5th Powers	1	32	243	1024	3125	7776	16807	32768	59049

The first of the second of the second **3. EXTRACTION OF THE SQUARE ROOT.**

To extract the square root of any number, is to find another number which multiplied by or into itself, would produce the given number; and after the root is found, such a multiplication is a proof of the work.

RULE.

1. "Distinguish the given number into periods of two figures each, by putting a point over the place of units, another over the place of hundreds, and so on, which points show the number of figures the root will consist of.

2. "Find the greatest square number in the first, or left hand period, place the root of it at the right hand of the given number, (after the manner of a quotient in division) for the first figure of the root, and the square number, under the period, and subtract it therefrom, and to the remainder bring down the next period for a dividend.

3. " Place the double of the root, already found, on the left hand of the

dividend for a divisor.

4. "Seek how often the divisor is contained in the dividend, (except the right hand figure) and place the answer in the root for the second figure of it, and likewise on the right hand of the divisor; multiply the divisor with the figure last annexed by the figure last placed in the root, and subtract the product from the dividend; to the remainder join the next period for uew dividend.

5. "Double the figures already found in the root for a new divisor, (or bring down your last divisor for a new one, doubling the right hand figure of it) and from these find the u-xt figure in the root, as last directed, and continue the operation in the same manner till you have brought down all the periods."

"Note 1. If, when the given power is pointed off as the power requires, the left hand period should be deficient, it must nevertheless stand

as the first period."

"Note 2. If there be decimals in the given number it must be pointed both ways from the place of units; If, when there are integers, the first period in the decimals be deficient, it may be completed by annexing so many cyphers as the power requires: And the root must be made to consist of so many whole numbers and decimals as there are periods belonging to each; and when the periods belonging to the given number are exhausted, the operation may be continued at pleasure by annexing cyphers."

EYAMPLES.

1. What is the square root of 729?

4	7 2 9(2'	the	100
	329 3 2 9	•	
. (000		
	800 7. 27 27		
	189 54		•
	729		•

The given number being distinguished into periods, I seek the greatest square number in the left hand period (7) which is 4, of which the root (2) being placed to the right hand of the given number, after the manner of a quotient, and the square number (4) subtracted from the period (7) to the remainder (3) I bring down the next period (29) making for a dividend, 329. Then the double of the root (4) being placed to the left hand for a divisor, I say how often 4 in 32? (excepting 9 the right hand figure) the answer is 7, which I place in the root for the second figure of it, and also to the right hand of the divisor; then multiplying the divisor thus increased by the figure (7) last obtained in the root, I place the

product underneath the dividend, and subtract it therefrom, and the work is done.

DEMONSTRATION

Of the reason and nature of the various steps in the extraction of the SQUARE ROOT.

The superficial content of any thing, that is the number of square feet, yards or inches, &c. contained in the surface of a thing, as of a table or floor, a picture, a field, &c. is found by multiplying the length into the breadth. If the length and breadth be equal, it is a square, then the measure of one of the sides as of a room, is the root, of which the superficial content in the floor of that room is the second power. So that having the superficial contents of the floor of a square room, if we extract the square root, we shall have the length of one side of that room. On the other hand, having the length of one side of a square room, if we multiply that number into itself, that is, raise it to the second power, we shall then have the superficial contents of the floor of that room.

The extraction of the square root therefore has this operation on numbers, to arrange the numbers of which we extract the root into a square

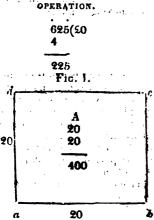
form. As if a man should have 625 yards of carpeting 1 yard wide, if he extract the square root of that number (625) he will then have the length of one side of a square room, the floor of which, 625 yards will be just sufficient to cover.

To proceed then to the demonstration.

EXAMPLE 2. Supposing a man has 625 yards of carpeting, 1 yard wide, what will be the length of one side of a square room, the floor of which

his carpeting will cover.

The first step is to point off the number into periods of two figures each. This determines the number of figures of which the root will consist, and is done on this principle, that the product of any two numbers can have at most but so many places of figures as there are places in both the factors, and at least but one less, of which any person may satisfy himself at pleasure.



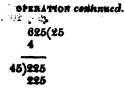
The number being pointed off as the rule directs, we find we have two periods, consequently the root will consist of two figures. The greatest square number in the left hand period (6) is 4, of which two is the root, therefore, 2 is the first figure of the root, and as it is certain we have one figure more to find in the root, we may for the present supply the place of that figure by a cypher (20) then 20 will express the just value of that part of the root now obtained. must be remembered, that a root is the side of a square of equal sides. Let us then form a square. A, Fig. I. each side of which shall be supposed 20 yards. Now the side a b of this square or either of the sides, shews the root 20, which we have obtained.

To proceed then by the rule "Place the square number underneath the period, subtract, and to the remainder bring down the next period."—Now the square number (4) is the superficial contents of the square A made evident thus—each side of the square A measures 20 yards, which number multiplied into itself, produces 400, the superficial contents of the square A, also the square number, or the square of the figure 2 already found in the root, is 4, which placed under the period (6) as it falls in the place of hundreds, is in reality 400, as might be seen also by filling the places to the right hand with cyphers, then 4 subtracted from 6 and to the remainder (2) the next period (25) being brought down, it is plain, the sum 625 has been diminished by the reduction of 400, a number equal to the superficial contents of the square A.

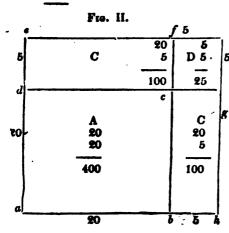
Hence Fig. I. exhibits the exact progress of the operation. By the operation 400 yards of the carpeting have been disposed of, and by the

figure is seen the displication made of them.

Now the square A is to be enlarged by the addition of the 225 yards which remain, and this addition must be so made that the figure at the same time shall continue to be a complete and perfect square. If the addition be made to one side only, the figure would lose its square form, it must be made to two sides; for this reason the rule directs, "place the double of the root already found on the left hand of the dividend for a divisor." The double of the root is just equal to two sides be and e d of the square, A, as may be set in by what follows

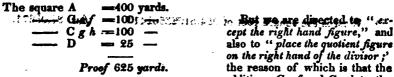


The double of the root is 4, which placed for a divisor in place of tens (for it must be remembered that the next figure in the root is to be placed before it) is in reality 40, equal to the sides $b \in$ (20) and c d (20) of the square A.



Again, by the rule, "seek how often the divisor is contained in the dividend (except the right hand figure) and place the answer in the root, for the second figure of it, and on the right hand of the divisor."

Now if the sides b c and c d of the square A Fig. II. is the length to which the remainder 225 yds. are to be added, and the divisor (4 tens) is the sum of these two sides, it is then evident that 225 divided by the length of the two sides, that is by the divisor (4 tens) will give the breadth of this new addition of the 225 yards to the sides b c and c d of the square A.



cept the right hand figure," and also to " place the quotient figure on the right hand of the divisor; the reason of which is that the addition, $C \in f$ and $C \in f$ to the

sides b c and c d of the square, A, do not leave the figure a complete square, but there is a deficiency D, at the corner.—Therefore in dividing the right hand figure is excepted, to leave something of the dividend, for this deficiency; and as the deficiency D, is limited by the additions C e f and Cgh, and as the quotient figure (5) is the width of these additions, consequently equal to one side of the square D; therefore the quotient figure (5) placed to the right hand of the divisor (4 tens) and multiplied into itself, gives the contents of the square D, and the 4 tens-to the sum of the sides, bc and cd of the addition of Cef and Cgh, multiplied by the quotient figure (5) the width of those additions give the contents $C \circ f$ and Cg h, which together subtracted from the dividend, and there being no remainder, shew that the 225 yards are disposed in these new additions C e f. Cg h, and D, and the figure is seen to be continued a complete square.

Consequently, Fig. II. shews the dimensions of a square room, 25 yards on a side, the floor of which 625 yards of carpeting, 1 yard wide will be sufficient to cover.

The Proof is seen by adding together the different parts of the figure. Such are the principles on which the operation of extracting the aquare rout is grounded.

3. What 19342656?	is the square root Ans. 3216	i. 43264 ?	is the square .	root of 20 8.
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SUPPLEMENT TO THE SQUARE ROOT.

QUESTIONS.

- 1. What is to be understood by a root? A power? The second, third and fourth powers?
- 2. What is the Index, or Exponent?
- 3. What is it to extract the Square Root?
- 4. Why is the given sum pointed into periods of two figures each !
- 5. In the operation, having found the first figure in the root, why do we subtract the square number, that is, the square of that figure from the period in which it was taken?
- 6. Why do we double the root for a divisor?
- 7. In dividing why do we except the right hand tigure of the dividend?
- 8. Why do we place the quotient figure in the root, and also to the right hand of the divisor?
- 9. If there be decimals in the given number how must it be pointed?
- 10. How is the operation of extracting the Square Root proved?

EXERCISES IN THE SQUARE ROOT.

27. 12p. the second, 2 acres, 2r. 15p. the third, 1 acre, 1r. 14p. in exchange for which the heritors agree to give him a square field equal to all the three. Sought the side of the square?

Ans. 39 poles.

\$. A general has an army of 4096 men; how many must be place in rank and file to form them into a square?

Ans. 64

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3. There is a circle whose diameter is 4 inches, what is the diameter of a circle 4 times as large?

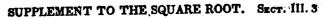
Note. Square the given dameter, multiple, this, against by the given proportion, and the square root of the product will be the diameter required. pot the same in all similar cases. P. STERRIGHT A. If the circle of the required diameter were to be

less than the circle of the given diameter, by a certain proportion, then the square of the given diameter must have been divided by that prohave been portion.

4. There are two circular pands in a gentleman's pleasure ground; the diameter of the less is 100 feet, and the greater is three times as large.-What is its diameter? Ans. 173,2+

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5. If the diameter of a circle be 12 Inches, what will be the diameter another circle half so large? Ans. 8.48



6. A wall is 36 feet high, and a ditch before it is 27 feet wide; what is the length of a ladder, that will reach to the top of the wall from the opposite side of the ditch?

Ans. 45 feet.

Note. A Figure of three

* 68

Note. A Figure of three sides, like that formed by the wall, the ditch and the ladder, is called a right angled triangle, of which the square of the hypothenuse, or slanting side, (the ladder) is equal to the sum of the squares of the two other sides, that is, the height of the wall and the width of the ditch.

(ii) The man at the control of the property of the control of t

7. A line of 36 yards will exactly reach from the top of a fort to the opposite bank of a river, known to be 24 yards broad; the height of the wall is required?

Ans. 26,83+ yards.

If the diameter is a crule be Is Mahes, what will be the short of a clark half so large?

8. Glasgow is 44 miles west from Edinburgh; Peebles is exactly south from Edinburgh, and 49 miles in a straight line from Glasgow; what is the distance between Edinburgh and Peebles?

Ans. 21,5-miles

6 4. EXTRACTION OF THE CUBE ROOT.

To extract the Cube Root of any number is to find another number, which multiplied into its square shall produce the given number.

RULE.

1. "Separate the given number into periods of three figures each, by putting a point over the unit figure, and every third figure beyond the place of units.

2. "Find the greatest cube in the left hand period, and put its root in

the quotient.

3. "Subtract the cube thus found, Trom the said period, and to the re-

mainder bring down the next period, and call this the dividend.

4. "Multiply the square of the quotient by 300, calling it the triple square, and the quotient by 30, calling it the triple quotient, and the sum of these call the divisor.

5. "Seek how often the divisor may be had in the dividend, and place

the result in the quotient.

6. "Multiply the triple square by the last quotient figure, and write the product under the dividend; multiply the square of the last quotient figure by the triple quotient, and place this product under the last; under all, set the cube of the last quotient figure, and call their sum the subtrahend.

7. "Subtract the subtrahend from the dividend, and to the remainder oring down the next period for a new dividend, with which proceed as be

fore, and so on till the whole be finished.

Note. The same rule must be observed for continuing the operation, and pointing for decimals, as in the square root

1. What is the cube root of 373248?

373248(72 the ro	ing to the relation to the first the state of the state o
343	7×7×300=14700, the triple square.
	7×30 = 210 the triple quotient
Divisor 14910)30248	
	14910 the divisor.
29400	14700×2==29400
840	2×2×210= 840
8	2×2×2 = 8
20240	30248 the subtrahend.
30248	50245 the subtranena.
` 00000	

DEMONSTRATION

Of the reason and nature of the various steps in the operation of extracting the Cube Root.

Any solid body having six equal sides, and each of the sides an exact square is a Cube, and the measure in length of one of its sides is the root of that cube. For if the measure in feet of any one side of such a body be multiplied three times into itself, that is, raised to the third power, the product will be the number of solid feet the whole body contains.

And on the other hand, if the cube root of any number of feet be extracted, this root will be the length of one side of a cubic body, the whole

contents of which will be equal to such a number of feet.

Supposing a man has 13824 feet of timber, in distinct antiseparate blocks of one foot each; he wishes to know how large a solid body they will make when laid together, or what will be the length of one of the sides of that cubic body?

To know this, all that is necessary is to extract the cube root of that number, in doing which I propose to illustrate the operation.

13824(20 8 5824 Fig. 1, C 20 D B A 20 F 20 400 20

PERATION.

In this number, pointed off as the rule directs, there are two periods: of sourse there will be two figures in the root.

The greatest cube in the right hand period (13) is 8, of which 2 is the root, therefore 2 placed in the quotient is the first figure of the root, and as it is certain we have one figure more to find in the root, we may for the present supply the place of that one figure by a cypher (20) then 20 will express the true value of that part of the root now obtained. But it must be remembered, that the cube root is the length of one of the sides of the cubic body, whose length, breadth and thickness are equal. Let us then form a cube, Fig. 1, each side of which shall be supposed 20 feet; now the side A B of this cube, or either of the sides, shews the root (20) which we have obtained.

y or oligina in progression

1000 feet-the solld contents of the Cabe of the Cabe

The Rule next directs, subtract the cube thus found from the eaid period, and to the remainder bring down the next period, &c. Now this cube (8) is the solid contents of the figure we have in representation. Made evident thus-Each side of this figure is 20, which being raised to the 3d power, that is the length, breadth and thickness being multiplied into each other. gives the solid contents of that figure=8000 feet, and the cube of the root, (2) which we have obtained, is 8, which placed under the period from which it was taken as it falls in the place of thousands, is 8000, equal to the solid contents of the cube A B C D E F, which being subtracted from the given number of feet, leaves 5824 feet.

Hence, Fig. I. exhibits the exact progress of the operation. By the operation 8000 feet of the timber are disposed of, and the figure shews the disposition made of them, into a solid pile, which measures 20 feet on every side.

Now this figure or pile is to be enlarged by the addition of the 5824 feet, which remains, and this addition must be so made, that the figure or pile shall continue to be a complete cube, that is, have the measure of all its sides equal.

To do this the addition must be made equally to the three different

squares, or faces a, c and b.

The next step in the operation is, to find a divisor: and the proper divisor will be, the number of square feet contained in all the points of the

figure, to which the addition of the 5824 feet is to be made.

Hence we are directed to "multiply the square of the quotient by \$00," the object of which is to find the superficial contents of three faces a, c, b, to which the addition is now to be made. And that the square of the quotient, multiplied by 300 gives the superficial contents of the faces a, c, k is evident from what follows:

The triple square 1200—the superficial contents of the faces a, c, and b.

The two sides AB & AF of the face a, multiplied into each other, give the superficial content of a, and as the faces, a, c, and b, are all equal, therefore the content of face z, multiplied by 3, will give the contents of a, c, and b.

The triple square 1200 the superficial contents of the faces a, c, and b.

Here the quotient figure 2 is properly, two tens, for there is another figure to follow it in the root, and the square of 2, standing as units, is 4, but its true value is 20 (the side A B) of which the square is 400, we therefore lose two cyphers, and these two cyphers are annexed to the figure 3—Hence it appears that we square the quotient with a view to find the superficial content of the face or square a, we

multiply the square of the quotient by 3, to find the superficial contents of the three squares, a, c, and b, and two cyphers are annexed to the 3, because in the square of the quotient two cyphers were lost, the quotient requiring a cypher before it in order to express its true value, which would throw the quotient (2) into the place of tens, whereas now it stands in the place of units.

Now when the additions are made to the squares a, c, and b, there will evidently be a deficiency, along the whole length of the sides of the squares, between each of the additions, which must be supplied before the figure can be a complete sube: These deficiencies will be 3, as may be seen,

Tr I and

Therefore it is, that we are directed, "multiply the quotient by 30, calling

it the triple quotient."

The triple quotient is the sum of the three lines, or sides, against which are the deficiencies n n, all which meet at a point, night he centre of the figure. This is evident from what follows.

The deficiencies are three in number, they are the whole length of the sides, the length of each side is 20 feet,

gth of each side is Theresore 20 **2** quotient. 30

.

Triple quotient 60—to the length of 3 sides where are deficiencies to be filled.

Triple quotient 60 equal the length of 3 sides, &c.

Here as before, the quotient lacks a cypher to the right hand, to exhibit its true value; the quotient itself is the length of

one of the sides, where are the deficiencies; it is multiplied by 3 because there are 3 deficiencies, and a cypher is annexed to the 3 because it has been omitted in the quotient, which gives the same product, as if the true value of the quotient 20, had been multiplied by 3 alone.

We now have 1200 the triple square.

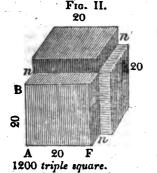
60 the triple quotient.

The sum of which, 1260 is the divisor, equal the number of square fact contained in all the points of the figure or pile, to which the addition of the 5824 feet is to be made.

OPERATION, continued. 13824(24 the root. 8

Divis. 1260)5824 the dividend.

960 64 5824 subtrahend.



4 last quotient figure.

This Figure in the root (4) shews the depth of the addition on every point where it is to be made to the pile or figure, represented, Fig. I.

Fig. II. exhibits the additions made to the squares a c b, by which they are covered or raised by a depth of 4 feet.

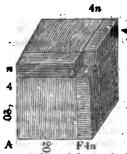
The next step in the operation is to find a subtrahend, which subtrahend is the number of solid feet contained in all the additions to the cube, by the last figure 4.

Therefore the rule directs, multiply the triple square by the last quotient figure.

The triple square it must be remembered, is the superficial contents of the faces a c and b, which multiplied by 4, the depth now added to these faces, or squares, gives the number of solid feet contained in the additions by the last quotient figure 4.

⁴⁸⁰⁰ feet, equal the addition made to the squares, or faces, a, c, b, of Fig. I a depth of 4 feet on each.

Fig. III.



Then, "Multiply the square of the last quotient figure by the triple quotient." This is to fill the deficiencies, n n n, Fig. II. Now these deficiencies are limited in length by the length of the sides (20) and the triple quotient is the sum of the length of the deficiencies. They are limited in width by the last quotient figure (4) the square of which gives the area or superficial contents at one end, which multiplied into their length, or the triple quotient, which is the same thing, gives the contents of those indictions 4n4, 4n, 4n, Fig. III.

60 triple quotient.

16 square of the last quotient.

360 :: 60

960 feet disposed in the deficiencies, between the additions to the squares a c b, Fig. III. exhibits these deficiencies, supplied 4n4, 4n, 4n, and discovers another deficiency where these approach together, of a corner wanting to make the figure a complete cube.

Fig. IV. 20 4n

16

Lastly, "Cube the last quotient figure." This is done to fill the deficiency, Fig. III. left at one corner, in filling up the other deficiencies, n.n. This corner is limited by those deficiencies on every side, which were 4 feet in breadth, consequently the square of 4 will be the solid content of the corner which in Fig. IV. e e e is seen filled.

Now the sum of these additions make the subtrahend, which subtract from the dividend and the work is done.

64 feet is the corner e e e, where the additions n n n, approach together.

Figure IV. Shews the pile which 13824 solid blocks of one foot each, would make when laid together. The root (24) shews the length of a side. Fig. I. shews the pile which would be formed by 8000 of those blocks, first laid together; Fig. II. Fig. III. and Fig. IV. shew the changes which the pile passes through in the addition of the remaining 5824 blocks or feet.

Proof. By adding the contents of the first fi ure, and the additions ex-

hibited in the other figures together.

Feet.

8000 Contents of Fig. I.

4800 addition to the faces or square a, c, and b, Fig. II.

960 addition to fill the deficiencies m, n, m, Fig. III.

64 addition at the corner, s, c, c, Fig. II where the additions

which fill the deficiencies n, n, n, approach together.

13824 Number of blocks or solid feet, all which are now disposed in Fig. IV. forming a pile or solid body of timber, 24 feet on a side.

Such it the demonstration of the reason and nature of the various steps in the operation of extracting the cube root. Proper views of the figures, and of those steps in the operation illustrated by them, will not generally be acquired without some diffigure or intention. Scholars more especially will meet with difficulty. For their assistance, small blocks might be formed of wood in imitation of the Figures, with their parts in different pieces. By the help of these, Masters, in most instances, would be able to lead their pupils into the right conceptions of those views, which are here given of the nature of this operation.

3. What is the cube root of 21024576?

Ans. 276.

The cube of the cube root of 21024576?

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SECT. III. 4. EXTRACTION OF THE CUBE ROOT.

5. What is the cube root of 84,604519 1 to the cube of it day 4,39.

6. What is the cube root of 2?

Ans. 1.25-

SUPPLEMENT TO THE CUBE ROOT.

QUESTIONS.

- 1. What is a Cube ?
- 2. What is understood by the cube root?
- 3. What is it to extract the cube root?
- 4. In the operation, having found the first figure of the root, why is the cube of it subtracted from the period in which it was taken?
- 5. Why is the square of the quotient multiplied by 300 ?
- 6. Why is the quotient multiplied Ly 30?
- 7. Why do we add the triple square and triple quotient together, and the sum of them call the divisor?
- 8. To find the subtrahend, why do we multiply the triple square by the last quotient figure? the square of the last quotient figure by the triple quotient? Why do we cube the quotient figure? Why do these sums added, make the subtrahend?
- 9. How is the operation proved?

EXERCISES IN THE CUBE ROOT.

1. If a bullet 6 inches in diameter weigh 32lb. what will a bullet of the same metal weigh whose diameter is 3 inches? Ans. 4lb.

NOTE. " The solid contents of similar figto each other, as the cubes of their similar «ides, or diameters."

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2. What is the side of a cubical mound, equal to one 268 feet long, 216 broad and 48 feet high? Ans. 144 feet.

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EXCURN NOW TO THE GRAD RANCE

3. There is a cubical vessel whose side is two feet; I demand the side of a vessel which shall contain three times as much?

Ans. 2 feet tru inches and 1 nearly.

Noze. Cube the given side, multiply it by the given proportion, and the cube root of the product will be the side sought.

4 5. FELLOWSHIP.

more restriction of the contract of the contra

FELLOWSHIP is a rule by which merchants and others, trading in partnership, compute their particular shares of the gain or loss, in proportion to their stock and the time of its continuance in trade.

It is of two kinds, Single and Double.

SINGLE FELLOWSHIP,

Is when the stocks are employed equal times.

RULE.

As the whole sum of the stock is to the whole gain or loss, so is each man's particular stock to his particular share of the gain or loss.

Proof. Add all the shares of the gain or less together; and if the work be right, the sum will be equal to the whole gain or loss.

EXAMPLES.

1. Two merchants, A and B, make a joint stock of 200 dollars; A puts in 75 dollars, and B 125 dollars; they trade and gain 50 dollars; what is each man's share of the gain?

OPERATION.

Dolls. Dolls.	Doll s.	
As 200 : 50 ::	75 As 2	00 : 50 : : 125
. 75		125
250		250
350		100
D. c	ts.	50
200)3750(18,7	5 A's share.	D. cts.
200	bine 6 22	00)6250(81,25 B's share.
		600
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1400	•	£00
		400
1000	18,75 A's share.	
1000	31,25 B's share.	1000
		1000
•	50,00 Proof.	

2 Divide the number 360 into 4 such parts, which shall be to each other as 3, 4, 5, and 6.

3. A man died leaving 3 sons, to whom he bequeathed his estate in the following manner, viz. to the eldest he gave 184 dollars, to the second 155 dollars, and to the third 96 dollars; but when his debts were paid, there were but 184 dollars left; What is each one's proportion of his estate?

Ans. 77,829 65,563 Shares

4. A and B companied A put in £45, and took & of the gain; What did B put in?

Ans. £30.

DOUBLE FELLOWSHIP.

DOUBLE FELLOWSHIP, or Fellowship with time, is when the stocks of partners are continued unequal times.

RULE.

Multiply each man's stock by the time it was continued in trade. Then, As the whole sum of the products is to the whole gain or loss, so is each man's particular product to his particular share of the loss or gain.

EXAMPLES.

1. A, B, and C, entered into partnership; A put in 85 dollars for 8 months; B put in 60 dollars for 10 months; and C put in 120 dollars for 3 months; by misfortune they lost 41 dollars: What must each man sustain of the loss?

OPERATION

	OLTUNITO	20
85 60	120	680 A's product.
810	3	600 B's product.
·		360 C's product.
680 600	360	
As 1640 : 41 :: 680		1640
680		As 1640 : 41 :: 600 600
680		,
2720		164 0)2460 0(15 B's loss.
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164 0)1476 0(9 C's loss.		15 B's loss.
1476		9 C's loss.
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0000		11 Proof.

2. A, R, and C, trade together; A, at first put in 480 dollars for 8 months, then put in 200 dollars more and continued the whole in trade 8 months longer, at the end of which he took out his whole stock; B put in 500 dollars for 9 months, then took out \$583,333 and continued the rest in trade 3 months; C put in \$366,666 for ten months, then put in 250 dollars mere, and continued the whole in trade 6 months longer. At the end of their partnership they had cleared 1000 dollars; what is each man's thare of the gain?

Ass. \$378,827 A's share. 320,452 B's share. 300,721 C's share.

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SUPPLEMENT TO FELLOWSHIP.

QUESTIONS.

- 1. What is Fellowship?
- 2. Of how many kinds is Fellowship?
- 3. What is Single Fellowship?
- 4. What is the rule for operating in Single Fellowship?
- 5. What is Double Fellowship?
- 6. What is the rule for operating in Double Fellowship?
 - 7. How is Fellowship proved?

EXERCISES IN FELLOWSHIP.

A, B, and C, held a pasture in common, for which they pay £20 per annum. In this posture, A had 40 oxem for 76 days; B had 36 oxem for 50 days, and C had 50 oxem for 90 days. I demand what part each of these tenants ought to pay of the £20.

£ s. d. q.

Ans. 6 10 2 1344 A's part.
3 17 1 03513 B's part.
9 12 8 24154 C's part.

(i)

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6. BARTER.

BARTER is the exchanging of one commodity for another, and teaches merchants so to proportion their quantities, that neither shall sustain loss.

Paoor. By changing the order of the question.

RULE.

1. When the quantity of one commodity is given with its value or the value of its integer, as also the value of the integer of some other commodity to be exchanged for it, to find the quantity of this commodity:—Find the value of the commodity of which the quantity is given, then find how much of the other commodity at the rate proposed may be had for that sum.

2. If the quantities of both commodities be given, and it should be required to find how much of some other commodity, or how much money should be given for the inequality of their values: Find the separate value of the two given commodities, subtract the less from the greater, and the remainder will be

the balance, or value of the other commodity.

3. If one commodity is rated above the ready money price, to find the beartering price of the other: Say, as the ready money price of the one is to the bartering price, so is that of the other to its bartering price.

EXAMPLES.

1. How much coffee at 25 cents per lb. can I have for 56lb. of tea at 43 cents per lb.?

OPERATION.

5 6 lb. of tea.

,4 3 per lb

2 5)1 2 8

2. I have 760 gallons of molasses, at 37 cents 5 mills per gallon, which I would exchange for 66 cwt. 2 qr. of cheese at 4 dollars per cwt. Must I pay or receive money, and how much?

Ans. must receive \$19.

3. A and B barter; A has 150 bushels of wheat at 5:. 9d. per bushel, for which B gives 65 bushels of barley, worth %2. 10d. per bushel, and the balance in oats at 2s. 1d. per bushel; what quantity of oats asset A receive from B?

Ans. 3254 bushels.

4. A has lines cloth worth 20d. an ell, ready money; but in barter he would have two shillings; B has broad cloth worth 14s. 6d. per yard, ready money; at what price ought the broad cloth to be rated in barter?

Ans. 17s. 4d. 3q. 4per yard.

SUPPLEMENT TO BARTER.

Other and the second the second secon

- 1. What is Barter?
- 2. When and how does this rule become useful to merchants?
- 3. When a given quantity of one commodity is bartered for some other commodity, how is the quantity that will be required of this last commodity found?
- 4. If the quantity of both commodities be given, and it be required to know how much of some other commodity, or how much money must be given for the inequality, what is the method of procedure?
- 5. If one commodity be rated above the money price, how do you proceed to find the bartering price of the other commodity?
- 6. How is Barter proved?

EXERCISES.

1. A and B bartered; A had 41 cwt. of hops, 30s. per cwt. for which B gave him £20 in money, and the rest in runes, at 5d per lb. I demand how many prunes B gave A, besides the £20.

Ans. 17C. 3grs. 4lb.

(a) Street of the following set that the positive west word following of the of mounts to add only the graph armag support so a preparation of a contract of the contract of the property of the contract o

the first control of the season of the control and A the

2. How much wine at \$1,28 per gallon, must I have for 26cwt. 2qr 14lb. of raisins, at \$2,444 per cwt.?

Ans. 196gal. 1qt. 14pt.

4 7. LOSS AND GAIN.

"Loss and Gain is a rule which enables merchants to estimate the profit or loss in buying and selling goods; also to raise or fall the price of them, so as to gain or lose so much per cent."

CASE I.

To know what is gained or lost per cent. First, find what the gain or loss is by known ction, then as the prize it cost is to the gain or loss, so is \$100 (or £100) to the gain or loss per cent.

min i i i i

EXAMPLES.

1. If I buy candles at 16 certs 7
mills per lb. and sell them at 20 cts.
per lb. what shall gain per cent or in laying out 100 dollars?

EXAMPLES.

2. Bought indigo at \$1,20 per lb. and sold the same at 90 cents per lb. what was lost per cent?

In laying out 100 dollars?

I sell at ,20 per lb. Bought at ,167 per lb.

I gain ,033 per lb.

Then as ,167: ,0 3 3:: 100

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D. cts.

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1 6 7

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3. Bought 37 gallons of Brandy at \$1,10 per gallon, and sold it for \$40; what was gained or lost per cent?

Ans. \$1,719 loss

4. Bought hats at 4s. a piece, and sold them again at 4s. 9d.; what is the profit in laying out £100?

Ans. £18,15s.

4, 13 F.

. CASE II.

To know how a commodity must be sold to gain or lose so much per cent; As 100 dollars (or £100) is to the price; so is 100 dollars (or £100) with the profit added or the loss subtracted to the gaining or losing price.

EXAMPLES.

- 1. If I buy wheat at \$1,25 per bushel, how must I sell it to gain 1,5 per cent?
 - l, 2. If a barrel of rum cost 15 dollars, how must it be sold to lose 10 per cent?

 .dns. \$13,50.

3. If 1905. of steel cost £7, how must I call it per Bi to gain 15} per cont?

SUPPLEMENT TO LOSS AND GAIN.

QUESTIONS.

1. What is Loss and Gain?

₹.

- 2. Having the price at which goods are bought and sold, how is the loss or gain estimated?
- 3. To know how much a commodity must be valued at to gain or lose so much per cent, what is the method of procedure?
- 4. How may questions in Loss and Gain be proved?

 EXERCISES.
- 1. A draper bought 100 yards of broadcloth for £56. I demand how he must sell it per vard to gain £15 in laying out £100?

 Ans. 12s. 12s. 12s. 12s.

2. Bought 30 hogsheads of molesses at \$600; paid in daties \$20,66; for freight \$40,78; for porterage \$6,05, and for insurance, \$30,84; If I sell it at \$26 per hogshead, how much shall I gain per cent?

Ans. \$11,695.

6 C. DUODECIMALS:

OR, CROSS MULTIPLICATION.

This rule is particularly woful to Workmen and Artificers in casting up the contents of their work.

Dimensions are taken in feet, inches and parts. Inches and parts are sometimes called primes (') seconds (") thirds ("") and fourths ("")

TABLE. By this rule also may be calcula-

12 Fourths make 1 Third. ted the solid contents of bodies, may-

12 Thirds - - - 1 Second. A ting the measures of their different

12 Seconds - - 1 digh or prime. . sides, analyis very useful therefore in 12 Inches or Pr. 1. Foot. say given measuring woodhire and in the team to 1. 3 . 1 . 3 . RULE.

1. Under the multiplicand write the corresponding denominations of the multiplier.

2 Multiply each term in the multiplicand, beginning at the lowest, by the feet in the multiplier, and write the result of each under its respective term, observing to carry an unit for every 12, from each lower denomination to its superior.

3. In the same manner multiply the multiplicand, by the inches in the multiplier, and write the result of each term in the multiplicand, thus mul-

tiplied, one place to the right hand in the product.

4. Proceed in the same manner with the other parts in the multiplier. swhich if seconds, write the result two places to the right hand; if thirds, three places, &c. and their sum will be the answer required.

The more easily to comprehend the rule-Note. Feet multiplied by feet

EXAMPLES.

seconds. The argument of the factor

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		<i>3</i>	

Prod. 11 7 9 116

give feet—Feet multiplied by inches give inches-Feet multiplied by seconds give seconds-Inches multiplied by inches give seconds—In-ches multiplied by seconds give # 1. Multiply 7 feet, 3 inches, 2 thirds—Seconds multiplied by se-seconds, by 1 foot, 7 inches and 3 seconds give seconds of 15 per 3 3 ्रेश रहे वर्षांक केरान रहा र १४० वर्ष वर्ष

Here I multiply the 7f. 3in. 2" by the 1f. in the multiplier, which gives seconds, inches and feet.

Next I multiply the same 7f. 3in. 2" by the 7in. saying 7 times 2 is 14 which is once 12 and 2 over, which (2) I set down one place to the right hand that is in the place of thirds and carry one to the next place and procced in the same manner with the other terms. Lastly, I multiply the multiplicand by the 3" saying 3 times

2 are 6, which I set down two places to the right hand and so proceed with the other terms of the multiplicand. The sum of all the products is the answer.

25 6 Frod.

6. Multiply 9f. 8in. 7" by 12f. 8in. 9" 3in. 10" Prod. 55f. 2in. 9" 3" 9" Prod. 119f. 8' 2" 10" 10""

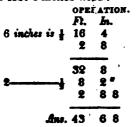
7. Most much segod in a load which measures 10f in length; 3f 9in in width, and 4f. 8in in beight; and how much will it cost at \$1,33 per cord? And I cord and 47 solid feet over-it will cost \$1 81cts. 8m. Ry or a read

A MONTH OF

Or, we may multiply by the feet as already directed, and for the inches, take such parts of the multiplicand, &c. as the inches are aliquot or even parts of a foot as done in the rule of Practice.

8. How many square feet in a board of 16 feet 4 inches in length, and

2 feet 8 inches wide?



Here in the first place I multiply the 16st. 4in. by the feet (2) of the multiplier; the inches (8) not being an even part of a foot, I take such as are an even part; thus, 6in. is half n foot, therefore divide the multiplicand by 2 for 6 inches, and that quotient by 3 (2in. is 1 of 6in.) for 2 inches, all which being added give the product of 16 feet 4 inches, multiplied by 2 feet 8 inches.

9. Another board is 18 feet 9 inches in length, and 2 feet 6 inches wide, how many square feet does it contain?

Ans. 46ft. 10in. 6"
By Pracesce.

By Duodecimals.

10. There is a stock of 15 boards, 12 feet 8 inches in length, and 13 inches wide; how many feet of boards does the stock contain?

Ass. 205ft. 10in.

By Practice.

By Duodecimals.

SUPPLEMENT TO DUODECIMALS.

QUESTIONS.

- 1. Of whet use are Duodecimals? To whom more specially are they useful?
- 2. In what are dimensions taken?
- 3. How do you proceed in the multiplication of duodecimals?
- '4. For what number do you carry?
- 5. What do you observe in regard to seiting down the product different from what is common in the multiplication of other numbers?
- 6. Of what term is the product which arises from the multiplication of feet by inches? feet by seconds? inches by inches? inches by seconds?
- 7. In what way can the operation be varied?

EXERCISES.

1. Multiply 76 feet 3 inches 9
seconds by 84 feet 7 inches 11 seconds.

2. What is the product of 371ft.
2in. 6 seconds, multiplied by 181ft.
1in. 9" ?

ne. 67242ft. 10in. 1" 4" 6" OPERATION. F. I. 6 inches is 1)76 3 9 84 7 11 76× 4-304 0 76× 8=608 0 0 $3 \times 84 = 21 0$ 9x34 = 53038 1 10 L 14) 61) 9 🖚 \$\display \text{3} \display \display \text{3} \display \d ้ง**10% aO 11 S**ections (คือ # กลุ่มน้ำจากการจุด กลุ่ง #กล้า โด 10 * 1 - 7 - 25.

Prod. 6460 7 1 8 3

3. How many square feet in a stock of 12 boards, 17st. 7' long, and 1st. 5in. wide? Aus. 298st. 11'

4. How many cubic feet of wood in a load 6ft. 7' long, 3ft. 5' high and 3ft. 8' wide? Ana. 82ft. 5' 8" 4"

or built gar asye to

The dimensions of wainscotting, paving, plastering and painting are taken in seet and inches, and the contents given in yards.

PAINTERS AND JOINERS

To find the dimensions of their work, take a line and apply one end of it to any comer of the room, then measure the room, going into every corner with the line, till you come to the place where you hist began; then see how many feet and inches the string contains; this call the Compuss or Round, which multiplied into the height of the room and the product divided by 9, the quesient will be the contents in yards.

EXAMPLES.

be 12ft. 4in. and the compass 8-1ft. 11in. How many square yards does it the height 7ft. 6'. What is the concontain f. ... Inc. 116Y. 3ft. 3'8" tent in square yards?

to on the standard of the self of the following self of the self o

1. If the height of a room painted 2. There is a room wainscotted, the compass of which is 47ft. 3' and

manger specific in the post of displaying

Transport in the first program of the first program of the

July 1974 to be a given at a tradition of the same at the rich of marked of the first of the second of the second of the second of the second of

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GLAZIERS WORK BY THE FOOT.

To find the dimensions of their work, multiply the height of windows by their breadth.

EXAMPLE.

There is a house with 4 tiers of windows, and 4 windows in a tier; the height of the first tier is 6ft. 8'; of the second set. 8'; of the third 4ft. 6'; and of the fourth 3ft. 10'; and the breadth of each is 3ft. 5'- What will the glazing come to at 19 cents per foot?

§ 9. ALLIGATION.

ALLIGATION is the method of mixing two or more simples of different qualities, so that the composition may be of a mean or middle quality. It is of two kinds, Medial and Alternate.

ALLIGATION MEDIAL.

Alligation Medial is when the quantities and prices of several things are given to find the mean price of the mixture compounded of those things.

RULE.

As the sum of the quantities or whole composition is to their total value, so is any part of the composition to its value or mean price.

EXAMPLES.

1. A farmer mingled 19 bushels of wheat at 6s. per bushel, and 40 bushels of rye at 4s. per bushel, and 12 bushels of barley at 3s. per bushel together. I demand what a bushel of this mixture is worth?

gemer. I demand what	a pusher or this mix	ture is worth :
Bush. 19 Wheat at, 40 Rye — 12 Barley — sum of the — simples 71 Total value.	6 is 5 14 4—8 3—1 16	Bush. £. s. Bush. As 71 : 15 10 :: 1 20 71)310(4s. 4d. 141q. Ass.
2. A Refiner having 510 of 80z. fine, 101b. of 70z. 60z. fine, would melt all twhat fineness 11b. of this 1 Ant. 60z. 13p	fine, and 151b. of ogether; I demand	
e e e e e e e e e e e e e e e e e e e		28
The second of th	en e)112(1q. 71
1 4		

ALLIGATION ALTERNATE,

Is the method of finding what quantity of any number of simples, whose rates are given will compose a mixture of a given rate, it is therefore, the reverse of Alligation Medial, and may be proved by it.

RULE.

- 1. Write the prices of the simples, the least uppermost, &c. in a column under each other.
- 2. Connect with a continued line the price of each simple or ingredient, which is less than that of the compound, with one or any number of those that are greater than the compound, and each greater rate or price with one or any number of those that are less.

3. Write the difference between the mean rate or price and that of each f the simples opposite to the rates with which they are connected.

4. Then if only one difference stand against any rate it will be the quantity belonging to that rate, but if there be several, their sum will be the quantity.

Note. Questions in this rule admit of as many various answers as there are various ways of connecting the rates of the ingredients together.

EXAMPLES.

A goldsmith would mix gold of 18 carats fine with some of 16, 19, 22, and 24 carats fine, so that the compound may be 20 carats fine; what quantity of each must be take?

2. A druggist had several sorts of tea, viz. one sort at 12s. per lb. another sort at 11s a third at 9s. and a fourth at 8s. per lb. I demand how much of each sort he must mix together, that the whole quantity may be afforded at 10s. per lb.

No. These seven answers arise from as many different ways of linking the lates of the simples together.

CASE 2.

When the rates of all the ingredients, the quantity of but one of them, and the mean rate of the whole mixture are given to find the several quantities of the rest, in proportion to the given quantity; take the difference between each price and the mean rate as before. Then say,

As the difference of that simple whose quantity is given,

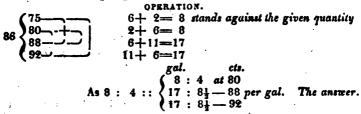
Is to the given quantity,

So is the rest of the differences severally;

To the several quantities required.

EXAMPLES.

1. How much wine, at 80 cents, at 68, and 92 cents per gallon must be mixed with four gallons of wine at 75 cents per gallon, so that the mixture may be worth 86 cents per gallon?



2. A man being determined to mix 10 bushels of wheat at 4s. per bushel, with rye at 3s. with barley at 2s. and with oats at 1s. per bushel; I demand how much rye, barley and oats must be mixed with the 10 bushels of wheat that the whole may be sold at 28d. per bushel?

CASE 3.

When the rates of the several ingredients, the quantity to be compounded, and the mean rate of the whole mixture are given, to find how much of each sort will make up the quantity, find the differences between the mean rate, &c. as in Case 1. Then,

As the sum of the quantities or differences, Is to the given quantity or whole composition; So is the difference of each rate, To the required quantity of each rate.

EXAMPLES.

1. How many gallons of water, of no value, must be mixed with brandy, at one dollar twenty cents per gallon, so as to fill a vessel of 75 gallons that may be afforded at 92 cents per gallon?

Gal. Gal. Gal. Gal. 92 { 0-28 Gal. Gal. { 28 : 17½ of Water. } 92 { 1,20-92 As 120 : 75 :: } 92 : 57½ - Brandy.

Sum 120
75 given quantity.

2. Suppose I have 4 sorts of currents of 8d. 12d. 18d. and 22d. per lb. of which I would mix 120lb. and so much of each sort as to sell them at 16d. per lb. how much of each must I take?

3. A Grocer has currents of 4d. 6d. 9d. and 11d. per lb. and he would make a mixture of 240lb. so that it might be afforded at 8d. per lb. how much of each sort must be take?

SUPPLEMENT TO ALLIGATION.

QUESTIONS.

- 1. What is Alligation?
- 2. Of how many kinds is Alligation?
- 3. What is Alligation MEDIAL ?
- 4. What is the rule for operating?
- 5. What is Alligation ALTERNATE ?
- 6. When a number of ingredients of different prices are mixed together, How do we proceed to find the mean price of the compound or
- 7. When one of the ingredients is limited to a certain quantity, what is the method of procedure?
- 8. When the whole composition is limited to a certain quantity, how do you proceed !
- 9. How is Alligation proved?

THE RESERVE OF THE PERCENTS.

1. A Grocer would mix three sorts of sugar together; one sort of gold; some of 24 carats fine, some at 10d. per lb. another at 7d. and another at 6d how much of each port must he take that the mixture mit be sold for 8d. per lb. t

Liter Entropy provides

Ans. 31b. at 10d. 21b. at 7d. 4 21b. at 6d. --

2. A Goldsmith has several sorts of 22 and some of 18 carats fine, and he would have compounded of these sorts the quantity of 6002. of 20 carats fine; I defnand how much of each sort must he have?

Ans. 1202. 24 carats fine, 12 at 22 earats fine, and 36 at 18 car. fine.

6 10. POSITION.

POSITION is a rule which by false or supposed numbers, taken at pleasure, discovers the true one required. It is of two kinds, Single and Double.

SINGLE POSITION.

Is the working of one supposed number; as if it were the true one to find the true number. 化抗性抗性 医二氯甲基甲基

RULE.

1 Take any number and perform the same operations with it as are described to be performed in the question.

2. Then say as the sum of the errors is to the given sum, so is the supposed number to the true-one required. As a second with the second William

Proof. Add the several parts of the sum together, and if it agree with the sum, it is right. e sit is the Arrangi telegraphy. Jan : 3 25471

EXAMPLES.

1. Two men, A and B, having found a bag of money, disputed who should have it. A said the half, third, and one fourth of the money made 180 dollars, and if B could tell how much was in it, he should have it all, otherwise he should have nothing; I demand how much was in the bog! OPERATION.

Suppose 60 dollars.

As 65 : 130 ; 60 was to 160 a said but the succession

The half 30

secretary to see and reson to 65)7800(120 dolla. the answer.

- third 20 - fourth 15

> 南 株式 は 5元 130

At to all the make the

130

000

2 A B and C talking of their ages, B said his age was once and a half the age of A; and C said his age was twice and one tenth the age of both, and that the sum of their ages was 93; what was the age of each?

A's 12, B's 18, C's 63 years

3. A person having spent 4 and 4 of his money, had £264 left, what had he at first?

4. Seven eighths of a certain number exceeds four fifths by 6; what is that number? Aur. 80.

DOUBLE POSITION.

DOUBLE POSITION is that which discovers the true number, or number sought, by making use of two supposed numbers.

RULE.

1. Take any two numbers and proceed with them according to the conditions of the question.

2. Place each error against its respective position or supposed number; af the error be too great, mark it with +; if too small, with -

3. Multiply them cross-wise, the first position by the last error, and the

last position by the first error.

4. If they be alike, that is, both greater, or both less than the given number, divide the difference of the products by the difference of the errors, and the quotient will be the answer; but if the errors be unlike, divide the sum of the products by the sum of the errors, and the quotient will be the answer.

EXAMPLES.

1. A man lying at the point of death, left to his throe sons all his estate, riz. to F half wanting 50 dollars; to G one third; and to H the rest, which was 10 dollars less than the share of G. I demand the sum left, and each son's share.

OPERATION.

Suppose the sum 300 dollars.

Again suppose the sum 900 dollars.

Then 300+2-50=100 F's part. 300 + 3=100 G's part. G's part 100-10= 90 H's part. Then 900-2-50-400 F's part. 900+ 3=300 G's part. G's part 300-10=290 H's part.

Sum of all their parts 290

Sum of all their parts 990

Error 10-Suppose. Errors. 10-90-900 .. . 9000 27000 27000

- Dollars.

Having proceeded with the supposed numbers according to the conditions of the question, the sum of all their parts must be subtracted from the supposed number thus the 290 is subtracted from 300, the

Error 50+

supposed number, &c.

Sum of Errors. 100)36000(360 Ans.

The divisor is the sum of the errors 90+and 10-

2. There is a fish whose head is 10 feet long; his tail as long is his nead and half the length of his body, and his body as long as his head and tail; what is the whole length of the fish? Ans. 80 fe st

Of the second of the first

3. A certain man having driven his swine to market, viz. hogs, sows and pigs, received for them all £50 being paid for every hog 18s. for every sow 16s. for every pig 2s.; there were as many logs as sows, and for every sow there were three pigs; I demand how many there were of every sow there were three pigs; I demand how many there were of each sort?

4. A and B laid out equal sums of money in trade; A gained a sum equal to 1 of his stock, and B lost 225 dollars; then A's money was double that of B's; what did each one lay out?

Ans. \$600.

5. A and B have the same income, A saves 1 6f his; but B by spending 30 dollars per annum more than A, at the end of 8 years finds himself 40 dollars in debt; what is their income, and what does each spend per annum?

Ans. Their income is \$900 per ann. A spends \$175, 4 B 205 per ann.

§ 11. DISCOUNT.

DISCOUNT is an allowance made for the payment of any sum of money before it becomes due, and is the difference between that sum, due sometime hence, and its present worth.

The present worth of any sum or debt due some time hence, is such a sum as, if put to interest, would in that time and at the rate per cent for which the discount is to be made, amount to the sum or debt then due.

RULE.

As the amount of 100 dollars for the given time and rate is to 100 dollars, so is the given sum to its present worth, which subtracted from the given sum leaves the discount.

EXAMPLES.

1. What is the discount of \$321,63 due 4 years hence at 6 per cent?

2. What is the present worth of \$426 payable in '4 years and 12 days, discounting at the rate of 5 per cent?

Ans. \$354,519.

OPERATION.

Dolls.

6 interest of 100 dolls.

4 years. [1 year

24

100

124 amount.

Then, as 124: 100: 321,63

and the same of the same of the

124)32163,00**(259,37**9

321,63 given sum. 259,379 present worth.

Ans. 62,251 discount.

6 12. EQUATION OF PAYMENTS.

EQUATION OF PAYMENTS is the finding of a time to pay at once, several debts due at different times, so that neither party shall sustain loss.

RULE.

Multiply each payment by the time at which it is due; then divide the sum of the products by the sum of the payments, and the quotient will be the equated time.

EXAMPLES.

1. A owes B 136 dollars to be paid in 10 months; 96 dollars to be paid in 7 months; and 260 to be paid in 4 months; what is the equated time for the payment of the whole?

2. I owe \$65,125, to be paid \$\frac{1}{4}\$ in 3 months, \$\frac{1}{4}\$ in 5 months, \$\frac{1}{4}\$ in 10 months, and the remainder in 14 months, at what time ought the whole to be paid?

Ans. 64 months

ie:	•		
OPERATION.			
136×	10 = 1360		
96×	7 = 672		
260×	4=1040		
492	3072		
492)3072(6 i 2952	months.		
120	r to the second		
30			
492)3600(7 3444	days.		
156			

3. A merchant has owing to him £300, to be paid as follows; £50 at 2 months, £100 at 5 months, and the rest at 8 months; and it is agreed to make one payment of the whole; I demand when that time

Ans. 6 months.

must be ?

4. A merchant owes me 900 dollars, to be paid in 96 days, 130 dollars in 120 days, 500 dollars in 80 days, 1267 dollars in 27 days; what is the mean time for the payment of the whole?

and the stage of

1000 804 3

Ans. 63 days, very nearly.

13. GUAGING.

GUAGING is taking the dimensions of a cask in inches to find its contents in gallons by the following

METHOD.

- 1. Add two thirds of the difference between the head and bung diameters to the head diameter for the mean diameter; but if the staves be but little curving from the head to the bung, add only six tenths of this difference.
- 2. Square the mean diameter, which multiplied by the length of the cask, and the product divided by 294, for wine, or by 359 for ale, the quotient will be the answer in gallons.

EXAMPLES.

- 1. How many ale or beer gallons will a cask hold, whose bung diameter is 31 inches, head diameter 25 inches, and whose length is 36 inches?

 OPERATION.
- 31 Bung diam. 25 head diam.
- 25 Head diam. 4 Two thirds difference.
 - 6 Difference. 29 Mean diam.

29

961

58

841 Square of mean diam. 36 Length,

5046 2523

359)30276(£4 galls. 1414 etc.

Note 1. In taking the length of the casks, an allowance must be made for the thickness for both heads of one inch, 1½ inches, or 2 inches according to the size of the cask.

Norm 2. The head disameter must be taken close to the chimes, and for small casks, add 3 tenths of an inch; for casks of 40 or 50 gallons, 4 tenths, and for larger casks, 5 or 6 tenths, and the sum will be very nearly the head disameter within.

14. MECHANICAL POWERS.

1. OF THE LEVER.

To find what weight may be raised or balanced by any given power, Say as the distance between the body to be raised or balanced, and the fulcrum or prop, is to the distance between the prop and the point where the power is applied; so is the power to the weight which it will balance or raise.

EXAMPLE.

IF a man weighing 150lb. rest on the end of a lever 12 feet long, what weight will he balance on the other end, supposing the prop 11 feet from the weight?

12 feet the Lever.

1,5 distance of the weight from the fulcrum.

10.5 distance from the fulcrum to the man. Therefore, Feet. Feet. lb. lb.

As 1,5 : 10,5 :: 150 : 1050 Ans.

2. OF THE WHEEL AND AXLE.

As the diameter of the axle is to the diameter of the wheel, so is the power applied to the wheel, to the weight suspended by the axle.

EXAMPLES.

1. A mechanic wishes to make a windlass in such a manner, as that Ilb. applied to the wheel should be equal to 12 suspended on the axle; now supposing the axle 4 inches diameter, required the diameter of the wheel?

lb. in. lb. in.
As 1: 4:: 12: 48 Ans. or diameter of the wheel.

2. Suppose the diameter of the axle 6 inches, and that of the white 60 inches, what power at the wheel will balance 10lb. at the axle? Ass 1lb

3. OF THE SCREW.

The power is to the weight to be raised as the distance between 2 threads of the sorew is to the circumference of a circle described by the power applied at the end of the lever and the sort of the sort of the lever and the so

Norg 1: To find the vircumference of the circle described by the end of the lever, multiply the double of the lever by 3,14159, the product will be the circumference.

Note 2. It is usual to abate 4 of the effect of the machine for friction.

EXAMPLES,

There is a screw whose threads are an inch astinder; the lever by which it is turned, is 36 inches long, and the weight to be raised a ton, or 2240lb. What power or force must be applied to the end of the lever, sufficient to turn the screw that is to raise the weight?

The lever $36 \times 2 = 72 \times 3,14159 = 226,194 + the circumference.$

circumf. in. lb. lb.

Then, as 226,194 : 1 :: 2240 : 9,903

PROBLEMS.

1. The diameter of a circle being given to thing the circumference, multiply the diameter by 3,14159; the product will be the circumference.

2. To find the area of a circle, the diameter being given, multiply the

square of the diameter by ,785398; the product is the area.

3. To measure the solidity of any irregular body, whose dimensions cannot be taken, put the body into some regular vessel and fill it with water, then taking out the body, measure the fall of water in the vessel; if the vessel be square, multiply the side by itself, and the product by the fall of water, which gives the solid contents of the irregular body.

MISCELLANEOUS QUESTIONS.

THE Northern Lights were first observed in London 1560; how many years since?

2. What number multiplied by 43 produces 88150?

Ans. 2050.

3. If a cannon may be discharged twice with 6lb. of powder, how many times will 7C. 3qrs. 17lbs. discharge the same piece?

Ans. 295 times.

4. Reduce 14 guineas and £75 13s. 63d. to Federal Money.

Ans. \$317,593.

5. What is the interest of \$79,47 one year and five months?

Ans. \$6,754.

6. A owed B \$317,19, for which he gave his note on interest, bearing date July 12th, 1787. On the back of the note are these several endorsements, viz.

Oct. 17th, 1797, Received in cash \$61,10.

March 20th, 1798, Received 17Cm. beef, at \$4,33 per cwt.

Jan. 1st. 1800, Received in cash, \$84.

What was there due from A to B of principal and interest, Sept. 18th, 801?

Ans. \$144,363.

7. What cost 131 yards of fiannel at 1s. 81d. per yard? Ans. £1 3s. 01d.

8. What must I give for 3Cmt. 2qrs. 13lb. of cheese at 7 cts. per lb.?

Ans. \$28,35.

9. What will 35 yards of broadcloth cost at 23s. 6d. per yard?

Ans. £41 2s. 6d.

10. What will be the cost of a loin of veal, weighing 167th. at 21d. per lb. ?. Ans. 3s. 57d.

11. What will 871lb. of tallow cost at 91d. per lb. ? Ans. £3 7s. 3d.

12. What will 196 yards of tape cost at 3 farthings per yard?

Ans. 12s. 3d

13. What will 56 bushels of oats cost at 2s. 31d. per bushel?

Ans. £6 8s. 4d.

14. At £3 7s. 6d. per cwt. for sugar, what is that per lb.? Ans. 7d.

15. How much in length of a board that is 10 inches wide will it require to make a square foot?

Ans. 14 to feet.

16. How many square feet in a board 1 foot 3 inches wide, and 14 feet ? inches long?

Ans. 18f. 5' 3"

17. How much wood in a load 9 feet long, 31 wide, and 2 feet 9 inches high?

Ans. 86f. 7' 6"

18. At \$1,33 per yard for cloth, what must I give for 72 yards?
Ass. \$95,76.

19. If 21 cwt. of cotton wool cost £11 17s. 6d. what is that per lb? Ans. 111d.

20. If 18321 gallons of wine cost £44 6s. what is that per gallon? Ans. 54d

21. What will 531 lb. of beef cost at 5cts. 5m. per lb.? Ans. \$2,942.

22. What will 50 bushels of potatoes cost at 21 cents per bushel? Ans. \$10,50.

23. At \$10,76 per cwt. for sugar, what is that per lb. ? Ans. \$0,096.

24. What will be a man's wages for 6 months, at 43 cents per day, Ans. \$61,49. working 51 days per week?

25. What must I give for pasturing my horse 19 weeks, at 33 cents per Ans. \$6,27. week?

26. How many revolutions does the moon perform in 144 years, 2 days

10 hours. One revolution being in 27 days, 7h. 43m. Ans. 1925. 27. What will 7 pieces of cloth containing 27 yards each, come to at

15s. 41d. per yard? Ans. £145 5s. 104d.,

28. A man spends 23 dolls. 69 cents, 5 mills, in a year, what is that per Ans. \$0,064. day? 29. Suppose the Legislature of this State should grant a tax of 7 cents 3

mills on a collar, what will a man's tax be, who is 149 dollars 40 cents on Ans. \$10,395. the list?

30. A Bankrupt, whose effects are 3948 dollars, can pay his creditors but 28 cts. 5 mills on the dollar. What does he owe? Ans. \$13852,631.

31. Suppose a cistern having a pipe that conveys 4 gallons, 2qts. into it in an hour, has another that lets out 2 gallons, 1qt. 1pt. in an hour, if the cistern contains 84 gallons, in what time will it be filled? Ars. 39h. 31m, 4514a

32. If 80 deliars worth of provisions will serve 20 men 25 days, what number of men will the same provisions serve 10 days? Ans. 50 men.

33. If 6 men spend 16 dollars 7 cents in 40 days, how long will 135 men be spending 100 collars? Ans. 11 days, 1h. 30m. 18s.

34. A bridge built across a river in 6 months, by 45 men, was washed away by the current; required the number of workmen sufficient to build Ans. 135 men.

another of twice as much worth in 4 months?

35. Four men, A, B, C, & D, found a purse of money containing 12 dollars, they agree that A shall have one third, B one fourth, C one sixth and D one eighth of it, what must each man have according to this agreement? Ans. A's share \$4,5713. B's share, \$3,4284.

C's share \$2,2854. D's share, \$1,7143.

36. A certain usurer lent £90 for 12 months, and received principal and interest £958s. I demand at what rate per cent he received interest. Ans. 6 per cent.

37. If a gentleman have an estate of £1000 per annum, how much may he spend per day to lay up three score guineas at the year's end?

Ans. £2 10s, 2d. 144q. 38. What is the length of a road, which being 33 feet wide contains an acre? Ans. 80 rods in length.

39. Required a number from which if 7 be subtracted, and the remainder be divided by 8, and the quotient be multiplied by 5, and 4 added to the product, the square root of the sum extracted, and three fourths of that root cubed, the cube divided by 9, the last quotient may be 34? Apr. 103.

40. If a quarter of wheat affords 60 ten penny loaves, how many eight permy loaves may be obtained from it? Ass. 75 eight penny loaves

41. If the carriage of 7 cwt. 2qr. for 105 miles be £1 5r. how far may 5 cwt. 1qr. be carried for the same money?

Ans. 150 miles.

42. If 50 men consume 15 bushels of grain in 40 days, how much will 30 men consume in sixty days?

Ans. 131 bushels.

43. On the same supposition, how long will 50 bushels maintain 64 men?

Ans. 104 days, 4 hours.

44. A gentleman having 50s. to pay among his laborers for a day's work, would give to every boy 6d. to every woman 8d. and to every man 16d. the number of boys, women and men was the same; I demand the number of each?

Ans. 20.

45. A gentleman had £7 17s. 6d. to pay among his laborers; to every boy he gave 6d. to every woman 8d. and to every man 16d. and there were for every boy three women, and for every woman 2 men; I demand the number of each?

Ans. 15 boys, 45 women, and 90 men.

46. Three Gardeners, A, B, and C, having bought a piece of ground, find the profits of it amount to 120£ per annum. Now the sum of money which they laid down was in such proportion, that as often as A paid 5£ B paid 7£ and as often as B paid 4£ C paid 6£. I demand how much each man must have per annum of the gain? Ans. A £26 13s. 4d. B £37 6s. 8d. C £56.

47. A young man received 210£ which was 2-3ds.of his eldest brother's portion: now three times the eldest brother's portion was half the father's estate; I demand how much the estate was?

Ans. £1890.

48. Two men depart both from one place, the one goes North, and the other South; the one goes 7 miles a day, the other 11 miles a day; how far are they distant the 12th day after their departure?

Ans. 216 miles.

49. Two men depart both from one place, and both go the same road the one travels 12 miles every day, the other 17 miles every day; how far are they distant the 10th day after their departure?

Ans. 50 miles.

50. The river Po is 1000 feet broad, and 10 feet deep, and it runs at the rate of 4 miles an hour. In what time will it discharge a cubic mile of water (reckoning 5000 feet to the mile) into the sea? Ans. 26 days, 1 hour.

51. If the country which supplies the river Po with water, be 380 miles long and 120 broad, and the whole land upon the surface of the earth be 62,700,000 square miles, and if the quantity of water discharged by the rivers into the sea be every where proportional to the extent of land by which the rivers are supplied; how many times greater than the Po will the whole amount of the rivers be?

Ans. 1375 times.

52. Upon the same supposition, what quantity of water altogether will be discharged by all the rivers into the sea in a year? Ans. 19272 cubic miles.

53. If the proportion of the sea on the surface of the earth to that of land be as $10\frac{1}{2}$ to 5, and the mean depth of the sea be a quarter of a mile; how many years would it take if the ocean were empty to fill it by the rivers running at the present rate?

Ans. 1708 years, 17 days, and 12 hours.

54. If a cubic foot of water weigh 1000 oz. avoirdupois, and the weight of mercury be 13½ times greater than of water, and the height of the mercury in the barometer (the weight of which is equal to the weight of a column of air on the same base, extending to the top of the atmosphere) be 30 inches; what will be the weight of the air upon a square foot? a square mile? and what will be the whole weight of the atmosphere, supposing the size of the earth as in questions 51 and 53?

Ans. 2109,375 pounds weight on a square foot.
52734375000 - - square miles,
10249980468750000000 - - of the whole atmosphere.

55. A began trade June 1, with 40 dollars, and took in B as a partner, Sept. 8, following, with 120 dollars; on Dec. 24, A put in 190 dollars more, and continued the whole in trade till May 5, following, when their whole gain was found to be 82 dollars; what is each partner's share?

Ans. A's share \$47,065+B's share \$34,934+

56. If I give 80 bushels of potatoes at 21 cents per bushel, and 240lb. of flax, at 15 cents per lb. for 64 bushels of salt, what is the salt per bushel? Ans. \$0,825.

57 What is the present worth of 482 dollars, payable 4 years hence, dis Ans. \$388,709.

counting at the rate of 6 per cent?

53. I have owing to me as follows: viz. \$18,73 in 8 months: \$46,00 in 5 months; and 104,84 in 3 months; what is the mean time for the payment Ans. 4 months 2 days. of the whole?

59. If I sell 500 deals at 15d. a piece, and lose £9 per cent, what do I Ans. £2 16s. 3d. lose in the whole quantity?

60. If I buy 1000 Ells Flemish of linen for £90, what may I sell it per Ell in London, to gain £10 in the whole? Ans. 3s. 4d.

61. How many wine gallons in a cask, whose bung diameter measures

27 inches, head diameter 21 inches, and length 30 inches?

Ans. 63 gals. 3qts.

- 62. A military officer drew up his soldiers in rank and file, having the number in rank and file equal; on being reinforced with three times his first number of men, he placed them all in the same form, and then the number in rank and file was just double what it was at first; he was again reinforced with three times his first number of men, and after placing the whole in the same form as at first, his number in rank and file was 40 men each; How many men had he at first? Ans. 100.
- 63. Two ships A and B sailed from a certain port at the same time; A sailed north 8 miles an hour, and B east 6 miles an hour; What was their distance at the end of one hour? Ans. 10 miles.
- 64. A hare starts 12 ruds before a hound; but is not perceived by him until she has been up 45 seconds; she scuds away at the rate of ten miles an hour, and the dog on view, makes after at the rate of 16 miles an hour. How long will the hound be in overtaking the hare, and what distance will he run? Ans. 974 seconds, he will run 2288 feet.
- 65. A fellow said that when he counted his nuts two by two, three by three, four by four, five by five, and six by six, there was still an odd one, but when he counted them seven by seven they came out even; How many had he? Ans. 721.

66. There is an island 50 miles in circumference, and three men start together to travel the same way about it; A goes 7 miles per day, B 8, and C 9; when will they all come together again, and how far will they trav-Ans. 50 days. A 350 miles. B 400, and C 450.

67. If a weight of 1440lb. be placed 1 foot from the prop, at what distance from the prop must a power of 160lb. be applied to balance it?

Ans. 9 feet. '68. Sound, uninterrupted, moves about 1142 feet in a second; supposing in a thunder storm, the space between the lightning and thunder be six seconds; at what distance was the explosion?

Ans. 1 mile, 94 rods, 21 feet

Ans. 19000.

- 69. A cannon ball at the first discharge, flies about a mile in eight seconds; at this rate, how long would a ball be in passing from the Earth to the Sun, it being, as astronomers well know, 95173000 miles distant?
- Ans. 24 years, 46 days, 7 hours, 33m. 20s.

 70. A general disposing his army into a square battalion, found he had
 231 over and above; but increasing each side with one soldier, he wanted
 44 to fill up the square; Of how many men did his army consist?

71. A and B cleared by an adventure at sea 45 guineas, which was £35 per cent upon the money advanced, and with which they agreed to purchase a genteel horse and carriage, whereof they were to have the use in proportion to the sums adventured, which was found to be 11 to A, as often as 8 to B; what money did each adventure?

Ans. A £104 4s. 214d. B £75 15s. 91sd.

72. Tubes may be made of gold weighing not more than at the rate of 111s of a grain per foot; what would be the weight of such a tube, which would extend across the Atlantic from Boston to London, estimating the distance at \$000 miles?

Ans. 20s. Speed. 3Afgr

PLEASING AND DIVERTING QUESTIONS.

- 1. There was a well 30 feet deep; a frog at the bottom could jump up 3 feet every day, but he would fall back two feet every night. How many days did it take the frog to jump out?
- 2. Two men were driving sheep to move as you; the other says, give me one of yours and I shall have as many as you; the other says, give me one of yours and I shall have as many again as you. How many had each?
 - 3. As I was going to St. Ives,
 I met seven wives,
 Every wife had seven sacks,
 Every sack had seven cats,
 Every cat had seven kits,
 Kits, cats, sacks and wives,
 How many were going to St. Ives?
- 4. The account of a certain school is as follows, viz. 1-16 of the boys learn geometry, 3-8 learn grammar, 3-10 learn arithmetic, 3-20 to write, and 9 learn to read: I demand the number of each?
- 5. A man driving his geese to market, was met by another, who said, Good morrow master, with your hundred geese; says he, I have not an hundred, but if I had half as many as I now have, and two geese and a half beside the number I now have already, I should have an hundred. How many had he?

Cc

- 6. Three travellers met at a Caravansary, or inn in Persia; and two of them brought their provision along with them, according to the custom of the country; but the third not having provided any, proposed to the others that they should eat together, and he would pay the value of his proportion. This being agreed to, A produces 5 loaves, and B 3 loaves, which the travellers eat together, and C paid 8 pieces of money as the value of his share, with which the others were satisfied, but quarrelled about the dividing of it. Upon this, the affair was referred to the judge, who decided the dispute by an impartial sentence. Required his decision?
- 7. Suppose the 9 digits to be placed in a quadrangular form; I demand in what order they must stand, that any three figures in a right line may make just 15?
- 8. A countryman having a Fox, a Goose, and a peck of corn, in his journey, came to a river, where it so happened that he could carry but one over at a time. Now as no two were to be left together that might destroy each other; so he was at his wits end how to dispose of them; for says he, tho' the corn can't eat the goose, nor the goose eat the fox; yet the fox can eat the goose, and the goose eat the corn. The question is, how he must carry them over that they may not devour each other?
- 9. Three jealous husbands with their wives, being ready to pass by night over a river, do find at the water side a boat which can carry but two persons at once, and for want of a waterman they are necessitated to row themselves over the river at several times: The question is, how those six persons shall pass by 2 and 2, so that none of the three wives may be found in the company of one or two men, unless her husband be present?
- 10. Two merry companions are to have equal shares of 8 gallons of wine, which are in a vessel containing exactly 8 gallons; now to divide it equally between them, they have only two other empty vessels, of which one contains 5 gallons, and the other 3: The question is, how they shall divide the said wine tween them by the help of these three vessels, so that they may have four allons apiece?

SECTION IV.

FORMS OF NOTES, DEEDS, BONDS, AND OTHER INSTRUMENTS OF WRITING.

6 1. OF NOTES.

No. I.

Overdean, Sept. 17, 1802.—For value received I promise to pay to Otsver Bountiful, or order, sixty three dollars fifty four cents, on demand, with interest after three months.

Attest, Timothy Testimony.

No. II.

Bilfort, Sept. 17, 1802.—For value received, I promise to pay to O. R. or bearer—dollars—cents, three months after date.

Peter Percept.

No. III.

By two Persons.

Arian, Sept. 17, 1802.—For value received, we jointly and severally promise to pay to C. D. or order,—Godollars,—Godollars,—cents, on demand with interest.

Attest, Constance Adley.

ALDEN FAITHFUL.
JAMES FAIRFACE.

OBSERVATIONS.

1. No note is negotiable unless the words, or order, otherwise or bearer, be inserted in it.

2. If the note be written to pay him "or order," (No. 1.) then Officer Bountiful may endorse this note, that is, write his name on the backside and sell it to A, B, C, or whom he pleases. Then A, who buys the note, calls on William Trusty for payment, and if he neglects, or is unable to pay, A may recover it of the endorser.

3. If a note be written to pay him "or bearer," (No. 2.) then any person who holds the note may sue and recover the same of Peter Pencil.

4. The rate of interest established by law, being six per cent per annum, it becomes unnecessary in writing notes to mention the rate of interest; it is sufficient to write them for the payment of such a sum, with interest, for it will be understood legal interest, which is six per cent.

5. All notes are either payable on demand or at the expiration of a certain term of time agreed upon by the parties and mentioned in the note, as

three months, a year, &c.

6. If a bond or note mention no time of payment, it is always on demand, whether the words, on demond, he expressed or not

7. All notes payable at a certain time are on interest as soon as they become due, though in such notes there be no mention made of interest.

This rule is founded on the principle that every man ought to receive his money when due, and that the non payment of it at that time is an injury to him. The law, therefore, to do him justice, allows him interest from the time the money becomes due, as a compensation for the injury.

8.) Upon the same principle a note payable on demand, without any mention made of interest, is on interest after a demand of payment, for upon

demand such notes immediately become due.

9. If a note be given for a specific article, as rye, payable in one, two, or three months, or in any certain time, and the signer of such note suffers the time to elapse without delivering such article, the holder of the note will not be obliged to take the article afterwards, but may demand and recover the value of it in money.

2. OF BONDS

A BOND WITH A CONDITION FROM ONE TO ANOTHER.

KNOW all men by these presents, that I, C. Q. of so in the county of sc. am held and firmly bound to E. F. of &c. in two hundred dollars, to be paid to the said E. F. or his certain attorney, his executors, administrators or assigns, to which payment, well and truly to be made, I hind myself, my heirs, executors and administrators, firmly by these presents; Sealed with my seal. Dated the eleventh day of in the year of our Lord one thousand eight hundred and two.

The Condition of this obligation is such, that if the above bound C. D. his heirs, executors, or administrators, do and shall well and truly pay, or cause to be paid unto the above named E. F. his executors, administrators of assigns, the full turn of two hundred dollars, with legal interest for the tame, on or before the eleventh day of—next ensuing the date hereof: Then this obligation to be void, or otherwise to remain in full force and virtue.

Signed, &c.

A Condition of a Counter Bond, or Bond of Indemnity, where one man becomes bound for another.

Note. The principal difference between a note and a bond, is that the latter is an instrument of more solemnity, being given under seal. Also, a note may be controuled by a special agreement, different from the note, whereas in case of a bond, no special agreement can in the least controul what appears to have been the intention of the parties as expressed by the words in the condition of the bond.

§ 3. OF RECEIPTS.

No.\L

Sitgrieves, Sept. 19, 1802. Received from Mr. Duranes Adley, ten dollars in fall of all accounts.

ORVAND CONSTANCE.

No. II.

Sitgrieves, Sept. 19, 1802. Received of Mr Orvand Constance, five dollars in full of all accounts.

DURANCE ADLEY.

No. III.

Receipt for an endorsement on a Note.

Sitgrieves, Sept. 19, 1802. Received of Mr. Simpson Eastly, (by the hand of Titus Trusty) sixteen dollars twenty five cents, which is endorsed on his note of June 3, 1802.

PETER CHEERFUL.

No. IV.

A Receipt for money received on account.

Sitgrieves, Sept. 19, 1802. Received of Mr. Orand Landike, fifty dollars on account.

ELDRO SLACKLEY.

No. V.

Receipt for interest due on a Bond.

Received this ____day of ____of Mr. A. B. the sum of five pounds in full of one year's interest of £100 due to me on the ____day of ____last on bond from the said A. B. I say received. By me C. D.

OBSERVATIONS.

1. There is a distinction between receipts given in full of all accounts; and others in full of all demands. The former cut off accounts only; the latter cut off not only all accounts, but all obligations and right of action.

2. When any two, persons make a settlement and pass receipts (No. I. and II.) each raceipt must specify a particular st in received, less of more It is not necessary that the sum specified in the receipt, he the exact sum received.

§ 4. OF ORDERS.

No. I.

Mr. Stephen Burgess,

my account.

Samuel Smin 9 1802

Archdale, Sept. 9, 1802.

No. II.

SIR, Boston, Sept. 9, 1802.

For value received, pay G. R. eighty six cents, and this with his receipt shall be your discharge from me.

NICHOLAS REVERS.

To Mr. James Robottom.

§ 5. OF DEEDS.

No. I.

A Warrantee Deed.

KNOW ALL MEN BY THESE PRESENTS, That I, Peter Careful, of Leominster, in the County of Worcester, and Commonwealth of Massachusetts, gentleman, for and in consideration of one hundred and fifty dollars, and forty five cents, paid to me by Samuel Pendleton of Ashby, in the County of Middlesex, and Commonwealth of Massachusetts, yeoman, the receipt whereof I do hereby acknowledge, do hereby give, grant, sell and convey to the said Samuel Pendleton, his heirs and assigns, a certain tract and parcel of land, bounded as follows, viz.

[Here insert the bounds, together with all the privileges and appurtenances

thereunto belonging.]

To have and to hold the same unto the said Samuel Pendleton, his heirs and assigns to his and their use and behoof forever. And I do covenant with the said Samuel Pendleton, his heirs and assigns, that I am lawfully seized in see of the premises, that they are free of all incumbrances, and that I will warrant and will defend the same to the said Samuel Pendleton, his heirs and assigns forever, against the lawful claims and demands of all persons.

In witness whereof, I hereunto set my hand and seal this day of

in the year of our Lord one thousand eight hundred and two.

Signed, sealed and delivered \ Peter Careful, O

in presence of L. R. F. G.

No. II.

Quitclaim Deed.

Know all Men by these presents, That I, A. B. of, &c. in consideration of the sum of—to be paid by C. D. of &c. the receipt whereof I do hereby acknowledge, have remissed, released, and forever quitclaimed, and do by these presents remit, release, and forever quitclaim unto the said C. D. his heirs and assigns forever (Here insert the premises.) To have and to hold the same, together with all the privileges and appurtenances thereunto belonging, to him the said C. D. his heirs and assigns forever.—b. witness, &c.

No. III. A Mortgage Deed.

KNOW ALL MEN BY THESE PRESENTS, That I Simpson Easley, of in the County of in the State of Blacksmith, in consideration of Dollars—Cents, paid by Elvin Fairface of in the county of —— in the State of —— Shoemaker, the receipt whereof I do hereby acknowledge, do hereby give, grant, sell and convey unto the said Elvin Fairface, his heirs and assigns, a certain tract and parcel of land, bounded as follows, viz. (Here insert the bounds, together with all the privileges and appurtenances thereunto belonging.) To have and to hold the afore granted premises to the said Elvin Fairface, his heirs and assigns. to his and their use and behoof forever. And I do covenant with the said Elvin Fairface, his heirs and assigns, That I am lawfully seized in fee of the afore granted premises. That they are free of all incumbrances: That I have good right to sell and convey the same to the said Elvin Fair-And that I will warrant and defend the same premises to the said Elvin, his heirs and assigns forever, against the lawful claims and demands of all persons. Provided nevertheless, That if I the said Simpson Easley, my heirs, Executors, or administrators shall well and truly pay to the said Elvin Fairface, his heirs, executors, administrators or assigns, the full and just sum of——dollars——cents on or before the— ----which will be in the year of our Lord eighteen hundred andwith lawful interest for the same until paid, then this deed, as also a certain bond [or note, as the case may be] bearing even date with these presents given by me to the said Fairface, conditioned to pay the same sum and interest at the time aforesaid, shall be void, otherwise to remain in full force and virtue. In witness whereof, I the said Simpson and Abigail py wife, in testimony that she relinquishes all her right to dower or alimony in and to the above described premises, hereunto set our hands and seals this --day of - in the year of our Lord one thousand eight handred and five.

Signed, sealed and delivered }
in presence of
L. N. V. X.

SIMPSON EALEY. O ARIGAIL DASLEY. O

§ 6. OF AN INDENTURE.

· A common Indenture to bind an Apprentics.

THIS Indenture witnesseth, That A. B. of, &c. ham put and placed, and by these presents doth put and bind out his son C. D. and the said C. D. doth hereby put, place and bind out himself, as an apprentice to R. P. to learn the art, trade, or mystery of ______ The said C. D. after the manner of an apprentice, to dwell with and serve the said R. D. from the day of the date hereof, until the ______ day of _____ which will be in the year of our Lord one thousand eight hundred and ______ which time the said apprentice, if he should be living, will be twenty one years of age: During which time or term the said apprentice his said master well and faithfully shall serve; his secrets keep, and his lawfal commands every where, and at all times readily obey. He shall do no damage to his said master, nor wilfully suffer any to be done by others; and if any to his knowledge be intended, he shall give his master seasonable notice thereof. He shall not waste the goods of his said master nor lend them unlawfully to any; at cards, dice, or any unlawful game he shall not play; fornication he shall not commit, nor matrimony contract during the said term; taverns, ale houses, or places of gaming he shall not haunt or frequent. From the see-

vice of his said master he shall not absent himself; but in all things, and at all times he shall carry and behave himself as a good and faithful apprentice

ought, during the whole time or term aforesaid.

And the said R. P. on his part doth hereby promise, covenant and agree to teach and instruct the said apprentice, or cause him to be taught and instructed in the art, trade or calling of a——by the best way or means he can, and also teach and instruct the said apprentice, or cause him to be taught and instructed to read and write, and cypher as far as the rule of Three, if the said apprentice be capable to learn, and shall well and faithfully find and provide for the said apprentice, good and sufficient meat, trink, cloathing, lodging a better necessaries fit and convenient for such an apprentice, during the term aforesaid, and at the expiration thereof, shall give unto the said apprentice, two suits of wearing apparel, one suitable for the Lord's day, and the other for working days.

In testimony whereof, the said parties have hereunto interchangeably set their hands and seals, this said——day of——in the year of our Lord one thousand eight hundred and—— (Seal)

Signed, sealed and delivered in presence of

(Seal)

9.7. OF A WILL.

The form of a Will with a Devise, of a Real Estate, Lease-hold, &c.

In the name of God, Amen, I, A. B. of, &c. being weak in body, but of sound and perfect mind, and memory, (or you may say thus, considering the uncertainty of this mortal life, and being of sound, &c.) blessed be Almighty God for the same, do make and publish this as my last Will and Testament in a mainer and form following (that is to say) First, I give and bequeath unto my elest son G. B. the sum of I do also give and bequeath unto my elest son G. B. the sum of I do also give and bequeath unto my two younger sons J. B. and F. B. the sum of apiece. I also give and be neath to my daughter in law, S. H. H. single woman, the sum of which said several legacies or sums of money, I will and order shall be paid to he said respective legatees within six months after my decease. I further give and devise to my said eldest son G. B. his heirs and assigns, All that my messuage or tenement, situate, lying and being in &c. together with all my other freehold estate whatsoever, to hold to him the said G. B. his heirs and assigns forever. And I hereby give and bequeath to my said younger sons J. B. and F. B. all my leasehold estate of and in all those messuages or tenements, with the appurtenances, situate &c. equally to be divided between them. And lastly, as to all the rest, residue and remainder of my personal estate, goods and chattels, of what kind and nature soever, I give and bequeath the same to my said beloved wife J. B. whom I hereby appoint sole executrix of this my last Will and Testament; and hereby revoking all former Wills by me made.

In witness whereof, I hereum set my hand and seal, this——day of—in the year of our Lord——

W. T. T. W.

Signed, sealed, published and declared by the above named

A. B. to be his last Will and Testament in the presence of us,
who have hereunto subscribed our names as witnesses, in the
presence of the testator,

W. T.

VULGAR FRACTIONS.

ULGAR FRACTIONS are parts of an unit, or integer; and are represented by two numbers, placed one above the other, with a line drawn between them.

The number above the line is called the numerator, and that below the line the denominator.

The denominator shews how many parts an integer is divided into, and the numerator shews how many of those parts are meant by the fraction

Fractions are either proper, improper, compound, or mixed.

A proper fraction is when the numerator is less than the denominator.; as 1, 1, 17, &c.

An improper fraction is when the numerator is greater than the denominator; as 5, 1, 11, &c.

A compound fraction is the fraction of a fraction, coupled by the word of; as \ of \ , &c.

A mixed number or fraction is composed of a whole number and a fraction; as 71, 284, &c.

Reduction of Vulgar Fractions

I. To reduce a given fraction to its lowest terms RULE.

Divide both the numerator and the denominator by some one number that will divide them both without a remainder divide the quotients in the same manner, and so on till no number greater than 1 will divide them both, and the last quotients express the fraction in its lowest terms

1. Reduce ### to its lowest terms. 4) 3) Thue, 8 211 = 21 = 2 the Answer.

- 2. Reduce 111 to its lowest terms.
- 3. Reduce 37 to its lowest terms.
- 4. Reduce 3417 to its lowest terms.

Are. 11

Or :- Find a common measure, thus,

Divide the denominator by the numerator, and that divisor by the remainder, continuing so to do till nothing remains; the last divisor the common measure; then divide both terms of the fraction by the common measure, * and the quotients will express the fraction required.

1 Reduce 1111 to its lowest terms. 1080)1224(1

1080

144)1080(7 1008

Common Measure.

72)144(2

Then 72) 1888 (14 the Answer.

2. Reduce 302 to its lowest terms.

Ans. 11

II. To reduce a mixed number to an improper fraction.

RULE.

Multiply the whole number by the denominator of the fraction, and to the product add the numerator for a new numerator, and place it over the denominator.

1. Reduce 1274 to an improper fraction.

127 17 889 127 Numerator, 4 Here we multiply the whole number, 127 by 17 the denominator of the fraction, adding in the numerator 4 the sum 2163 is the numerator to the fraction sought, and 17 the denominator, so that 2142 is the improper fraction, equal to 127 47.

And the second of the second

2 Reduce 653 3 to an improper fraction.

Ans, 1249 .

III. To reduce an improper fraction to its proper terms, or mixed number.

RULE.

Divide the numerator by the denominator, the quotient will be the whole number, and the remainder, if any, will be the numerator to the given denominator.

EXAMPLES.

1. Reduce 🛂 to a mixed number.

6) 15(23 Aus.

2. Reduce 245 to its proper terms.

Ans. 274.

3. Reduce * 143 to a mixed number.

Ans. 127 A.

4. Reduce 1240 to a mixed number.

Ans. 653 ...

^{*} If the common measure happens to be 1, the fraction is already in its lowest terms.

IV. To find the least common multiple of two or more numbers.

RULE

Divide by any number that will divide two, or more, of the given numbers without a remainder, and set the quotients, together with the undivided numbers, in a line underneath.

Divide these quotients and undivided numbers as before, and so on, till there are no two numbers that can be divided; then the continued product of the divisors and the last quotients together will be the least common multiple required.

EXAMPLES.

1. What is the least common multiple of 9, 8, 15 and 16 ?

Then $8\times3\times3\times5\times2=720$ Ans.

- 2. What is the least number that 3, 5, 8, and 10 will measure?

 Aug. 120.
- 3. What is the least number that can be divided by the nine digits without a remainder?

 Ans. 2520.
 - V. To reduce a compound fraction to a single one.

RULE.

Multiply all the numerators together for a new numerator, and all the denominators for a new denominator, then reduce the new fraction to its lowest term by Case I.

EXAMPLES.

1. Reduce $\frac{3}{4}$ of $\frac{4}{16}$ to a single fraction. $3\times5\times9$

$$\frac{3\times5\times9}{-\frac{134}{4\times6\times10}}$$
 Answer.

2. Reduce 4 of 4 of 15 to a single fraction.

Ans. 114.

3. Reduce 13 of 13 of 15 of 20 to a simple (or improper) fraction.

Ans. 4112=27.

VI. To reduce fractions of different denominations to equivalent fractions having a common denominator.

RULE.

Multiply each numerator into all the denominators, except its own, for a new numerator, and all the denominators into each other, continually, for a common denominator.

^{*} Any whole number may be reduced to an improper fraction, by placing 1 under it for a denominator, which must be done in this case, thus 2.0.

EXAMPLES.

1. Reduce 1, 2 and 1 to equivalent fractions, having a common denominator.

1×5×8=40 the new numerator for ‡
2×4×8=64 for ‡
5×4×5=100 for ‡

4×5×8=160 the common denominator:

Hence the new equivalent fractions are 10, 100 and 100 the answer

2. Reduce $\frac{1}{4}$, $\frac{3}{4}$ of $\frac{3}{6}$, $7\frac{3}{4}$, and $\frac{3}{12}$ to a common denominator.

Ans. 930, 1040, 14508, 439.

3. Reduce $\frac{11}{12}$, $\frac{3}{4}$ of $2\frac{1}{2}$, $\frac{7}{12}$, and $\frac{5}{4}$ to a common denominator.

Ans. \$445, \$1500, 6720, and 7200.

VII. To reduce a fraction of one denomination to the fraction of another, but greater, retaining the same value.

RULE.

Reduce the given fraction to a compound one by comparing it with all the denominations between it and that denomination you would reduce it to; then reduce that compound fraction to a simple one, by Case V.

A CARROLL EXAMPLES. THE WAS A CONTROL OF THE PARTY OF

1. Reduce ‡ of a penny to the fraction of a pound.

By comparing it, the compound fraction will be $\frac{7}{4}$ of $\frac{1}{18}$ of $\frac{1}{20}$. Then $7 \times 1 \times 1$

 $=_{15}^{7}_{10} \text{ of a pound, the Answer.}$ $8 \times 12 \times 20$

2. Reduce s of a pound Avoirdupois to the fraction of 1 cwt.

Ans. 1 Cwt.

3. Reduce 4 of a Pennyweight to the fraction of a pound Troy.

Ans. 310 lb.

4. Reduce 4 of a penny to the fraction of a Guinea.

Ans. - Grinel.

VIII. To reduce the fraction of one denomination to the fraction of another but less, retaining the same value.

RULE.

Reduce the given fraction to a compound one, as in the preceding case, only observing to invert the parts contained in the integer; then reduce this compound fraction to a simple one, and that to its lowest terms.

EXAMPLES. The second of the Additional Control of the

1. Reduce 1720 of a pound to the fraction of a penny.

Thus $\frac{7}{1920}$ of $\frac{2}{1}$ of $\frac{1}{4}$. Then $\frac{7}{1920\times 12}$ $\frac{1980}{1920\times 12}$ $\frac{1}{1920}$ $\frac{1}{1}$ $\frac{1}{1920}$ $\frac{1}{1920}$ $\frac{1}{1}$ $\frac{1}{1920}$ $\frac{1}{1920}$

2. Reduce Ties of a pound to the fraction of a farthing.

Ans. 3q.

3. Reduce $\frac{7}{1030}$ of a lb Troy to the fraction of a pwt.

Ans. I pwt.

4. Reduce 4 * of a guinea to the fraction of a pound. Ant. 16.

^{*} Compared thus 4 of 28 of 3.

IX. To find the value of a fraction in the known parts of the integer.

BULE.

Multiply the numerator by the parts in the next inferior denomination, and divide the product by the denominator; and if any thing remain, multiply it by the next inferior denomination and divide as before, and so on, as far as necessary; the several quotients will be the answer.

EXAMPLES.

1. What is the value of 4 of a pound?

$$\begin{array}{r}
20 \\
\hline
3)40 \\
\hline
13s.-1 \\
12 \\
\hline
3)12 \\
4d.
\end{array}$$

Ans. 13s. 4d.

Multiply the numerator of the fraction (2) by 20, the number of shillings in a pound; the product, (40) divided by 3, the denominator, gives 13, the number of shillings, and I remaining, being multiplied by 12 the number of pence in a shilling, and the product, (12) divided as before by 3, gives 4, the number of pence, and no remainder. Hence the answer, 13s. 4d.

2 What is the value of ? of a pound Troy?

Ans. 7 oz. 4 pwt.

3. What is the value of 4 of a pound Avoirdupgis?

Ans. 12 oz. 124 dr.

4. Reduce 4 of a mile to its proper quantity.

Ans. 6 fur. 16 poles.

X. To reduce any given quantity to the fraction of a greater denomination of the same kind.

RULE.

Reduce the given quantity to the lowest denomination mentioned for a numerator; then reduce the integral part to the same denomination for a denominator, which placed under the numerator before found will express the fraction required.

STOREST CONTRACTOR STATES OF SEXAMPLES: 11

1. Reduce 16s. 8d. to the fraction of a pound.

1£. Integral part.

16s. 8d.

20

20 200 Numerator. 12

and the second

240 Denominator.

Ans. 318-1£.

- 2. Reduce 6 furlongs and 16 poles to the fraction of a mile.
- 3. Reduce 12 oz. 124 dr. to the fraction of a possid Avoirdupeis.

 Aus. 4 of a pound

Addition of Vulgar Fractions.

RULE.

Reduce compound fractions to single ones, mixed numbers to improper fractions, and fractions of different integers to those of the same, and all of them to a common denominator; then the sum of the numerators written over the common denominator will be the sum of the fraction required.

EXAMPLES.

1. Add \$, 9 \, and \$ of \ \text{together.}

First, the mixed number 91—4; the compound fraction 3 of 1—3. Then the fractions are 3, 4 and 3; which reduce to a common denominator.

 $3 \times 5 \times 6 = 90$ $46 \times 7 \times 6 = 1932$ $2 \times 7 \times 5 = 70$ $7 \times 5 \times 6 = 2922 = 91$

 $7 \times 5 \times 6 = \frac{2993}{210} = 9\frac{1}{10}\frac{3}{2}$ Answer. 2. Add $1\frac{1}{12}$, $2\frac{1}{12}$, $3\frac{1}{12}$ and $14\frac{1}{12}$ together.

Ans. 22.

3. Add 1£. 3s. and 4d. together.

Ans. 2s. 8 4.d.

4. Add ? of 17£. 9f£. and ? of 1 of \$£. together.

Ans. 16£. 12s. 34d.

Subtraction of Vulgar Fractions

RULE.

Prepare the fractions as in addition, and the difference of the numerators written above the common denominator will give the difference of the fractions required.

To subtract a fraction from a whole number; from the denominator of the fraction subtract the numerator and place the remainder over the denominator: then deduct 1 from the integer or whole number.

EXAMPLES.

1. From ## take #.— 49× 9—441 5×50—250

50 × 9=450 com. denom.

Therefore 441-448-411 the Answer

2. From 131 take 2 of 15.

Ans. $2\frac{1}{12}$.

3. From 2£. take 2 of a shilling.

Ans. 14s. 3d.

4 From 7 weeks take 970 days.

Ans. 5w. 4d. 7h. 12m.

5 From 3 take A.

Aris. 214.

Multiplication of Vulgar Fractions.

RULE.

Reduce compound fractions to simple ones, and mixed numbers to improper fractions; then multiply the numerators together for a new numerator, and the denominators for a new denominator.

EXAMPLES.

1. Multiply 41 by 1.

 $4\frac{1}{2}$. Then $\frac{9\times 1}{2\times 8}$ the Answer.

2. Multiply 1 of 5 by 3 of 4.

4. Multiply A by 4 of 3 of 3.

Ans. 4. Ans. 672 A.

3. Multiply 483 by 134.

Ans. 🛧

Division of Vulgar Fractions.

RULE.

Prepare the fractions, as already directed; then invert the divisor and proceed as in multiplication.

EXAMPLES.

1. Divide $\frac{4}{7}$ by $\frac{7}{9}$.

The divisor $\frac{7}{9}$ inverted will be $\frac{1}{9}$. Then $\frac{4\times3}{7\times2}$

2 Divide 5 by 7.

Ans. 74.

3. Divide 91 by 1 of 7.

Ans. 217.

Divide # by 9.
 Divide 7 by #.

Ans. 11.
Ans. 184.

3 Divide 52051 by 4 of 91.

Ans. 714.

Rule of Three Direct in Vulgar Fractions

RULE.

Having stated the question, make the necessary preparations, as in Reduction of Fractions, and invert the first term; then proceed as in Multiplication of Fractions.

EXAMPLES

 If i of a yard cost i of a pound what will i of an ell English come to, at the same rate?

First, reduce the 1 of a yard to the fraction of an EH English; thus 1 of of 1 E. Eng.

E. E. E.E. Then, as 4 : 1 :: 3. Invert the first term, and proceed as in Multiplication-

Thus $\frac{20 \times 2 \times 3}{4 \times 3 \times 5} = 60$ £2. 0 0.

- 2. If \(\frac{1}{2}\) yd. cost \(\frac{1}{2}\)E. what will 40\(\frac{1}{2}\) yds. come to ? Ans. \(\frac{1}{2}\)59 1s. 3d.
- 3. If 7 of a ship cost £51, what are 2 of her worth? Ans. £10 18s. 6d. 34q.
- 4. At £34 per Cwt. what will 92 lb come to?

 Ans. 6s. 35 d.

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Commence of the state of the state of

- 5. If \(\frac{1}{2}\) yd. cost \(\frac{1}{2}\) of a \(\frac{1}{2}\). what will \(\frac{1}{2}\) Ell English cost? Ans. 17s. 1d; 2819
- 6. A man owning \$ of a farm, sells \$ of his share for £171; what is the whole farm valued at? Ans. £380. Same of march of the grant of the &

Rule of Three Inverse in Vulgar Fractions. EXAMPLES.

- 1. If 254s. will pay for the carriage of an Cwt. 1451 miles, how far may 61 Cwt. be carried for the same money? Ans. 22 miles.
- 2. If the penny white-loaf weigh 7 oz. when a bushel of wheat cost 5s. 6d. what is the bushel worth when the penny white-loaf weights 21 oz.?
- 3. How much shalloon, that is 3 yard wide, will line 63 yards of cloth this is 14 yard wide? Ans. 111 yarıls

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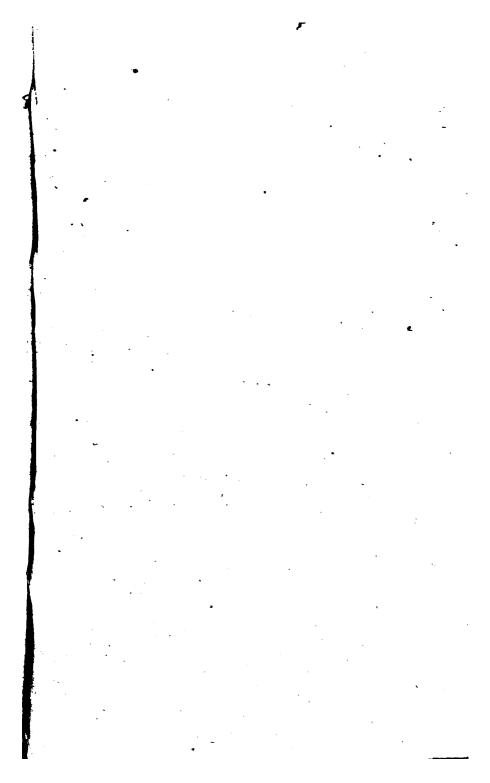
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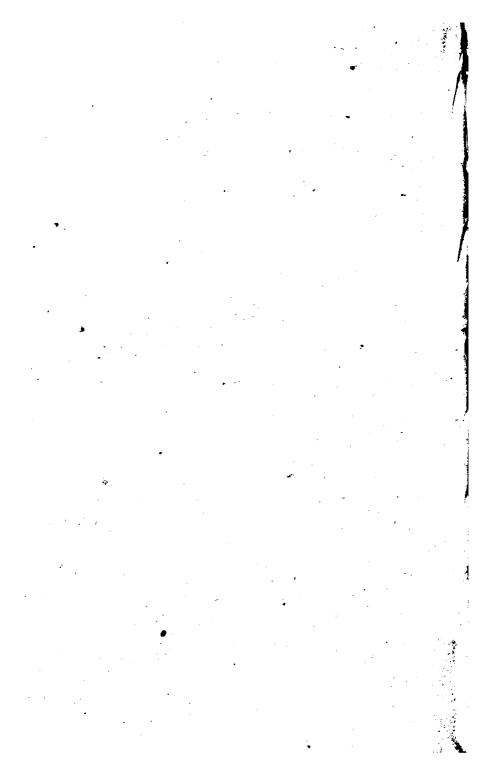
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